

# Package: highfrequency (via r-universe)

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**Title** Tools for Highfrequency Data Analysis

**Description** Provide functionality to manage, clean and match highfrequency trades and quotes data, calculate various liquidity measures, estimate and forecast volatility, detect price jumps and investigate microstructure noise and intraday periodicity. A detailed vignette can be found in the paper ``Analyzing Intraday Financial Data in R: The highfrequency Package'' by Boudt, Kleen, and Sjoerup (2022, <doi:10.18637/jss.v104.i08>). The DOI in the CITATION is for a new Journal of Statistical Software publication that will be registered after publication on CRAN. A working paper version can be found on SSRN: <doi:10.2139/ssrn.3917548>.

**License** GPL (>= 2)

**Encoding** UTF-8

**LazyData** true

**URL** <https://github.com/jonathancornelissen/highfrequency>

**BugReports** <https://github.com/jonathancornelissen/highfrequency/issues>

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**LinkingTo** Rcpp, RcppArmadillo

**Suggests** mvtnorm, covr, FKF, rugarch, testthat, knitr, rmarkdown

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**Repository** <https://jonathancornelissen.r-universe.dev>

**RemoteUrl** <https://github.com/jonathancornelissen/highfrequency>

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highfrequency-package *highfrequency: Tools for Highfrequency Data Analysis*

---

## Description

The **highfrequency** package provides numerous tools for analyzing high-frequency financial data, including functionality to:

- Clean, handle, and manage high frequency trades and quotes data.
- Calculate liquidity measures
- Calculate (multivariate) realized measures of the distribution of high-frequency returns
- Estimate models for realized measures of volatility and the corresponding forecasts
- Detect jumps in prices
- Analyze market microstructure noise in asset prices
- Estimate spot volatility and drift as well as analyze intraday periodicity of spot volatility

## Author(s)

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Thanks: We would like to thank Brian Peterson, Chris Blakely, Dirk Eddelbuettel, Maarten Schermer, and Eric Zivot

## See Also

Useful links:

- <https://github.com/jonathancornelissen/highfrequency>
- Report bugs at <https://github.com/jonathancornelissen/highfrequency/issues>

---

`aggregatePrice`*Aggregate a time series but keep first and last observation*

---

## Description

Function to aggregate high frequency data by last tick aggregation to an arbitrary periodicity based on wall clocks. Alternatively the aggregation can be done by number of ticks. In case we DON'T do tick-based aggregation, this function accepts arbitrary number of symbols over a arbitrary number of days. Although the function has the word Price in the name, the function is general and works on arbitrary time series, either `xts` or `data.table` objects the latter requires a DT column containing POSIXct time stamps.

## Usage

```
aggregatePrice(  
  pData,  
  alignBy = "minutes",  
  alignPeriod = 1,  
  marketOpen = "09:30:00",  
  marketClose = "16:00:00",  
  fill = FALSE,  
  tz = NULL  
)
```

## Arguments

<code>pData</code>	<code>data.table</code> or <code>xts</code> object to be aggregated containing the intraday price series, possibly across multiple days.
<code>alignBy</code>	character, indicating the time scale in which <code>alignPeriod</code> is expressed. Possible values are: "secs", "seconds", "mins", "minutes", "hours", and "ticks". To aggregate based on a 5 minute frequency, set <code>alignPeriod</code> to 5 and <code>alignBy</code> to "minutes".
<code>alignPeriod</code>	positive numeric, indicating the number of periods to aggregate over. E.g. to aggregate based on a 5 minute frequency, set <code>alignPeriod</code> to 5 and <code>alignBy</code> to "minutes".
<code>marketOpen</code>	the market opening time, by default: <code>marketOpen = "09:30:00"</code> .
<code>marketClose</code>	the market closing time, by default: <code>marketClose = "16:00:00"</code> .
<code>fill</code>	indicates whether rows without trades should be added with the most recent value, FALSE by default.
<code>tz</code>	fallback time zone used in case we are unable to identify the timezone of the data, by default: <code>tz = NULL</code> . We attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use <code>tz</code> if specified, and if it is not specified, we use "UTC"

**Details**

The time stamps of the new time series are the closing times and/or days of the intervals. The element of the returned series with e.g. time stamp 09:35:00 contains the last observation up to that point, including the value at 09:35:00 itself.

In case `alignBy = "ticks"`, the sampling is done such the sampling starts on the first tick, and the last tick is always included. For example, if 14 observations are made on one day, and these are 1, 2, 3, ... 14. Then, with `alignBy = "ticks"` and `alignPeriod = 3`, the output will be 1, 4, 7, 10, 13, 14.

**Value**

A `data.table` or `xts` object containing the aggregated time series.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

**Examples**

```
# Aggregate price data to the 30 second frequency
aggregatePrice(sampleTData, alignBy = "secs", alignPeriod = 30)
# Aggregate price data to the 30 second frequency including zero return price changes
aggregatePrice(sampleTData, alignBy = "secs", alignPeriod = 30)

# Aggregate price data to half a second frequency including zero return price changes
aggregatePrice(sampleTData, alignBy = "milliseconds", alignPeriod = 500, fill = TRUE)
```

---

aggregateQuotes

*Aggregate a data.table or xts object containing quote data*

---

**Description**

Aggregate tick-by-tick quote data and return a `data.table` or `xts` object containing the aggregated quote data. See [sampleQData](#) for an example of the argument `qData`. This function accepts arbitrary number of symbols over an arbitrary number of days.

**Usage**

```
aggregateQuotes(
  qData,
  alignBy = "minutes",
  alignPeriod = 5,
  marketOpen = "09:30:00",
  marketClose = "16:00:00",
  tz = NULL
)
```

## Arguments

qData	data.table or xts object to be aggregated, containing the intraday quote data of a stock for one day.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "secs", "seconds", "mins", "minutes", "hours", and "ticks". To aggregate based on a 5 minute frequency, set alignPeriod to 5 and alignBy to "minutes".
alignPeriod	positive numeric, indicating the number of periods to aggregate over. E.g. to aggregate based on a 5 minute frequency, set alignPeriod to 5 and alignBy to "minutes".
marketOpen	the market opening time, by default: marketOpen = "09:30:00".
marketClose	the market closing time, by default: marketClose = "16:00:00".
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. We attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC"

## Details

The output "BID" and "OFR" columns are constructed using previous tick aggregation.

The variables "BIDSIZ" and "OFRSIZ" are aggregated by taking the sum of the respective inputs over each interval.

The timestamps of the new time series are the closing times of the intervals.

Please note: Returned objects always contain the first observation (i.e. opening quotes,...).

## Value

A data.table or an xts object containing the aggregated quote data.

## Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

## Examples

```
# Aggregate quote data to the 30 second frequency
qDataAggregated <- aggregateQuotes(sampleQData, alignBy = "seconds", alignPeriod = 30)
qDataAggregated # Show the aggregated data
```

---

aggregateTrades      *Aggregate a data.table or xts object containing trades data*

---

### Description

Aggregate tick-by-tick trade data and return a time series as a `data.table` or `xts` object where first observation is always the opening price and subsequent observations are the closing prices over the interval. This function accepts arbitrary number of symbols over an arbitrary number of days.

### Usage

```
aggregateTrades(
  tData,
  alignBy = "minutes",
  alignPeriod = 5,
  marketOpen = "09:30:00",
  marketClose = "16:00:00",
  tz = NULL
)
```

### Arguments

<code>tData</code>	<code>data.table</code> or <code>xts</code> object to be aggregated, containing the intraday price series of a stock for possibly multiple days.
<code>alignBy</code>	character, indicating the time scale in which <code>alignPeriod</code> is expressed. Possible values are: "secs", "seconds", "mins", "minutes", "hours". To aggregate based on a 5 minute frequency, set <code>alignPeriod = 5</code> and <code>alignBy = "minutes"</code> .
<code>alignPeriod</code>	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5 minute frequency, set <code>alignPeriod = 5</code> and <code>alignBy = "minutes"</code> .
<code>marketOpen</code>	the market opening time, by default: <code>marketOpen = "09:30:00"</code> .
<code>marketClose</code>	the market closing time, by default: <code>marketClose = "16:00:00"</code> .
<code>tz</code>	fallback time zone used in case we are unable to identify the timezone of the data, by default: <code>tz = NULL</code> . We attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use <code>tz</code> if specified, and if it is not specified, we use "UTC"

### Details

The time stamps of the new time series are the closing times and/or days of the intervals.

The output "PRICE" column is constructed using previous tick aggregation.

The variable "SIZE" is aggregated by taking the sum over each interval.

The variable "VWPRICE" is the aggregated price weighted by volume.

The time stamps of the new time series are the closing times of the intervals.



In case of previous tick aggregation or `alignBy = "seconds"/"minutes"/"hours"`, the element of the returned series with e.g. time stamp 09:35:00 contains the last observation up to that point, including the value at 09:35:00 itself.

### Value

A `data.table` or `xts` object containing the aggregated time series.

### Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

### Examples

```
# Aggregate trade data to 5 minute frequency
tDataAggregated <- aggregateTrades(sampleTData, alignBy = "minutes", alignPeriod = 5)
tDataAggregated
```

---

aggregateTS	<i>Aggregate a time series</i>
-------------	--------------------------------

---

### Description

Aggregate a time series as `xts` or `data.table` object. It can handle irregularly spaced time series and returns a regularly spaced one. Use univariate time series as input for this function and check out [aggregateTrades](#) and [aggregateQuotes](#) to aggregate Trade or Quote data objects.

### Usage

```
aggregateTS(
  ts,
  FUN = "previoustick",
  alignBy = "minutes",
  alignPeriod = 1,
  weights = NULL,
  dropna = FALSE,
  tz = NULL,
  ...
)
```

### Arguments

<code>ts</code>	<code>xts</code> or <code>data.table</code> object to aggregate.
<code>FUN</code>	function to apply over each interval. By default, previous tick aggregation is done. Alternatively one can set e.g. <code>FUN = "mean"</code> . In case weights are supplied, this argument is ignored and a weighted average is taken.

alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "secs", "seconds", "mins", "minutes", "hours", "days", "weeks", "ticks".
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5 minute frequency, set alignPeriod to 5 and alignBy to "minutes".
weights	By default, no weighting scheme is used. When you assign an xts object with weights to this argument, a weighted mean is taken over each interval. Of course, the weights should have the same time stamps as the supplied time series.
dropna	boolean, which determines whether empty intervals should be dropped. By default, an NA is returned in case an interval is empty, except when the user opts for previous tick aggregation, by setting FUN = "previoustick" (default).
tz	character denoting which timezone the output should be in. Defaults to NULL
...	extra parameters passed on to FUN

### Details

The time stamps of the new time series are the closing times and/or days of the intervals. For example, for a weekly aggregation the new time stamp is the last day in that particular week (namely Sunday).

In case of previous tick aggregation, for alignBy is either "seconds" "minutes", or "hours", the element of the returned series with e.g. timestamp 09:35:00 contains the last observation up to that point, including the value at 09:35:00 itself.

Please note: In case an interval is empty, by default an NA is returned.. In case e.g. previous tick aggregation it makes sense to fill these NAs by the function `na.locf` (last observation carried forward) from the **zoo** package.

In case alignBy = "ticks", the sampling is done such the sampling starts on the first tick and the last tick is always included. For example, if 14 observations are made on one day, and these are 1, 2, 3, ... 14. Then, with alignBy = "ticks" and alignPeriod = 3, the output will be 1, 4, 7, 10, 13, 14.

### Value

An xts object containing the aggregated time series.

### Author(s)

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

### Examples

```
# Load sample price data
## Not run:
library(xts)
ts <- as.xts(sampleTData[, list(DT, PRICE, SIZE)])
```

```

# Previous tick aggregation to the 5-minute sampling frequency:
tsagg5min <- aggregateTS(ts, alignBy = "minutes", alignPeriod = 5)
head(tsagg5min)
# Previous tick aggregation to the 30-second sampling frequency:
tsagg30sec <- aggregateTS(ts, alignBy = "seconds", alignPeriod = 30)
tail(tsagg30sec)
tsagg3ticks <- aggregateTS(ts, alignBy = "ticks", alignPeriod = 3)

## End(Not run)

```

---

AJumpTest

*Ait-Sahalia and Jacod (2009) tests for the presence of jumps in the price series.*


---

### Description

This test examines the presence of jumps in highfrequency price series. It is based on the theory of Ait-Sahalia and Jacod (2009). It consists in comparing the multi-power variation of equi-spaced returns computed at a fast time scale ( $h$ ),  $r_{t,i}$  ( $i = 1, \dots, N$ ) and those computed at the slower time scale ( $kh$ ),  $y_{t,i}$  ( $i = 1, \dots, N/k$ ).

They found that the limit (for  $N \rightarrow \infty$ ) of the realized power variation is invariant for different sampling scales and that their ratio is 1 in case of jumps and  $k^{p/2} - 1$  if no jumps. Therefore the AJ test detects the presence of jump using the ratio of realized power variation sampled from two scales. The null hypothesis is no jumps.

The function returns three outcomes: 1.z-test value 2.critical value under confidence level of 95% and 3.  $p$ -value.

Assume there is  $N$  equispaced returns in period  $t$ . Let  $r_{t,i}$  be a return (with  $i = 1, \dots, N$ ) in period  $t$ .

And there is  $N/k$  equispaced returns in period  $t$ . Let  $y_{t,i}$  be a return (with  $i = 1, \dots, N/k$ ) in period  $t$ .

Then the AJumpTest is given by:

$$AJumpTest_{t,N} = \frac{S_t(p, k, h) - k^{p/2-1}}{\sqrt{V_{t,N}}}$$

in which,

$$S_t(p, k, h) = \frac{PV_{t,M}(p, kh)}{PV_{t,M}(p, h)}$$

$$PV_{t,N}(p, kh) = \sum_{i=1}^{N/k} |y_{t,i}|^p$$

$$\begin{aligned} \mathbf{PV}_{t,N}(p, h) &= \sum_{i=1}^N |r_{t,i}|^p \\ \mathbf{V}_{t,N} &= \frac{N(p, k)A_{t,N(2p)}}{NA_{t,N(p)}} \\ N(p, k) &= \left( \frac{1}{\mu_p^2} \right) (k^{p-2}(1+k))\mu_{2p} + k^{p-2}(k-1)\mu_p^2 - 2k^{p/2-1}\mu_{k,p} \\ A_{t,n(2p)} &= \frac{(1/N)^{(1-p/2)}}{\mu_p} \sum_{i=1}^N |r_{t,i}|^p \text{ for } |r_j| < \alpha(1/N)^w \\ \mu_{k,p} &= E(|U|^p | U + \sqrt{k-1}V|^p) \end{aligned}$$

$U, V$ : independent standard normal random variables;  $h = 1/N$ ;  $p, k, \alpha, w$ : parameters.

### Usage

```
AJjumpTest(
  pData,
  p = 4,
  k = 2,
  alignBy = NULL,
  alignPeriod = NULL,
  alphaMultiplier = 4,
  alpha = 0.975,
  ...
)
```

### Arguments

<code>pData</code>	either an <code>xts</code> or a <code>data.table</code> containing the prices of a single asset, possibly over multiple days.
<code>p</code>	can be chosen among 2 or 3 or 4. The author suggests 4. 4 by default.
<code>k</code>	can be chosen among 2 or 3 or 4. The author suggests 2. 2 by default.
<code>alignBy</code>	character, indicating the time scale in which <code>alignPeriod</code> is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours" To aggregate based on a 5 minute frequency, set <code>alignPeriod</code> to 5 and <code>alignBy</code> to "minutes".
<code>alignPeriod</code>	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5 minute frequency, set <code>alignPeriod</code> = 5 and <code>alignBy</code> = "minutes".
<code>alphaMultiplier</code>	alpha multiplier
<code>alpha</code>	numeric of length one with the significance level to use for the jump test(s). Defaults to 0.975.
<code>...</code>	used internally

## Details

The theoretical framework underlying jump test is that the logarithmic price process  $X_t$  belongs to the class of Brownian semimartingales, which can be written as:

$$X_t = \int_0^t a_u du + \int_0^t \sigma_u dW_u + Z_t$$

where  $a$  is the drift term,  $\sigma$  denotes the spot volatility process,  $W$  is a standard Brownian motion and  $Z$  is a jump process defined by:

$$Z_t = \sum_{j=1}^{N_t} k_j$$

where  $k_j$  are nonzero random variables. The counting process can be either finite or infinite for finite or infinite activity jumps.

Using the convergence properties of power variation and its dependence on the time scale on which it is measured, Ait-Sahalia and Jacod (2009) define a new variable which converges to 1 in the presence of jumps in the underlying return series, or to another deterministic and known number in the absence of jumps (Theodosiou and Zikes, 2009).

## Value

a list or xts in depending on whether input prices span more than one day.

## Author(s)

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

## References

Ait-Sahalia, Y. and Jacod, J. (2009). Testing for jumps in a discretely observed process. *The Annals of Statistics*, 37(1), 184-222.

Theodosiou, M., & Zikes, F. (2009). A comprehensive comparison of alternative tests for jumps in asset prices. Unpublished manuscript, Graduate School of Business, Imperial College London.

## Examples

```
jt <- AJumpTest(sampleTData[, list(DT, PRICE)], p = 2, k = 3,
               alignBy = "seconds", alignPeriod = 5, makeReturns = TRUE)
```

---

`autoSelectExchangeQuotes`*Retain only data from the stock exchange with the highest volume*

---

**Description**

Filters raw quote data and return only data that stems from the exchange with the highest value for the sum of "BIDSIZ" and "OFRSIZ", i.e. the highest quote volume.

**Usage**

```
autoSelectExchangeQuotes(qData, printExchange = TRUE)
```

**Arguments**

- |                            |  |
|----------------------------|--|
| <code>qData</code>         | a <code>data.table</code> or <code>xts</code> object with at least a column "EX", indicating the exchange symbol and columns "BIDSIZ" and "OFRSIZ", indicating the volume available at the bid and ask respectively.   |
| <code>printExchange</code> | indicates whether the chosen exchange is printed on the console, default is TRUE. The possible exchanges are: <ul style="list-style-type: none"><li>• A: AMEX</li><li>• N: NYSE</li><li>• B: Boston</li><li>• P: Arca</li><li>• C: NSX</li><li>• T/Q: NASDAQ</li><li>• D: NASD ADF and TRF</li><li>• X: Philadelphia</li><li>• I: ISE</li><li>• M: Chicago</li><li>• W: CBOE</li><li>• Z: BATS</li></ul> |

**Value**

`data.table` or `xts` object depending on input.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

**Examples**

```
autoSelectExchangeQuotes(sampleQDataRaw)
```

---

`autoSelectExchangeTrades`*Retain only data from the stock exchange with the highest trading volume*

---

**Description**

Filters raw trade data and return only data that stems from the exchange with the highest value for the variable "SIZE", i.e. the highest trade volume.

**Usage**

```
autoSelectExchangeTrades(tData, printExchange = TRUE)
```

**Arguments**

<code>tData</code>	an xts object with at least a column "EX" indicating the exchange symbol and "SIZE" indicating the trade volume.
<code>printExchange</code>	indicates whether the chosen exchange is printed on the console, default is TRUE. The possible exchanges are: <ul style="list-style-type: none"><li>• A: AMEX</li><li>• N: NYSE</li><li>• B: Boston</li><li>• P: Arca</li><li>• C: NSX</li><li>• T/Q: NASDAQ</li><li>• D: NASD ADF and TRF</li><li>• X: Philadelphia</li><li>• I: ISE</li><li>• M: Chicago</li><li>• W: CBOE</li><li>• Z: BATS</li></ul>

**Value**

data. table or xts object depending on input.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

**Examples**

```
autoSelectExchangeTrades(sampleTDataRaw)
```

---

BNSjumpTest	<i>Barndorff-Nielsen and Shephard (2006) tests for the presence of jumps in the price series.</i>
-------------	---

---

### Description

This test examines the presence of jumps in highfrequency price series. It is based on theory of Barndorff-Nielsen and Shephard (2006). The null hypothesis is that there are no jumps.

### Usage

```
BNSjumpTest(
  rData,
  IVestimator = "BV",
  IQestimator = "TP",
  type = "linear",
  logTransform = FALSE,
  max = FALSE,
  alignBy = NULL,
  alignPeriod = NULL,
  makeReturns = FALSE,
  alpha = 0.975
)
```

### Arguments

rData	either an xts or a data.table containing the log-returns or prices of a single asset, possibly over multiple days-
IVestimator	can be chosen among jump robust integrated variance estimators: <a href="#">rBPCov</a> , <a href="#">rMinRVar</a> , <a href="#">rMedRVar</a> , <a href="#">rOWCov</a> and corrected threshold bipower variation ( <a href="#">rThresholdCov</a> ). If <a href="#">rThresholdCov</a> is chosen, an argument of startV, start point of auxiliary estimators in threshold estimation can be included. <a href="#">rBPCov</a> by default.
IQestimator	can be chosen among jump robust integrated quarticity estimators: <a href="#">rTPQuar</a> , <a href="#">rQPVar</a> , <a href="#">rMinRQuar</a> and <a href="#">rMedRQuar</a> . <a href="#">rTPQuar</a> by default.
type	a method of BNS testing: can be linear or ratio. Linear by default.
logTransform	boolean, should be TRUE when QVestimator and IVestimator are in logarithm form. FALSE by default.
max	boolean, should be TRUE when max adjustment in SE. FALSE by default.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours" To aggregate based on a 5 minute frequency, set alignPeriod = 5 and alignBy = "minutes".
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5 minute frequency, set alignPeriod = 5 and alignBy = "minutes".



makeReturns	boolean, should be TRUE when pData contains prices. FALSE by default.
alpha	numeric of length one with the significance level to use for the jump test(s). Defaults to 0.975.

### Details

Assume there is  $N$  equispaced returns in period  $t$ . Assume the Realized variance (RV), IVestimator and IQestimator are based on  $N$  equi-spaced returns.

Let  $r_{t,i}$  be a return (with  $i = 1, \dots, N$ ) in period  $t$ .

Then the BNSjumpTest is given by

$$\text{BNSjumpTest} = \frac{\text{RV} - \text{IVestimator}}{\sqrt{(\theta - 2) \frac{1}{N} \text{IQestimator}}}.$$

The options for IVestimator and IQestimator are listed above.  $\theta$  depends on the chosen IVestimator (Huang and Tauchen, 2005).

The theoretical framework underlying the jump test is that the logarithmic price process  $X_t$  belongs to the class of Brownian semimartingales, which can be written as:

$$X_t = \int_0^t a_u du + \int_0^t \sigma_u dW_u + Z_t$$

where  $a$  is the drift term,  $\sigma$  denotes the spot volatility process,  $W$  is a standard Brownian motion and  $Z$  is a jump process defined by:

$$Z_t = \sum_{j=1}^{N_t} k_j$$

where  $k_j$  are nonzero random variables. The counting process can be either finite or infinite for finite or infinite activity jumps.

Since the realized volatility converges to the sum of integrated variance and jump variation, while the robust IVestimator converges to the integrated variance, it follows that the difference between RV and the IVestimator captures the jump part only, and this observation underlines the BNS test for jumps (Theodosiou and Zikes, 2009).

### Value

a list or xts (depending on whether input prices span more than one day) with the following values:

- $z$ -test value.
- critical value (with confidence level of 95%).
- $p$ -value of the test.

### Author(s)

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

## References

- Barndorff-Nielsen, O. E., and Shephard, N. (2006). Econometrics of testing for jumps in financial economics using bipower variation. *Journal of Financial Econometrics*, 4, 1-30.
- Corsi, F., Pirino, D., and Reno, R. (2010). Threshold bipower variation and the impact of jumps on volatility forecasting. *Journal of Econometrics*, 159, 276-288.
- Huang, X., and Tauchen, G. (2005). The relative contribution of jumps to total price variance. *Journal of Financial Econometrics*, 3, 456-499.
- Theodosiou, M., and Zikes, F. (2009). A comprehensive comparison of alternative tests for jumps in asset prices. Unpublished manuscript, Graduate School of Business, Imperial College London.

## Examples

```
bns <- BNSjumpTest(sampleTData[, list(DT, PRICE)], Ivestimator= "rMinRVar",
                  IQestimator = "rMedRQuar", type= "linear", makeReturns = TRUE)
bns
```

---

businessTimeAggregation

*Business time aggregation*

---

## Description

Time series aggregation based on ‘business time’ statistics. Instead of equidistant sampling based on time during a trading day, business time sampling creates measures and samples equidistantly using these instead. For example when sampling based on volume, business time aggregation will result in a time series that has an equal amount of volume between each observation (if possible).

## Usage

```
businessTimeAggregation(
  pData,
  measure = "volume",
  obs = 390,
  bandwidth = 0.075,
  tz = NULL,
  ...
)
```

## Arguments

pData	xts or data.table containing data to aggregate.
measure	character denoting which measure to use. Valid options are "intensity", "vol", and "volume", denoting the trade intensity process of Oomen (2005), volatility, and volume, respectively. Default is "volume".

obs	integer valued numeric of length 1 denoting how many observations is wanted after the aggregation procedure.
bandwidth	numeric of length one, denoting which bandwidth parameter to use in the trade intensity process estimation of Oomen (2005).
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. We attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC".
...	extra arguments passed on to <code>spotVol</code> when measure is "vol".

### Value

A list containing "pData" which is the aggregated data and a list containing the intensity process, split up day by day.

### Author(s)

Emil Sjoerup.

### References

Dong, Y., and Tse, Y. K. (2017). Business time sampling scheme with applications to testing semi-martingale hypothesis and estimating integrated volatility. *Econometrics*, 5, 51.

Oomen, R. C. A. (2006). Properties of realized variance under alternative sampling schemes. *Journal of Business & Economic Statistics*, 24, 219-237

### Examples

```
pData <- sampleTData[,list(DT, PRICE, SIZE)]
# Aggregate based on the trade intensity measure. Getting 390 observations.
agged <- businessTimeAggregation(pData, measure = "intensity", obs = 390, bandwidth = 0.075)
# Plot the trade intensity measure
plot.ts(agged$intensityProcess$`2018-01-02`)
rCov(agged$pData[, list(DT, PRICE)], makeReturns = TRUE)
rCov(pData[,list(DT, PRICE)], makeReturns = TRUE, alignBy = "minutes", alignPeriod = 1)

# Aggregate based on the volume measure. Getting 78 observations.
agged <- businessTimeAggregation(pData, measure = "volume", obs = 78)
rCov(agged$pData[,list(DT, PRICE)], makeReturns = TRUE)
rCov(pData[,list(DT, PRICE)], makeReturns = TRUE, alignBy = "minutes", alignPeriod = 5)
```

**Description**

Calculates the test-statistic for the drift burst hypothesis

Let the efficient log-price be defined as:

$$dX_t = \mu_t dt + \sigma_t dW_t + dJ_t,$$

where  $\mu_t$ ,  $\sigma_t$ , and  $J_t$  are the spot drift, the spot volatility, and a jump process respectively. However, due to microstructure noise, the observed log-price is

$$Y_t = X_t + \varepsilon_t$$

In order to robustify the results to the presence of market microstructure noise, the pre-averaged returns are used:

$$\Delta_i^n \bar{Y} = \sum_{j=1}^{k_n-1} g_j^n \Delta_{i+j}^n Y,$$

where  $g(\cdot)$  is a weighting function,  $\min(x, 1-x)$ , and  $k_n$  is the pre-averaging horizon.

The test statistic for the Drift Burst Hypothesis can then be calculated as

$$\bar{T}_t^n = \sqrt{\frac{h_n}{K_2}} \frac{\hat{\mu}_t^n}{\sqrt{\hat{\sigma}_t^n}},$$

where

$$\hat{\mu}_t^n = \frac{1}{h_n} \sum_{i=1}^{n-k_n+2} K\left(\frac{t_{i-1}-t}{h_n}\right) \Delta_{i-1}^n \bar{Y},$$

and

$$\hat{\sigma}_t^n = \frac{1}{h_n'} \left[ \sum_{i=1}^{n-k_n+2} \left( K\left(\frac{t_{i-1}-t}{h_n'}\right) \Delta_{i-1}^n \bar{Y} \right)^2 + 2 \sum_{L=1}^{L_n} \omega\left(\frac{L}{L_n}\right) \sum_{i=1}^{n-k_n-L+2} K\left(\frac{t_{i-1}-t}{h_n'}\right) K\left(\frac{t_{i+L-1}-t}{h_n'}\right) \Delta_{i-1}^n \bar{Y} \Delta_{i-1+L}^n \bar{Y} \right],$$

where  $\omega(\cdot)$  is a smooth kernel function, in this case the Parzen kernel.  $L_n$  is the lag length for adjusting for auto-correlation and  $K(\cdot)$  is a kernel weighting function, which in this case is the left-sided exponential kernel.

**Usage**

```
driftBursts(
  pData,
  testTimes = seq(34260, 57600, 60),
  preAverage = 5,
  ACLag = -1L,
```

```

    meanBandwidth = 300L,
    varianceBandwidth = 900L,
    parallelize = FALSE,
    nCores = NA,
    warnings = TRUE
)

```

## Arguments

pData	Either a <code>data.table</code> or an <code>xts</code> object. If <code>pData</code> is a <code>data.table</code> , columns <code>DT</code> and <code>PRICE</code> must be present, containing timestamps of the trades and the price of the trades (in levels) respectively. If <code>pData</code> is an <code>xts</code> object and the number of columns is greater than one, <code>PRICE</code> must be present.
testTimes	A numeric containing the times at which to calculate the tests. The standard of <code>seq(34260, 57600, 60)</code> denotes calculating the test-statistic once per minute, i.e. 390 times for a typical 6.5 hour trading day from 9:31:00 to 16:00:00. See details. Additionally, <code>testTimes</code> can be set to 'all' where the test statistic will be calculated on each tick more than 5 seconds after opening
preAverage	A positive integer denoting the length of pre-averaging window for the log-prices. Default is 5
ACLag	A positive integer greater than 1 denoting how many lags are to be used for the HAC estimator of the variance - the default of -1 denotes using an automatic lag selection algorithm for each iteration. Default is -1L
meanBandwidth	An integer denoting the bandwidth for the left-sided exponential kernel for the mean. Default is 300L
varianceBandwidth	An integer denoting the bandwidth for the left-sided exponential kernel for the variance. Default is 900L
parallelize	A logical to determine whether to parallelize the underlying C++ code (Using OpenMP). Default is <code>FALSE</code> . Note that the parallelized code is not interruptable, while the non-parallel code is interruptable and it's checked every 100 iterations.
nCores	An integer denoting the number of cores to use for calculating the code when parallelized. If this argument is not provided, sequential evaluation will be used even though <code>parallelize</code> is <code>TRUE</code> . Default is <code>NA</code>
warnings	A logical denoting whether warnings should be shown. Default is <code>TRUE</code>

## Details

If the `testTimes` vector contains instructions to test before the first trade, or more than 15 minutes after the last trade, these entries will be deleted, as not doing so may cause crashes. The test statistic is unstable before  $\max(\text{meanBandwidth}, \text{varianceBandwidth})$  seconds has passed. The lags from the Newey-West algorithm is increased by  $2 * (\text{preAverage} - 1)$  due to the pre-averaging we know at least this many lags should be corrected for. The maximum of 20 lags is also increased by this factor for the same reason.

**Value**

An object of class DBH and list containing the series of the drift burst hypothesis test-statistic as well as the estimated spot drift and variance series. The list also contains some information such as the variance and mean bandwidths along with the pre-averaging setting and the amount of observations. Additionally, the list will contain information on whether testing happened for all testTimes entries. Objects of class DBH has the methods `print.DBH`, `plot.DBH`, and `getCriticalValues.DBH` which prints, plots, and retrieves critical values for the test described in appendix B of Christensen, Oomen, and Reno (2020).

**Author(s)**

Emil Sjoerup

**References**

Christensen, K., Oomen, R., and Reno, R. (2020) The drift burst hypothesis. *Journal of Econometrics*. Forthcoming.

**Examples**

```
# Usage with data.table object
dat <- sampleTData[as.Date(DT) == "2018-01-02"]
# Testing every 60 seconds after 09:45:00
DBH1 <- driftBursts(dat, testTimes = seq(35100, 57600, 60), preAverage = 2, ACLag = -1L,
                  meanBandwidth = 300L, varianceBandwidth = 900L)
print(DBH1)

plot(DBH1, pData = dat)
# Usage with xts object (1 column)
library("xts")
dat <- xts(sampleTData[as.Date(DT) == "2018-01-03"]$PRICE,
          order.by = sampleTData[as.Date(DT) == "2018-01-03"]$DT)
# Testing every 60 seconds after 09:45:00
DBH2 <- driftBursts(dat, testTimes = seq(35100, 57600, 60), preAverage = 2, ACLag = -1L,
                  meanBandwidth = 300L, varianceBandwidth = 900L)
plot(DBH2, pData = dat)

## Not run:
# This block takes some time
dat <- xts(sampleTDataEurope$PRICE,
          order.by = sampleTDataEurope$DT)
# Testing every 60 seconds after 09:00:00
system.time({DBH4 <- driftBursts(dat, testTimes = seq(32400 + 900, 63000, 60), preAverage = 2,
                              ACLag = -1L, meanBandwidth = 300L, varianceBandwidth = 900L)})

system.time({DBH4 <- driftBursts(dat, testTimes = seq(32400 + 900, 63000, 60), preAverage = 2,
                              ACLag = -1L, meanBandwidth = 300L, varianceBandwidth = 900L,
                              parallelize = TRUE, nCores = 8)})
plot(DBH4, pData = dat)

# The print method for DBH objects takes an argument alpha that determines the confidence level
```

```
# of the test performed
print(DBH4, alpha = 0.99)
# Additionally, criticalValue can be passed directly
print(DBH4, criticalValue = 3)
max(abs(DBH4$tStat)) > getCriticalValues(DBH4, 0.99)$quantile

## End(Not run)
```

---

exchangeHoursOnly      *Extract data from an xts object for the exchange hours only*

---

### Description

Filter raw trade data such and return only data between market close and market open. By default, marketOpen = "09:30:00" and marketClose = "16:00:00" (see Brownlees and Gallo (2006) for more information on good choices for these arguments).

### Usage

```
exchangeHoursOnly(
  data,
  marketOpen = "09:30:00",
  marketClose = "16:00:00",
  tz = NULL
)
```

### Arguments

data	a data.table or xts object containing the time series data. Multiple days of input are allowed.
marketOpen	character in the format of "HH:MM:SS", specifying the opening time of the exchange(s).
marketClose	character in the format of "HH:MM:SS", specifying the closing time of the exchange(s).
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. We attempt to extract the timezone from the DT column of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC"

### Value

xts or data.table object depending on input.

### Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

**References**

Brownlees, C. T. and Gallo, G. M. (2006). Financial econometric analysis at ultra-high frequency: Data handling concerns. *Computational Statistics & Data Analysis*, 51, pages 2232-2245.

**Examples**

```
exchangeHoursOnly(sampleTDataRaw)
```

---

gatherPrices	<i>Make TAQ format</i>
--------------	------------------------

---

**Description**

Convenience function to gather data from one `xts` or `data.table` with at least "DT", and `d` columns containing price data to a "DT", "SYMBOL", and "PRICE" column. This function the opposite of [spreadPrices](#).

**Usage**

```
gatherPrices(data)
```

**Arguments**

`data` An `xts` or a `data.table` object with at least "DT" and `d` columns with price data with their names corresponding to the respective symbols.

**Value**

a `data.table` with columns DT, SYMBOL, and PRICE

**Author(s)**

Emil Sjoerup

**See Also**

[spreadPrices](#)

**Examples**

```
## Not run:
library(data.table)
data1 <- copy(sampleTData)[, `:=`(PRICE = PRICE * runif(.N, min = 0.99, max = 1.01),
                               DT = DT + runif(.N, 0.01, 0.02))]

data2 <- copy(sampleTData)[, SYMBOL := 'XYZ']
dat1 <- rbind(data1[, list(DT, SYMBOL, PRICE)], data2[, list(DT, SYMBOL, PRICE)])
setkeyv(dat1, c("DT", "SYMBOL"))
dat1
dat <- spreadPrices(dat1) # Easy to use for realized measures
```



```
dat
dat <- gatherPrices(dat)
dat
all.equal(dat1, dat) # We have changed to RM format and back.

## End(Not run)
```

---

getAlphaVantageData    *Get high frequency data from Alpha Vantage*

---

### Description

Function to retrieve high frequency data from Alpha Vantage - wrapper around quantmod's get-Symbols.av function

### Usage

```
getAlphaVantageData(
  symbols = NULL,
  interval = "5min",
  outputType = "xts",
  apiKey = NULL,
  doSleep = TRUE
)
```

### Arguments

symbols	character vector with the symbols to import.
interval	the sampling interval of the data retrieved. Should be one of one of "1min", "5min", "15min", "30min", or "60min"
outputType	string either "xts" or "DT" to denote the type of output wanted. "xts" will yield an xts object, "DT" will yield a data.table object.
apiKey	string with the api key provided by Alpha Vantage.
doSleep	logical when the length of symbols > 5 the function will sleep for 12 seconds by default.

### Details

The doSleep argument is set to true as default because Alpha Vantage has a limit of five calls per minute. The function does not try to extract when the last API call was made which means that if you made successive calls to get 3 symbols in rapid succession, the function may not retrieve all the data.

### Value

An object of type xts or data.table in case the length of symbols is 1. If the length of symbols > 1 the xts and data.table objects will be put into a list.

**Author(s)**

Emil Sjoerup (wrapper only) Paul Teetor (for quantmod's getSymbols.av)

**See Also**

The getSymbols.av function in the quantmod package

**Examples**

```
## Not run:
# Get data for SPY at an interval of 1 minute in the standard xts format.
data <- getAlphaVantageData(symbols = "SPY", apiKey = "yourKey", interval = "1min")

# Get data for 3M and Goldman Sachs at a 5 minute interval in the data.table format.
# The data.tables will be put in a list.
data <- getAlphaVantageData(symbols = c("MMM", "GS"), interval = "5min",
                             outputType = "DT", apiKey = 'yourKey')

# Get data for JPM and Citicorp at a 15 minute interval in the xts format.
# The xts objects will be put in a list.
data <- getAlphaVantageData(symbols = c("JPM", "C"), interval = "15min",
                             outputType = "xts", apiKey = "yourKey")

## End(Not run)
```

---

getCriticalValues

*Get critical value for the drift burst hypothesis t-statistic*

---

**Description**

Method for DBH objects to calculate the critical value for the presence of a burst of drift. The critical value is that of the test described in appendix B in Christensen Oomen Reno

**Usage**

```
getCriticalValues(x, alpha = 0.95)
```

**Arguments**

x	object of class DBH
alpha	numeric denoting the confidence level for the critical value. Possible values are c(0.9 0.95 0.99 0.995 0.999 0.9999)

**Author(s)**

Emil Sjoerup

## References

Christensen, K., Oomen, R., and Reno, R. (2020) The drift burst hypothesis. *Journal of Econometrics*. Forthcoming.

---

getLiquidityMeasures *Compute Liquidity Measure*

---

## Description

Function returns an `xts` or `data.table` object containing 23 liquidity measures. Please see details below.

Note that this assumes a regular time grid.

## Usage

```
getLiquidityMeasures(tqData, win = 300)
```

## Arguments

<code>tqData</code>	A <code>data.table</code> or <code>xts</code> object as in the <b>highfrequency</b> merged trades and quotes data.
<code>win</code>	A windows length for the forward-prices used for ‘realized’ spread

## Details

NOTE: `xts` or `data.table` should only contain one day of observations Some markets have publish information about whether it was a buyer or a seller who initiated the trade. This information can be passed in a column `DIRECTION` this column must only have 1 or -1 as values.

The respective liquidity measures are defined as follows:

- `effectiveSpread`

$$\text{effective spread}_t = 2 * D_t * \left( \text{PRICE}_t - \frac{(\text{BID}_t + \text{OFR}_t)}{2} \right),$$

where  $D_t$  is 1 (-1) if  $trade_t$  was buy (sell) (see Boehmer (2005), Bessembinder (2003)). Note that the input of this function consists of the matched trades and quotes, so this is were the time indication refers to (and thus not to the registered quote timestamp).

- `realizedSpread`: realized spread

$$\text{realized spread}_t = 2 * D_t * \left( \text{PRICE}_t - \frac{(\text{BID}_{t+300} + \text{OFR}_{t+300})}{2} \right),$$

where  $D_t$  is 1 (-1) if  $trade_t$  was buy (sell) (see Boehmer (2005), Bessembinder (2003)). Note that the time indication of `BID` and `OFR` refers to the registered time of the quote in seconds.

- `valueTrade`: trade value

$$\text{trade value}_t = \text{SIZE}_t * \text{PRICE}_t.$$

- signedValueTrade: signed trade value

$$\text{signed trade value}_t = D_t * (\text{SIZE}_t * \text{PRICE}_t),$$

where  $D_t$  is 1 (-1) if  $\text{trade}_t$  was buy (sell) (see Boehmer (2005), Bessembinder (2003)).

- depthImbalanceDifference: depth imbalance (as a difference)

$$\text{depth imbalance (as difference)}_t = \frac{D_t * (\text{OFRSIZ}_t - \text{BIDSIZ}_t)}{(\text{OFRSIZ}_t + \text{BIDSIZ}_t)},$$

where  $D_t$  is 1 (-1) if  $\text{trade}_t$  was buy (sell) (see Boehmer (2005), Bessembinder (2003)). Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- depthImbalanceRatio: depth imbalance (as ratio)

$$\text{depth imbalance (as ratio)}_t = \left( \frac{\text{OFRSIZ}_t}{\text{BIDSIZ}_t} \right)^{D_t},$$

where  $D_t$  is 1 (-1) if  $\text{trade}_t$  was buy (sell) (see Boehmer (2005), Bessembinder (2003)). Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- proportionalEffectiveSpread: proportional effective spread

$$\text{proportional effective spread}_t = \frac{\text{effective spread}_t}{(\text{OFR}_t + \text{BID}_t)/2}$$

(Venkataraman, 2001).

Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- proportionalRealizedSpread: proportional realized spread

$$\text{proportional realized spread}_t = \frac{\text{realized spread}_t}{(\text{OFR}_t + \text{BID}_t)/2}$$

(Venkataraman, 2001).

Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered

- priceImpact: price impact

$$\text{price impact}_t = \frac{\text{effective spread}_t - \text{realized spread}_t}{2}$$

(see Boehmer (2005), Bessembinder (2003)).

- proportionalPriceImpact: proportional price impact

$$\text{proportional price impact}_t = \frac{\frac{(\text{effective spread}_t - \text{realized spread}_t)}{2}}{\frac{\text{OFR}_t + \text{BID}_t}{2}}$$

(Venkataraman, 2001). Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- halfTradedSpread: half traded spread

$$\text{half traded spread}_t = D_t * (\text{PRICE}_t - \frac{(\text{BID}_t + \text{OFR}_t)}{2}),$$

where  $D_t$  is 1 (-1) if  $\text{trade}_t$  was buy (sell) (see Boehmer (2005), Bessembinder (2003)). Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- proportionalHalfTradedSpread: proportional half traded spread

$$\text{proportional half traded spread}_t = \frac{\text{half traded spread}_t}{\frac{\text{OFR}_t + \text{BID}_t}{2}}.$$

Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- squaredLogReturn: squared log return on trade prices

$$\text{squared log return on Trade prices}_t = (\log(\text{PRICE}_t) - \log(\text{PRICE}_{t-1}))^2.$$

- absLogReturn: absolute log return on trade prices

$$\text{absolute log return on Trade prices}_t = |\log(\text{PRICE}_t) - \log(\text{PRICE}_{t-1})|.$$

- quotedSpread: quoted spread

$$\text{quoted spread}_t = \text{OFR}_t - \text{BID}_t$$

Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- proportionalQuotedSpread: proportional quoted spread

$$\text{proportional quoted spread}_t = \frac{\text{quoted spread}_t}{\frac{\text{OFR}_t + \text{BID}_t}{2}}$$

(Venkataraman, 2001). Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- logQuotedSpread: log quoted spread

$$\text{log quoted spread}_t = \log\left(\frac{\text{OFR}_t}{\text{BID}_t}\right)$$

(Hasbrouck and Seppi, 2001). Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- logQuotedSize: log quoted size

$$\text{log quoted size}_t = \log(\text{OFRSIZ}_t) + \log(\text{BIDSIZ}_t)$$

(Hasbrouck and Seppi, 2001). Note that the input of this function consists of the matched trades and quotes, so this is where the time indication refers to (and thus not to the registered quote timestamp).

- quotedSlope: quoted slope

$$\text{quoted slope}_t = \frac{\text{quoted spread}_t}{\log \text{quoted size}_t}$$

(Hasbrouck and Seppi, 2001).

- logQSlope: log quoted slope

$$\log \text{quoted slope}_t = \frac{\log \text{quoted spread}_t}{\log \text{quoted size}_t}$$

- midQuoteSquaredReturn: midquote squared return

$$\text{midquote squared return}_t = (\log(\text{midquote}_t) - \log(\text{midquote}_{t-1}))^2,$$

where  $\text{midquote}_t = \frac{\text{BID}_t + \text{OFR}_t}{2}$ .

- midQuoteAbsReturn: midquote absolute return

$$\text{midquote absolute return}_t = |\log(\text{midquote}_t) - \log(\text{midquote}_{t-1})|,$$

where  $\text{midquote}_t = \frac{\text{BID}_t + \text{OFR}_t}{2}$ .

- signedTradeSize: signed trade size

$$\text{signed trade size}_t = D_t * \text{SIZE}_t,$$

where  $D_t$  is 1 (-1) if  $\text{trade}_t$  was buy (sell).

## Value

A modified (enlarged) xts or data.table with the new measures.

## References

- Bessembinder, H. (2003). Issues in assessing trade execution costs. *Journal of Financial Markets*, 223-257.
- Boehmer, E. (2005). Dimensions of execution quality: Recent evidence for US equity markets. *Journal of Financial Economics*, 78, 553-582.
- Hasbrouck, J. and Seppi, D. J. (2001). Common factors in prices, order flows and liquidity. *Journal of Financial Economics*, 59, 383-411.
- Venkataraman, K. (2001). Automated versus floor trading: An analysis of execution costs on the Paris and New York exchanges. *The Journal of Finance*, 56, 1445-1485.

## Examples

```
tqData <- matchTradesQuotes(sampleTData[as.Date(DT) == "2018-01-02"],
                           sampleQData[as.Date(DT) == "2018-01-02"])
res <- getLiquidityMeasures(tqData)
res
```

---

getTradeDirection	<i>Get trade direction</i>
-------------------	----------------------------

---

### Description

Function returns a vector with the inferred trade direction which is determined using the Lee and Ready algorithm (Lee and Ready, 1991).

### Usage

```
getTradeDirection(tqData)
```

### Arguments

tqData            data.table or xts object, containing joined trades and quotes (e.g. using [matchTradesQuotes](#))

### Details

NOTE: By convention the first observation is always marked as a buy.

### Value

A vector which has values 1 or (-1) if the inferred trade direction is buy or sell respectively.

### Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup. Special thanks to Dirk Eddelbuettel.

### References

Lee, C. M. C. and Ready, M. J. (1991). Inferring trade direction from intraday data. *Journal of Finance*, 46, 733-746.

### Examples

```
# Generate matched trades and quote data set
tqData <- matchTradesQuotes(sampleTData[as.Date(DT) == "2018-01-02"],
                           sampleQData[as.Date(DT) == "2018-01-02"])
directions <- getTradeDirection(tqData)
head(directions)
```

---

HARmodel	<i>Heterogeneous autoregressive (HAR) model for realized volatility model estimation</i>
----------	--

---

### Description

Function returns the estimates for the heterogeneous autoregressive model (HAR) for realized volatility discussed in Andersen et al. (2007) and Corsi (2009). This model is mainly used to forecast the next day's volatility based on the high-frequency returns of the past.

### Usage

```
HARmodel(
  data,
  periods = c(1, 5, 22),
  periodsJ = c(1, 5, 22),
  periodsQ = c(1),
  leverage = NULL,
  RVest = c("rCov", "rBPCov", "rQuar"),
  type = "HAR",
  inputType = "RM",
  jumpTest = "ABDJumptest",
  alpha = 0.05,
  h = 1,
  transform = NULL,
  externalRegressor = NULL,
  periodsExternal = c(1),
  ...
)
```

### Arguments

data	an xts object containing either: intraday (log-)returns or realized measures already computed from such returns. In case more than one realized measure is needed, the object should have the as many columns as realized measures needed. The first column should always be the realized variance proxy. In case type is either "HARQJ" or "CHARQ" the order should be "RV", "BPV", "RQ", or the relevant proxies.
periods	a vector of integers indicating over how days the realized measures in the model should be aggregated. By default periods = c(1,5,22), which corresponds to one day, one week and one month respectively. This default is in line with Andersen et al. (2007).
periodsJ	a vector of integers indicating over what time periods the jump components in the model should be aggregated. By default periodsJ = c(1,5,22), which corresponds to one day, one week and one month respectively.



periodsQ	a vector of integers indicating over what time periods the realized quarticity in the model should be aggregated. By default <code>periodsQ = c(1,5,22)</code> , which corresponds to one day, one week and one month respectively.
leverage	a vector of integers indicating over what periods the negative returns should be aggregated. See Corsi and Reno (2012) for more information. By default <code>leverage = NULL</code> and the model assumes the absence of a leverage effect. Set <code>leverage = c(1,5,22)</code> to mimic the analysis in Corsi and Reno (2012).
RVest	a character vector with one, two, or three elements. The first element always refers to the name of the function to estimate the daily integrated variance (non-jump-robust). The second and third element depends on which type of model is estimated: If <code>type = "HARJ"</code> , <code>type = "HARCJ"</code> , <code>type = "HARQJ"</code> the second element refers to the name of the function to estimate the continuous component of daily volatility (jump robust). If <code>type = "HARQ"</code> , the second element refers to the name of the function used to estimate the integrated quarticity. If <code>type = "HARQJ"</code> the third element always refers to the name of the function used to estimate integrated quarticity. By default <code>RVest = c("rCov", "rBPCov", "rQuar")</code> , i.e. using the realized volatility, realized bi-power variance, and realized quarticity.
type	a string referring to the type of HAR model you would like to estimate. By default <code>type = "HAR"</code> , the most basic model. Other valid options for type are <code>"HARJ"</code> , <code>"HARCJ"</code> , <code>"HARQ"</code> , <code>"HARQJ"</code> , <code>"CHAR"</code> , or <code>"CHARQ"</code> .
inputType	a string denoting if the input data consists of realized measures or high-frequency returns. Default <code>"RM"</code> is the only way to denote realized measures and everything else denotes returns.
jumpTest	the function name of a function used to test whether the test statistic which determines whether the jump variability is significant that day. By default <code>jumpTest = "ABDJumptest"</code> , hence using the test statistic in Equation or Equation (18) of Andersen et al. (2007). It is also possible to provide pre-computed test statistics for jump tests by setting <code>jumpTest</code> to <code>"testStat"</code> . These test statistics should still be passed as the third column.
alpha	a real indicating the confidence level used in testing for jumps. By default <code>alpha = 0.05</code> .
h	an integer indicating the number over how many days the dependent variable should be aggregated. By default, <code>h = 1</code> , i.e. no aggregation takes place, you just model the daily realized volatility.
transform	optionally a string referring to a function that transforms both the dependent and explanatory variables in the model. By default <code>transform = NULL</code> , so no transformation is done. Typical other choices in this context would be <code>"log"</code> or <code>"sqrt"</code> .
externalRegressor	an xts object of same number of rows as data, and one column. This is used as an external regressor. Default is <code>NULL</code> .
periodsExternal	a vector of integers indicating over how days <code>externalRegressor</code> should be aggregated.
...	extra arguments for jump test.

## Details

The basic specification in Corsi (2009) is as follows. Let  $RV_t$  be the realized variances at day  $t$  and  $RV_{t-k:t}$  the average realized variance in between  $t - k$  and  $t$ ,  $k \geq 0$ .

The dynamics of the model are given by

$$RV_{t+1} = \beta_0 + \beta_1 RV_t + \beta_2 RV_{t-4:t} + \beta_3 RV_{t-21:t} + \varepsilon_{t+1}$$

which is estimated by ordinary least squares under the assumption that at time  $t$ , the conditional mean of  $\varepsilon_{t+1}$  is equal to zero.

For other specifications, please refer to the cited papers.

The standard errors reporting in the print and summary methods are Newey-West standard errors calculated with the **sandwich** package.

## Value

The function outputs an object of class `HARmodel` and `lm` (so `HARmodel` is a subclass of `lm`). Objects of class `HARmodel` has the following methods `plot.HARmodel`, `predict.HARmodel`, `print.HARmodel`, and `summary.HARmodel`.

## Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

## References

Andersen, T. G., Bollerslev, T., and Diebold, F. (2007). Roughing it up: Including jump components in the measurement, modelling and forecasting of return volatility. *The Review of Economics and Statistics*, 89, 701-720.

Corsi, F. (2009). A simple approximate long memory model of realized volatility. *Journal of Financial Econometrics*, 7, 174-196.

Corsi, F. and Reno R. (2012). Discrete-time volatility forecasting with persistent leverage effect and the link with continuous-time volatility modeling. *Journal of Business & Economic Statistics*, 30, 368-380.

Bollerslev, T., Patton, A., and Quaedvlieg, R. (2016). Exploiting the errors: A simple approach for improved volatility forecasting, *Journal of Econometrics*, 192, 1-18.

## Examples

```
# Example 1: HAR
# Forecasting daily Realized volatility for the S&P 500 using the basic HARmodel: HAR
library(xts)
RVSPY <- as.xts(SPYRM$RV5, order.by = SPYRM$DT)

x <- HARmodel(data = RVSPY , periods = c(1,5,22), RVest = c("rCov"),
              type = "HAR", h = 1, transform = NULL, inputType = "RM")
class(x)
x
summary(x)
```

```

plot(x)
predict(x)

# Example 2: HARQ
# Get the highfrequency returns
dat <- as.xts(sampleOneMinuteData[, makeReturns(STOCK), by = list(DATE = as.Date(DT))])
x <- HARmodel(dat, periods = c(1,5,10), periodsJ = c(1,5,10),
              periodsQ = c(1), RVest = c("rCov", "rQuar"),
              type="HARQ", inputType = "returns")
# Estimate the HAR model of type HARQ
class(x)
x
# plot(x)
# predict(x)

# Example 3: HARQJ with already computed realized measures
dat <- SPYRM[, list(DT, RV5, BPV5, RQ5)]
x <- HARmodel(as.xts(dat), periods = c(1,5,22), periodsJ = c(1),
              periodsQ = c(1), type = "HARQJ")
# Estimate the HAR model of type HARQJ
class(x)
x
# plot(x)
predict(x)

# Example 4: CHAR with already computed realized measures
dat <- SPYRM[, list(DT, RV5, BPV5)]

x <- HARmodel(as.xts(dat), periods = c(1, 5, 22), type = "CHAR")
# Estimate the HAR model of type CHAR
class(x)
x
# plot(x)
predict(x)

# Example 5: CHARQ with already computed realized measures
dat <- SPYRM[, list(DT, RV5, BPV5, RQ5)]

x <- HARmodel(as.xts(dat), periods = c(1,5,22), periodsQ = c(1), type = "CHARQ")
# Estimate the HAR model of type CHARQ
class(x)
x
# plot(x)
predict(x)

# Example 6: HARCJ with pre-computed test-statistics
## BNSJumptest manually calculated.
testStats <- sqrt(390) * (SPYRM$RV1 - SPYRM$BPV1)/sqrt((pi^2/4+pi-3 - 2) * SPYRM$medRQ1)
model <- HARmodel(cbind(as.xts(SPYRM[, list(DT, RV5, BPV5)]), testStats), type = "HARCJ")

```

---

HEAVYmodel

*HEAVY model estimation*


---

**Description**

This function calculates the High frEQUENCY bAsed VolatilitY (HEAVY) model proposed in Shephard and Sheppard (2010).

**Usage**

```
HEAVYmodel(data, startingValues = NULL)
```

**Arguments**

`data` an xts object where the first column is a vector of returns and the second column is a vector of realized stock market variation

`startingValues` a vector of alternative starting values: first three arguments for variance equation and last three arguments for measurement equation.

**Details**

Let  $r_t$  and  $RM_t$  be series of demeaned returns and realized measures of daily stock price variation. The HEAVY model is a two-component model. We assume  $r_t = h_t^{1/2} Z_t$  where  $Z_t$  is an i.i.d. zero-mean and unit-variance innovation term. The dynamics of the HEAVY model are given by

$$h_t = \omega + \alpha RM_{t-1} + \beta h_{t-1}$$

and

$$\mu_t = \omega_R + \alpha_R RM_{t-1} + \beta_R \mu_{t-1}.$$

The two equations are estimated separately as mentioned in Shephard and Sheppard (2010). We report robust standard errors based on the matrix-product of inverted Hessians and the outer product of gradients.

Note that we always demean the returns in the data input as we don't include a constant in the mean equation.

**Value**

The function outputs an object of class HEAVYmodel, a list containing

- `coefficients` = estimated coefficients.
- `se` = robust standard errors based on inverted Hessian matrix.
- `residuals` = the residuals in the return equation.
- `llh` = the two-component log-likelihood values.
- `varCondVariances` = conditional variances in the variance equation.
- `RMCondVariances` = conditional variances in the RM equation.

- data = the input data.

The class `HEAVYmodel` has the following methods: `plot.HEAVYmodel`, `predict.HEAVYmodel`, `print.HEAVYmodel`, and `summary.HEAVYmodel`.

### Author(s)

Onno Kleen and Emil Sjorup.

### References

Shephard, N. and Sheppard, K. (2010). Realising the future: Forecasting with high frequency based volatility (HEAVY) models. *Journal of Applied Econometrics* 25, 197–231.

### See Also

[predict.HEAVYmodel](#)

### Examples

```
# Calculate returns in percentages
logReturns <- 100 * makeReturns(SPYRM$CLOSE)[-1]

# Combine both returns and realized measures into one xts
# Due to return calculation, the first observation is missing
dataSPY <- xts::xts(cbind(logReturns, SPYRM$BPV5[-1] * 10000), order.by = SPYRM$DT[-1])

# Fit the HEAVY model
fittedHEAVY <- HEAVYmodel(dataSPY)

# Examine the estimated coefficients and robust standard errors
fittedHEAVY

# Calculate iterative multi-step-ahead forecasts
predict(fittedHEAVY, stepsAhead = 12)
```

---

ICov

*Estimators of the integrated covariance*

---

### Description

This documentation page functions as a point of reference to quickly look up the estimators of the integrated covariance provided in the **highfrequency** package.

The implemented estimators are:

Realized covariance [rCov](#)

Realized bipower covariance [rBPCov](#)

Hayashi-Yoshida realized covariance [rHYCov](#)

Realized kernel covariance [rKernelCov](#)

Realized outlyingness-weighted covariance [rOWCov](#)

Realized threshold covariance [rThresholdCov](#)

Realized two-scale covariance [rTSCov](#)

Robust realized two-scale covariance [rRTSCov](#)

Subsampled realized covariance [rAVGCov](#)

Realized semi-covariance [rSemiCov](#)

Modulated Realized covariance [rMRCov](#)

Realized Cholesky covariance [rCholCov](#)

Beta-adjusted realized covariance [rBACov](#)

### See Also

[IVar](#) for a list of implemented estimators of the integrated variance.

---

intradayJumpTest	<i>Intraday jump tests</i>
------------------	----------------------------

---

### Description

This function can be used to test for jumps in intraday price paths.

The tests are of the form  $L(t) = (R(t) - mu(t))/sigma(t)$ .

See [spotVol](#) and [spotDrift](#) for Estimators for  $\sigma(t)$  and  $\mu(t)$ , respectively.

### Usage

```
intradayJumpTest(
  pData,
  volEstimator = "RM",
  driftEstimator = "none",
  alpha = 0.95,
  alignBy = "minutes",
  alignPeriod = 5,
  marketOpen = "09:30:00",
  marketClose = "16:00:00",
  tz = NULL,
  n = NULL,
  ...
)
```



```

alignBy = "minutes", alignPeriod = 5, marketOpen = "09:30:00",
marketClose = "16:00:00")

plot(LMtest)

# We can just as easily use the pre-averaged version from the "Fact or Friction" paper
FoFtest <- intradayJumpTest(pData = sampleTData[, list(DT, PRICE)],
volEstimator = "PARM", driftEstimator = "none",
RM = "rBPCov", lookBackPeriod = 20, theta = 1.2,
marketOpen = "09:30:00", marketClose = "16:00:00")

plot(FoFtest)

## End(Not run)

```

---

IVar

*Estimators of the integrated variance*


---

### Description

This documentation page functions as a point of reference to quickly look up the estimators of the integrated variance provided in the **highfrequency** package.

The implemented estimators are: Realized Variance [rRVar](#)

Median realized variance [rMedRVar](#)

Minimum realized variance [rMinRVar](#)

Realized quadpower variance [rQPVar](#)

Realized multipower variance [rMPVar](#)

Realized semivariance [rSVar](#)

Note that almost all estimators in the list in [ICov](#) also work yield estimates of the integrated variance on the diagonals.

### See Also

[ICov](#) for a list of implemented estimators of the integrated covariance.

---

IVinference

*Function returns the value, the standard error and the confidence band of the integrated variance (IV) estimator.*


---



**Description**

This function supplies information about standard error and confidence band of integrated variance (IV) estimators under Brownian semimartingales model such as: bipower variation, rMinRV, rMedRV. Depending on users' choices of estimator (integrated variance (IVestimator), integrated quarticity (IQestimator)) and confidence level, the function returns the result.(Barndorff (2002)) Function returns three outcomes: 1.value of IV estimator 2.standard error of IV estimator and 3.confidence band of IV estimator.

Assume there is  $N$  equispaced returns in period  $t$ .

Then the IVinference is given by:

$$\text{standard error} = \frac{1}{\sqrt{N}} * sd$$

$$\text{confidence band} = \hat{IV} \pm cv * se$$

in which,

$$sd = \sqrt{\theta \times \hat{IQ}}$$

$cv$  : critical value.

$se$  : standard error.

$\theta$  : depending on IQestimator,  $\theta$  can take different value (Andersen et al. (2012)).

$\hat{IQ}$  integrated quarticity estimator.

**Usage**

```
IVinference(
  rData,
  IVestimator = "RV",
  IQestimator = "rQuar",
  confidence = 0.95,
  alignBy = NULL,
  alignPeriod = NULL,
  makeReturns = FALSE,
  ...
)
```

**Arguments**

rData	xts object containing all returns in period t for one asset.
IVestimator	can be chosen among integrated variance estimators: RV, BV, rMinRV or rMedRV. RV by default.
IQestimator	can be chosen among integrated quarticity estimators: rQuar, realized tri-power quarticity (TPQ), quad-power quarticity (QPQ), rMinRQuar or rMedRQuar. TPQ by default.
confidence	confidence level set by users. 0.95 by default.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"

alignPeriod	positive numeric, indicating the number of periods to aggregate over. E.g. to aggregate based on a 5 minute frequency, set alignPeriod to 5 and alignBy to "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	additional arguments.

### Details

The theoretical framework is the logarithmic price process  $X_t$  belongs to the class of Brownian semimartingales, which can be written as:

$$X_t = \int_0^t a_u du + \int_0^t \sigma_u dW_u$$

where  $a$  is the drift term,  $\sigma$  denotes the spot volatility process,  $W$  is a standard Brownian motion (assume that there are no jumps).

### Value

list

### Author(s)

Giang Nguyen, Jonathan Cornelissen and Kris Boudt

### References

Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75-93.

Barndorff-Nielsen, O. E. (2002). Econometric analysis of realized volatility and its use in estimating stochastic volatility models. *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 64, 253-280.

### Examples

```
## Not run:
library("xts") # This function only accepts xts data currently
ivInf <- IVinference(as.xts(sampleTData[, list(DT, PRICE)]), IVestimator= "rMinRV",
                    IQestimator = "rMedRQ", confidence = 0.95, makeReturns = TRUE)
ivInf

## End(Not run)
```

JOjumpTest

*Jiang and Oomen (2008) tests for the presence of jumps in the price series.*

### Description

This test examines the jump in highfrequency data. It is based on theory of Jiang and Oomen (JO). They found that the difference of simple return and logarithmic return can capture one half of integrated variance if there is no jump in the underlying sample path. The null hypothesis is no jumps.

Function returns three outcomes: 1.z-test value 2.critical value under confidence level of 95% and 3.p-value.

Assume there is  $N$  equispaced returns in period  $t$ .

Let  $r_{t,i}$  be a logarithmic return (with  $i = 1, \dots, N$ ) in period  $t$ .

Let  $R_{t,i}$  be a simple return (with  $i = 1, \dots, N$ ) in period  $t$ .

Then the JOjumpTest is given by:

$$\text{JOjumpTest}_{t,N} = \frac{NBV_t}{\sqrt{\Omega_{SwV}} \left(1 - \frac{RV_t}{SwV_t}\right)}$$

in which,  $BV$ : bipower variance;  $RV$ : realized variance (defined by Andersen et al. (2012));

$$SwV_t = 2 \sum_{i=1}^N (R_{t,i} - r_{t,i})$$

$$\Omega_{SwV} = \frac{\mu_6}{9} \frac{N^3 \mu_{6/p}^{-p}}{N-p-1} \sum_{i=0}^{N-p} \prod_{k=1}^p |r_{t,i+k}|^{6/p}$$

$$\mu_p = E[|U|^p] = 2^{p/2} \frac{\Gamma(1/2(p+1))}{\Gamma(1/2)}$$

$U$ : independent standard normal random variables

$p$ : parameter (power).

### Usage

```
JOjumpTest(
  pData,
  power = 4,
  alignBy = NULL,
  alignPeriod = NULL,
  alpha = 0.975,
  ...
)
```

**Arguments**

pData	a zoo/xts object containing all prices in period t for one asset.
power	can be chosen among 4 or 6. 4 by default.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. E.g. to aggregate based on a 5 minute frequency, set alignPeriod to 5 and alignBy to "minutes".
alpha	numeric of length one with the significance level to use for the jump test(s). Defaults to 0.975.
...	Used internally, do not set.

**Details**

The theoretical framework underlying jump test is that the logarithmic price process  $X_t$  belongs to the class of Brownian semimartingales, which can be written as:

$$X_t = \int_0^t a_u du + \int_0^t \sigma_u dW_u + Z_t$$

where  $a$  is the drift term,  $\sigma$  denotes the spot volatility process,  $W$  is a standard Brownian motion and  $Z$  is a jump process defined by:

$$Z_t = \sum_{j=1}^{N_t} k_j$$

where  $k_j$  are nonzero random variables. The counting process can be either finite or infinite for finite or infinite activity jumps.

The the Jiang and Oomen test is that in the absence of jumps, the accumulated difference between the simple returns and log returns captures half of the integrated variance. (Theodosiou and Zikes, 2009). If this difference is too great, the null hypothesis of no jumps is rejected.

**Value**

list

**Author(s)**

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup

**References**

- Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75- 93.
- Jiang, J. G., and Oomen, R. C. A (2008). Testing for jumps when asset prices are observed with noise- a "swap variance" approach. *Journal of Econometrics*, 144, 352-370.
- Theodosiou, M., Zikes, F. (2009). A comprehensive comparison of alternative tests for jumps in asset prices. Unpublished manuscript, Graduate School of Business, Imperial College London.

**Examples**

```
joDT <- JOjumpTest(sampleTData[, list(DT, PRICE)])
```

---

knChooseReMeDI	<i>ReMeDI tuning parameter</i>
----------------	--------------------------------

---

**Description**

Function to choose the tuning parameter, kn in ReMeDI estimation. The optimal parameter kn is the smallest value that where the criterion:

$$SqErr(k_n)_t^n = \left( \hat{R}_{t,0}^{n,k_n} - \hat{R}_{t,1}^{n,k_n} - \hat{R}_{t,2}^{n,k_n} + \hat{R}_{t,3}^{n,k_n} - \hat{R}_{t,l}^{n,k_n} \right)^2$$

is perceived to be zero. The tuning parameter tol can be set to choose the tolerance of the perception of 'close to zero', a higher tolerance will lead to a higher optimal value.

**Usage**

```
knChooseReMeDI(
  pData,
  knMax = 10,
  tol = 0.05,
  size = 3,
  lower = 2,
  upper = 5,
  plot = FALSE
)
```

**Arguments**

pData	xts or data.table containing the log-prices of the asset.
knMax	max value of kn to be considered.
tol	tolerance for the minimizing value. If tol is high, the algorithm will choose a lower optimal value.
size	size of the local window.
lower	lower boundary for the method if it fails to find an optimal value. If this is the case, the best kn between lower and upper is returned
upper	upper boundary for the method if it fails to find an optimal value. If this is the case, the best kn between lower and upper is returned
plot	logical whether to plot the errors.

**Details**

This is the algorithm B.2 in the appendix of the Li and Linton (2019) working paper.

**Value**

integer containing the optimal kn

**Note**

We Thank Merrick Li for contributing his Matlab code for this estimator.

**Author(s)**

Emil Sjoerup.

**References**

Li, M. and Linton, O. (2019). A ReMeDI for microstructure noise. Cambridge Working Papers in Economics 1908.

**Examples**

```

optimalKn <- knChooseReMeDI(sampleTData[as.Date(DT) == "2018-01-02",],
                             knMax = 10, tol = 0.05, size = 3,
                             lower = 2, upper = 5, plot = TRUE)

optimalKn
## Not run:
# We can also have a much larger search-space
optimalKn <- knChooseReMeDI(sampleTDataEurope,
                             knMax = 50, tol = 0.05,
                             size = 3, lower = 2, upper = 5, plot = TRUE)

optimalKn

## End(Not run)

```

---

leadLag

*Lead-Lag estimation*

---

**Description**

Function that estimates whether one series leads (or lags) another.

Let  $X_t$  and  $Y_t$  be two observed price over the time interval  $[0, 1]$ .

For every integer  $k \in \mathcal{Z}$ , we form the shifted time series

$$Y_{(k+i)/n}, \quad i = 1, 2, \dots$$

$H = (\underline{H}, \overline{H}]$  is an interval for  $\vartheta \in \Theta$ , define the shift interval  $H_\vartheta = H + \vartheta = (\underline{H} + \vartheta, \overline{H} + \vartheta]$  then let

$$X(H)_t = \int_0^t 1_H(s) dX_s$$

Which will be abbreviated:

$$X(H) = X(H)_{T+\delta} = \int_0^{T+\delta} 1_H(s) dX_s$$

Then the shifted HY contrast function is:

$$\tilde{\vartheta} \rightarrow U^n(\tilde{\vartheta}) = 1_{\tilde{\vartheta} \geq 0} \sum_{I \in \mathcal{I}, J \in \mathcal{J}, \bar{I} \leq T} X(I) Y(J) 1_{\{I \cap J_{-\tilde{\vartheta}} \neq \emptyset\}} + 1_{\tilde{\vartheta} < 0} \sum_{I \in \mathcal{I}, J \in \mathcal{J}, \bar{J} \leq T} X(I) Y(Y) 1_{\{J \cap I_{\tilde{\vartheta}} \neq \emptyset\}}$$

This contrast function is then calculated for all the lags passed in the argument lags

### Usage

```
leadLag(
  price1 = NULL,
  price2 = NULL,
  lags = NULL,
  resolution = "seconds",
  normalize = TRUE,
  parallelize = FALSE,
  nCores = NA
)
```

### Arguments

price1	xts or data.table containing prices in levels, in case of data.table, use a column DT to denote the date-time in POSIXct format, and a column PRICE to denote the price
price2	xts or data.table containing prices in levels, in case of data.table, use a column DT to denote the date-time in POSIXct format, and a column PRICE to denote the price
lags	a numeric denoting which lags (in units of resolution) should be tested as leading or lagging
resolution	the resolution at which the lags is measured. The default is "seconds", use this argument to gain 1000 times resolution by setting it to either "ms", "milliseconds", or "milli-seconds".
normalize	logical denoting whether the contrasts should be normalized by the product of the L2 norms of both the prices. Default = TRUE. This does not change the value of the lead-lag-ratio.
parallelize	logical denoting whether to use a parallelized version of the C++ code (parallelized using OPENMP). Default = FALSE
nCores	integer valued numeric denoting how many cores to use for the lead-lag estimation procedure in case parallelize is TRUE. Default is NA, which does not parallelize the code.

### Details

The lead-lag-ratio (LLR) can be used to see if one asset leads the other. If  $LLR < 1$ , then price1 MAY be leading price2 and vice versa if  $LLR > 1$ .

**Value**

A list with class `leadLag` which contains contrasts, lead-lag-ratio, and lags, denoting the estimated values for each lag calculated, the lead-lag-ratio, and the tested lags respectively.

**References**

Hoffmann, M., Rosenbaum, M., and Yoshida, N. (2013). Estimation of the lead-lag parameter from non-synchronous data. *Bernoulli*, 19, 1-37.

**Examples**

```
## Not run:
# Toy example to show the usage
# Spread prices
spread <- spreadPrices(sampleMultiTradeData[SYMBOL %in% c("ETF", "AAA")])
# Use lead-lag estimator
llEmpirical <- leadLag(spread[!is.na(AAA), list(DT, PRICE = AAA)],
                      spread[!is.na(ETF), list(DT, PRICE = ETF)], seq(-15,15))
plot(llEmpirical)

## End(Not run)
```

---

listAvailableKernels Available kernels

---

**Description**

Returns a vector of the available kernels.

**Usage**

```
listAvailableKernels()
```

**Details**

The available kernels are:

- Rectangular:  $K(x) = 1$ .
- Bartlett:  $K(x) = 1 - x$ .
- Second-order:  $K(x) = 1 - 2x - x^2$ .
- Epanechnikov:  $K(x) = 1 - x^2$ .
- Cubic:  $K(x) = 1 - 3x^2 + 2x^3$ .
- Fifth:  $K(x) = 1 - 10x^3 + 15x^4 - 6x^5$ .
- Sixth:  $K(x) = 1 - 15x^4 + 24x^5 - 10x^6$ .
- Seventh:  $K(x) = 1 - 21x^5 + 35x^6 - 15x^7$ .



- Eighth:  $K(x) = 1 - 28x^6 + 48x^7 - 21x^8$ .
- Parzen:  $K(x) = 1 - 6x^2 + 6x^3$  if  $k \leq 0.5$  and  $K(x) = 2(1 - x)^3$  if  $k > 0.5$ .
- TukeyHanning:  $K(x) = 1 + \sin(\pi/2 - \pi \cdot x))/2$ .
- ModifiedTukeyHanning:  $K(x) = (1 - \sin(\pi/2 - \pi (1 - x)^2))/2$ .

**Value**

a character vector.

**Author(s)**

Scott Payseur.

**References**

Barndorff-Nielsen, O. E., Hansen, P. R., Lunde, A., and Shephard, N. (2008). Designing realized kernels to measure the ex post variation of equity prices in the presence of noise. *Econometrica*, 76, 1481-1536.

**Examples**

```
listAvailableKernels
```

---

listCholCovEstimators *Utility function listing the available estimators for the CholCov estimation*

---

**Description**

Utility function listing the available estimators for the CholCov estimation

**Usage**

```
listCholCovEstimators()
```

**Value**

This function returns a character vector containing the available estimators.

---

 makeOHLCV

*Make Open-High-Low-Close-Volume bars*


---

### Description

This function makes OHLC-V bars at arbitrary intervals. If the SIZE column is not present in the input, no volume column is created.

### Usage

```
makeOHLCV(pData, alignBy = "minutes", alignPeriod = 5, tz = NULL)
```

### Arguments

pData	data.table or xts object to make the bars out of, containing the intraday price series of possibly multiple stocks for possibly multiple days.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "secs", "seconds", "mins", "minutes", "hours", and "ticks". To aggregate based on a 5 minute frequency, set alignPeriod to 5 and alignBy to "minutes".
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5 minute frequency, set alignPeriod to 5 and alignBy to "minutes".
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. With the non-disk functionality, we attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC".

### Author(s)

Emil Sjoerup

### Examples

```
## Not run:
minuteBars <- makeOHLCV(sampleTDataEurope, alignBy = "minutes", alignPeriod = 1)
# We can use the quantmod package's chartSeries function to plot the ohlcv data
quantmod::chartSeries(minuteBars)

minuteBars <- makeOHLCV(sampleTDataEurope[,], alignBy = "minutes", alignPeriod = 1)
# Again we plot the series with chartSeries
quantmod::chartSeries(minuteBars)

# We can also handle data across multiple days.
fiveMinuteBars <- makeOHLCV(sampleTData)
# Again we plot the series with chartSeries
quantmod::chartSeries(fiveMinuteBars)
```

```
# We can use arbitrary alignPeriod, here we choose pi
bars <- makeOHLCV(sampleTDataEurope, alignBy = "seconds", alignPeriod = pi)
# Again we plot the series with chartSeries
quantmod::chartSeries(bars)

## End(Not run)
```

---

makePsd	<i>Returns the positive semidefinite projection of a symmetric matrix using the eigenvalue method</i>
---------	---

---

### Description

Function returns the positive semidefinite projection of a symmetric matrix using the eigenvalue method.

### Usage

```
makePsd(S, method = "covariance")
```

### Arguments

S	a non-PSD matrix.
method	character, indicating whether the negative eigenvalues of the correlation or covariance should be replaced by zero. Possible values are "covariance" and "correlation".

### Details

We use the eigenvalue method to transform  $S$  into a positive semidefinite covariance matrix (see, e.g., Barndorff-Nielsen and Shephard, 2004, and Rousseeuw and Molenberghs, 1993). Let  $\Gamma$  be the orthogonal matrix consisting of the  $p$  eigenvectors of  $S$ . Denote  $\lambda_1^+, \dots, \lambda_p^+$  its  $p$  eigenvalues, whereby the negative eigenvalues have been replaced by zeroes. Under this approach, the positive semi-definite projection of  $S$  is  $S^+ = \Gamma' \text{diag}(\lambda_1^+, \dots, \lambda_p^+) \Gamma$ .

If `method = "correlation"`, the eigenvalues of the correlation matrix corresponding to the matrix  $S$  are transformed, see Fan et al. (2010).

### Value

A matrix containing the positive semi definite matrix.

### Author(s)

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

## References

- Barndorff-Nielsen, O. E. and Shephard, N. (2004). Measuring the impact of jumps in multivariate price processes using bipower covariation. Discussion paper, Nuffield College, Oxford University.
- Fan, J., Li, Y., and Yu, K. (2012). Vast volatility matrix estimation using high frequency data for portfolio selection. *Journal of the American Statistical Association*, 107, 412-428
- Rousseeuw, P. and Molenberghs, G. (1993). Transformation of non positive semidefinite correlation matrices. *Communications in Statistics - Theory and Methods*, 22, 965-984.

---

makeReturns

*Compute log returns*

---

## Description

Convenience function to calculate log-returns, also used extensively internally. Accepts `xts` and `matrix`-like objects. If you use this with a `data.table` object, remember to not pass the DT column.

$$\log \text{return}_t = (\log(\text{PRICE}_t) - \log(\text{PRICE}_{t-1})).$$

## Usage

```
makeReturns(ts)
```

## Arguments

`ts` a possibly multivariate matrix-like object containing prices in levels. If `ts` is an `xts` object, we return an `xts` object. Other types will result in a `matrix`

## Details

Note: the first (row of) observation(s) is set to zero.

## Value

Depending on input, either a `matrix` or an `xts` object containing the log returns.

## Author(s)

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup

---

makeRMFormat	<i>DEPRECATED</i> use <a href="#">spreadPrices</a>
--------------	--

---

**Description**

DEPRECATED use [spreadPrices](#)

**Usage**

```
makeRMFormat(data)
```

**Arguments**

data	DEPRECATED
------	------------

---

matchTradesQuotes	<i>Match trade and quote data</i>
-------------------	-----------------------------------

---

**Description**

Match the trades and quotes of the input data. All trades are retained and the latest bids and offers are retained, while 'old' quotes are discarded.

**Usage**

```
matchTradesQuotes(
  tData,
  qData,
  lagQuotes = 0,
  BFM = FALSE,
  backwardsWindow = 3600,
  forwardsWindow = 0.5,
  plot = FALSE,
  ...
)
```

**Arguments**

tData	data.table or xts-object containing the trade data possibly with multiple symbols and over multiple days possible
qData	data.table or xts-object containing the quote data possibly with multiple symbols and over multiple days possible
lagQuotes	numeric, number of seconds the quotes are registered faster than the trades (should be round and positive). Default is 0. For older datasets, i.e. before 2010, it may be a good idea to set this to e.g. 2. See Vergote (2005)

BFM	a logical determining whether to conduct 'Backwards - Forwards matching' of trades and quotes. The algorithm tries to match trades that fall outside the bid - ask and first tries to match a small window forwards and if this fails, it tries to match backwards in a bigger window. The small window is a tolerance for inaccuracies in the timestamps of bids and asks. The backwards window allow for matching of late reported trades. I.e. block trades.
backwardsWindow	a numeric denoting the length of the backwards window used when BFM = TRUE. Default is 3600, corresponding to one hour.
forwardsWindow	a numeric denoting the length of the forwards window used when BFM = TRUE. Default is 0.5, corresponding to one half second.
plot	a logical denoting whether to visualize the forwards, backwards, and unmatched trades in a plot.
...	used internally. Don't set this parameter

**Value**

Depending on the input data type, we return either a `data.table` or an `xts` object containing the matched trade and quote data. When using the BFM algorithm, a report of the matched and unmatched trades are also returned (This is omitted when we call this function from the [tradesCleanupUsingQuotes](#) function).

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

**References**

Vergote, O. (2005). How to match trades and quotes for NYSE stocks? K.U.Leuven working paper.  
 Christensen, K., Oomen, R. C. A., Podolskij, M. (2014): Fact or Friction: Jumps at ultra high frequency. *Journal of Financial Economics*, 144, 576-599

**Examples**

```
# Multi-day input allowed
tqData <- matchTradesQuotes(sampleTData, sampleQData)
# Show output
tqData
```

---

```
mergeQuotesSameTimestamp
```

*Merge multiple quote entries with the same time stamp*

---

**Description**

Merge quote entries that have the same time stamp to a single one and returns an `xts` or a `data.table` object with unique time stamps only.

**Usage**

```
mergeQuotesSameTimestamp(qData, selection = "median")
```

**Arguments**

- |           |  |
|-----------|--|
| qData     | an xts object or data.table containing the time series data, with at least two columns named BID and OFR indicating the bid and ask price as well as two columns BIDSIZ, OFRSIZ indicating the number of round lots available at these prices. For data.table an additional column DT is necessary that stores the date/time information.  |
| selection | indicates how the bid and ask price for a certain time stamp should be calculated in case of multiple observation for a certain time stamp. By default, selection = "median", and the median price is taken. Alternatively: <ul style="list-style-type: none"> <li>• selection = "max.volume": use the (bid/ask) price of the entry with largest (bid/ask) volume.</li> <li>• selection = "weighted.average": take the weighted average of all bid (ask) prices, weighted by "BIDSIZ" ("OFRSIZ").</li> </ul> |

**Value**

Depending on the input data type, we return either a data.table or an xts object containing the quote data which has been cleaned.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

---

```
mergeTradesSameTimestamp
```

*Merge multiple transactions with the same time stamp*

---

**Description**

Merge trade entries that have the same time stamp to a single one and returns an xts or a data.table object with unique time stamps only.

**Usage**

```
mergeTradesSameTimestamp(tData, selection = "median")
```

**Arguments**

- |       |   |
|-------|---|
| tData | an xts object containing the time series data, with one column named PRICE indicating the transaction price and one column SIZE indicating the number of shares traded. |
|-------|---|

- selection indicates how the price for a certain time stamp should be calculated in case of multiple observation for a certain time stamp. By default, selection = "median", and the median price is taken. Alternatively:
- selection = "max.volume": use the price of the transaction with largest volume.
  - selection = "weighted.average": take the weighted average of all prices.

**Value**

data.table or xts object depending on input.

**Note**

previously this function returned the mean of the size of the merged trades (pre version 0.7 and when not using max.volume as the criterion), now it returns the sum.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

---

noZeroPrices

*Delete the observations where the price is zero*

---

**Description**

Function deletes the observations where the price is zero.

**Usage**

```
noZeroPrices(tData)
```

**Arguments**

tData an xts or data.table object at least containing a column PRICE.

**Value**

an xts or data.table object depending on input.

**Author(s)**

Jonathan Cornelissen and Kris Boudt.



---

noZeroQuotes	<i>Delete the observations where the bid or ask is zero</i>
--------------	---

---

**Description**

Function deletes the observations where the bid or ask is zero.

**Usage**

```
noZeroQuotes(qData)
```

**Arguments**

qData            an xts or data.table object at least containing the columns BID and OFR.

**Value**

xts object or data.table depending on type of input.

**Author(s)**

Jonathan Cornelissen and Kris Boudt.

---

plot.DBH	<i>Plotting method for DBH objects</i>
----------	--

---

**Description**

Plotting method for DBH objects

**Usage**

```
## S3 method for class 'DBH'  
plot(x, ...)
```

**Arguments**

x                an object of class DBH  
...              optional arguments, see details

**Details**

The plotting method has the following optional parameters:

- `pData` A `data.table` or an `xts` object, containing the prices and timestamps of the data used to calculate the test statistic. If specified, and `which = "tStat"`, the price will be shown on the right y-axis along with the test statistic
- `which` A string denoting which of four plots to make. `"tStat"` denotes plotting the test statistic. `"sigma"` denotes plotting the estimated volatility process. `"mu"` denotes plotting the estimated drift process. If `which = c("sigma", "mu")` or `which = c("mu", "sigma")`, both the drift and volatility processes are plotted. `CaPiTAlizAtIOn` doesn't matter

**Author(s)**

Emil Sjoerup

**Examples**

```
# Testing every 60 seconds after 09:15:00
DBH <- driftBursts(sampleTDataEurope, testTimes = seq(32400 + 900, 63000, 60), preAverage = 2,
                  ACLag = -1L, meanBandwidth = 300L, varianceBandwidth = 900L)

plot(DBH)
plot(DBH, pData = sampleTDataEurope)
plot(DBH, which = "sigma")
plot(DBH, which = "mu")
plot(DBH, which = c("sigma", "mu"))
```

---

plot.HARmodel

*Plotting method for HARmodel objects*

---

**Description**

Plotting method for HARmodel objects

**Usage**

```
## S3 method for class 'HARmodel'
plot(x, ...)
```

**Arguments**

`x` an object of class `HARmodel`  
`...` extra arguments, see details

**Details**

The plotting method has the following optional parameter:

- `legend.loc` A string denoting the location of the legend passed on to `addLegend` of the `xts` package

---

plot.HEAVYmodel	<i>Plotting method for HEAVYmodel objects</i>
-----------------	---

---

**Description**

Plotting method for HEAVYmodel objects

**Usage**

```
## S3 method for class 'HEAVYmodel'
plot(x, ...)
```

**Arguments**

x	an object of class HEAVYmodel.
...	extra arguments, see details.

**Details**

The plotting method has the following optional parameter:

- legend.loc A string denoting the location of the legend passed on to addLegend of the **xts** package
- type A string denoting the type of lot to be made. If type is "condVar" the fitted values of the conditional variance of the returns is shown. If type is different from "condVar", the fitted values of the realized measure is shown. Default is "condVar"

---

plotTQData	<i>Plot Trade and Quote data</i>
------------	----------------------------------

---

**Description**

Plot trade and quote data, trades are marked by crosses, and quotes are plotted as boxes denoting the bid-offer spread for all the quotes.

**Usage**

```
plotTQData(
  tData,
  qData = NULL,
  xLim = NULL,
  tradeCol = "black",
  quoteCol = "darkgray",
  format = "%H:%M:%S",
  axisCol = "black",
  ...
)
```

**Arguments**

tData	cleaned trades data
qData	cleaned quotes data
xLim	timestamps for the start and the end of the plots.
tradeCol	color in which to paint the trade crosses.
quoteCol	color in which to fill out the bid-offer spread.
format	format string to pass to axis.POSIXct when creating the timestamps on the x axis. If you are plotting a very short time interval, use "%H:%M:%OS" to get fractional seconds on the time axis.
axisCol	string to denote which color to use for the x axis
...	passed to plot and points.

**Examples**

```
## Not run:
cleanedQuotes = quotesCleanup(qDataRow = sampleQDataRow, report = FALSE, printExchange = FALSE)
cleanedTrades <- tradesCleanupUsingQuotes(
  tData = tradesCleanup(tDataRow = sampleTDataRow, report = FALSE, printExchange = FALSE),
  qData = quotesCleanup(qDataRow = sampleQDataRow, report = FALSE, printExchange = FALSE)
)[as.Date(DT) == "2018-01-03"]
xLim <- range(as.POSIXct(c("2018-01-03 15:30:00", "2018-01-03 16:00:00"), tz = "EST"))
plotTQData(cleanedTrades, cleanedQuotes, xLim = xLim,
  main = "Raw trade and quote data from NYSE TAQ")

## End(Not run)
```

---

predict.HARmodel      *Predict method for objects of type HARmodel*

---

**Description**

Predict method for objects of type HARmodel

**Usage**

```
## S3 method for class 'HARmodel'
predict(object, ...)
```

**Arguments**

object	an object of class HARmodel
...	extra arguments. See details

**Details**

The print method has the following optional parameters:

- newdata new data to use for forecasting
- warnings A logical denoting whether to display warnings, default is TRUE
- backtransform A string. If the model is estimated with transformation this parameter can be set to transform the prediction back into variance The possible values are "simple" which means inverse of transformation, i.e. exp when log-transformation is applied. If using log transformation, the option "parametric" can also be used to transform back. The parametric method adds a correction that stems from using the log-transformation

---

predict.HEAVYmodel      *Iterative multi-step-ahead forecasting for HEAVY models*

---

**Description**

Calculates forecasts for  $h_{T+k}$ , where  $T$  denotes the end of the estimation period for fitting the HEAVYmodel and  $k = 1, \dots, \text{stepsAhead}$ .

**Usage**

```
## S3 method for class 'HEAVYmodel'
predict(object, stepsAhead = 10, ...)
```

**Arguments**

object	an object of class HEAVYmodel.
stepsAhead	the number of days iterative forecasts are calculated for (default 10).
...	further arguments passed to or from other methods.

---

print.DBH      *Printing method for DBH objects*

---

**Description**

Printing method for DBH objects

**Usage**

```
## S3 method for class 'DBH'
print(x, ...)
```

**Arguments**

x                    an object of class DBH  
 ...                  optional arguments, see details

**Details**

The print method has the following optional parameters:

- `criticalValue` A numeric denoting a custom critical value of the test.
- `alpha` A numeric denoting the confidence level of the test. The alpha value is passed on to [getCriticalValues](#). The default value is 0.95

**Author(s)**

Emil Sjoerup

**Examples**

```
## Not run:
DBH <- driftBursts(sampleTDataEurope, testTimes = seq(32400 + 900, 63000, 300), preAverage = 2,
                  ACLag = -1L, meanBandwidth = 300L, varianceBandwidth = 900L)
print(DBH)
print(DBH, criticalValue = 1) # This value doesn't make sense - don't actually use it!
print(DBH, alpha = 0.95) # 5% confidence level - this is the standard
print(DBH, alpha = 0.99) # 1% confidence level

## End(Not run)
```

---

`print.HARmodel`

*Printing method for HARmodel objects*

---

**Description**

Printing method for HARmodel objects

**Usage**

```
## S3 method for class 'HARmodel'
print(x, ...)
```

**Arguments**

x                    object of type HARmodel  
 ...                  extra options

**Details**

The printing method has the extra option `digits` which can be used to set the number of digits for printing pass `lag` to determine the maximum order of the Newey West estimator. Default is 22

---

quotesCleanup	<i>Cleans quote data</i>
---------------	--------------------------

---

### Description

This is a wrapper function for cleaning the quote data in the entire folder `dataSource`. The result is saved in the folder `dataDestination`.

In case you supply the argument `qDataRaw`, the on-disk functionality is ignored and the function returns the cleaned quotes as `xts` or `data.table` object (see examples).

The following cleaning functions are performed sequentially: [noZeroQuotes](#), [exchangeHoursOnly](#), [autoSelectExchangeQuotes](#) or [selectExchange](#), [rmNegativeSpread](#), [rmLargeSpread](#), [mergeQuotesSameTimestamp](#), [rmOutliersQuotes](#).

### Usage

```
quotesCleanup(
  dataSource = NULL,
  dataDestination = NULL,
  exchanges = "auto",
  qDataRaw = NULL,
  report = TRUE,
  selection = "median",
  maxi = 50,
  window = 50,
  type = "standard",
  marketOpen = "09:30:00",
  marketClose = "16:00:00",
  rmoutliersmaxi = 10,
  printExchange = TRUE,
  saveAsXTS = FALSE,
  tz = NULL
)
```

### Arguments

<code>dataSource</code>	character indicating the folder in which the original data is stored.
<code>dataDestination</code>	character indicating the folder in which the cleaned data is stored.
<code>exchanges</code>	vector of stock exchange symbols for all data in <code>dataSource</code> , e.g. <code>exchanges = c("T", "N")</code> retrieves all stock market data from both NYSE and NASDAQ. The possible exchange symbols are: <ul style="list-style-type: none"> <li>• A: AMEX</li> <li>• N: NYSE</li> <li>• B: Boston</li> <li>• P: Arca</li> </ul>

- C: NSX
- T/Q: NASDAQ
- D: NASD ADF and TRF
- X: Philadelphia
- I: ISE
- M: Chicago
- W: CBOE
- Z: BATS

. The default value is "auto" which automatically selects the exchange for the stocks and days independently using the [autoSelectExchangeQuotes](#)

qDataRaw	xts or data.table object containing raw quote data, possibly for multiple symbols over multiple days. This argument is NULL by default. Enabling it means the arguments dataSource and dataDestination will be ignored. (only advisable for small chunks of data)
report	boolean and TRUE by default. In case it is true and we don't use the on-disk functionality, the function returns (also) a vector indicating how many quotes were deleted by each cleaning step.
selection	argument to be passed on to the cleaning routine <a href="#">mergeQuotesSameTimestamp</a> . The default is "median".
maxi	spreads which are greater than median spreads of the day times maxi are excluded.
window	argument to be passed on to the cleaning routine <a href="#">rmOutliersQuotes</a> .
type	argument to be passed on to the cleaning routine <a href="#">rmOutliersQuotes</a> .
marketOpen	passed to <a href="#">exchangeHoursOnly</a> . A character in the format of "HH:MM:SS", specifying the starting hour, minute and second of an exchange.
marketClose	passed to <a href="#">exchangeHoursOnly</a> . A character in the format of "HH:MM:SS", specifying the closing hour, minute and second of an exchange.
rmoutliersmaxi	argument to be passed on to the cleaning routine <a href="#">rmOutliersQuotes</a> .
printExchange	Argument passed to <a href="#">autoSelectExchangeQuotes</a> indicates whether the chosen exchange is printed on the console, default is TRUE. This is only used when exchanges is "auto"
saveAsXTS	indicates whether data should be saved in xts format instead of data.table when using on-disk functionality. FALSE by default, which means we save as data.table.
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. With the non-disk functionality, we attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC". In the on-disk functionality, if tz is not specified, the timezone used will be the system default.



## Details

Using the on-disk functionality with .csv.zip files which is the standard from the WRDS database will write temporary files on your machine - we try to clean up after it, but cannot guarantee that there won't be files that slip through the crack if the permission settings on your machine does not match ours.

If the input data.table does not contain a DT column but it does contain DATE and TIME\_M columns, we create the DT column by REFERENCE, altering the data.table that may be in the user's environment!

## Value

The function converts every (compressed) csv (or rds) file in dataSource into multiple xts or data.table files.

In dataDestination, there will be one folder for each symbol containing .rds files with cleaned data stored either in data.table or xts format.

In case you supply the argument qDataRow, the on-disk functionality is ignored and the function returns a list with the cleaned quotes as an xts or data.table object depending on input (see examples).

## Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

## References

Barndorff-Nielsen, O. E., Hansen, P. R., Lunde, A., and Shephard, N. (2009). Realized kernels in practice: Trades and quotes. *Econometrics Journal* 12, C1-C32.

Brownlees, C.T. and Gallo, G.M. (2006). Financial econometric analysis at ultra-high frequency: Data handling concerns. *Computational Statistics & Data Analysis*, 51, pages 2232-2245.

Falkenberry, T.N. (2002). High frequency data filtering. Unpublished technical report.

## Examples

```
# Consider you have raw quote data for 1 stock for 2 days
head(sampleQDataRow)
dim(sampleQDataRow)
qDataAfterCleaning <- quotesCleanup(qDataRow = sampleQDataRow, exchanges = "N")
qDataAfterCleaning$report
dim(qDataAfterCleaning$qData)

# In case you have more data it is advised to use the on-disk functionality
# via "dataSource" and "dataDestination" arguments
```

---

rankJumpTest	<i>Rank jump test</i>
--------------	-----------------------

---

### Description

Calculate the rank jump test of Li et al. (2019). The procedure tests for the rank of the jump matrix at simultaneous jump events in market returns as well as individual assets.

### Usage

```
rankJumpTest(
  marketPrice,
  stockPrices,
  alpha = c(5, 3),
  coarseFreq = 10,
  localWindow = 30,
  rank = 1,
  BoxCox = 1,
  quantiles = c(0.9, 0.95, 0.99),
  nBoot = 1000,
  dontTestAtBoundaries = TRUE,
  alignBy = "minutes",
  alignPeriod = 5,
  marketOpen = "09:30:00",
  marketClose = "16:00:00",
  tz = NULL
)
```

### Arguments

marketPrice	data.table or xtscontaining the market prices in levels
stockPrices	list containing the individual stock prices in either data.table or xtsformat. The format should be the the same as marketPrice
alpha	significance level (in standard deviations) to use for the jump detections. Default is c(5, 3) for 5 and 3 in the market and stocks respectively.
coarseFreq	numeric denoting the coarse sampling frequency. Default is 10
localWindow	numeric denoting the local window for the bootstrap algorithm. Default is 30
rank	rank of the jump matrix under the null hypothesis. Default is 1
BoxCox	numeric of exponents for the Box-Cox transformation, default is 1
quantiles	numeric denoting which quantiles of the bootstrapped critical values to return and compare against. Default is c(0.9, 0.95, 0.99)
nBoot	numeric denoting how many replications to be used for the bootstrap algorithm. Default is 1000

dontTestAtBoundaries	logical determining whether to exclude data across different days. Default is TRUE
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "secs", "seconds", "mins", "minutes", "hours", and "ticks". To aggregate based on a 5 minute frequency, set alignPeriod to 5 and alignBy to "minutes".
alignPeriod	positive numeric, indicating the number of periods to aggregate over. E.g. to aggregate based on a 5 minute frequency, set alignPeriod to 5 and alignBy to "minutes".
marketOpen	the market opening time, by default: marketOpen = "09:30:00".
marketClose	the market closing time, by default: marketClose = "16:00:00".
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. We attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC"

## Details

Let the jump times be defined as:

$$\mathcal{I}_n = \{i : |\Delta_i^n Z| > u_n\}$$

Then the estimated jump matrix is:

$$\hat{\mathbf{J}}_n = [\Delta_{i,k}^n \mathbf{X}]_{i \in \mathcal{I}_n}$$

Let  $\hat{\lambda}_{n,1}^2 \geq \hat{\lambda}_{n,2}^2 \geq \dots \geq \hat{\lambda}_{n,d}^2$  be the ordered eigenvalues of  $\hat{\mathbf{J}}_n \hat{\mathbf{J}}_n'$ , then test statistic is

$$\hat{S}_{n,t} = \sum_{j=r+1}^d \hat{\lambda}_{n,j}^2.$$

The critical values are computed by applying a bootstrapping method

The singular value decomposition of the jump matrix  $\hat{\mathbf{J}}_n$  is:

$$\hat{\mathbf{J}} = \hat{\mathbf{U}}_n \hat{\mathbf{D}}_n \hat{\mathbf{V}}_n'$$

then  $\hat{\mathbf{U}}_n = [\hat{\mathbf{U}}_{1n} : \hat{\mathbf{U}}_{2n}]$  and  $\hat{\mathbf{V}}_n = [\hat{\mathbf{V}}_{1n} : \hat{\mathbf{V}}_{2n}]$

$\mathbf{v}_n = (v_{j,n})_{1 \leq j \leq d}$  such that  $v_{j,n} \asymp \Delta_n^\varpi$  for  $\varpi \in (0, 1/2)$  which is used to trim jumps. The bootstrapping method is calculated by the following algorithm

- Step 1.

For each  $i \in \mathcal{I}_n$ , draw  $\kappa_i^* \sim \text{Uniform}[0, 1]$  and draw with equal probability,

$$\boldsymbol{\xi}_{n,i-}^* \text{ from } \{ \min(\max(\Delta_{i-j}^n \mathbf{X}, -\mathbf{v}_n), \mathbf{v}_n) : 1 \leq j \leq k_n \},$$

$$\boldsymbol{\xi}_{n,i+}^* \text{ from } \{ \min(\max(\Delta_{i+j}^n \mathbf{X}, -\mathbf{v}_n), \mathbf{v}_n) : 1 \leq j \leq k_n \},$$

and set  $\boldsymbol{\zeta}_{n,i}^* = \sqrt{\kappa_i^*} \boldsymbol{\xi}_{n,i-}^* + \sqrt{k - \kappa_i^*} \boldsymbol{\xi}_{n,i+}^*$  and  $\boldsymbol{\zeta}_n^* = [\boldsymbol{\zeta}_{n,i}^*]_{i \in \mathcal{I}_n}$

- Step 2.

Repeat 1 for a large number of iterations. Set  $cv_{n,\alpha}$  as as the  $1 - \alpha$  quantile of  $\left\| \hat{U}'_{2n} \xi_n^* \hat{V}_{2n} \right\|^2$  in the simulated sample.

### Value

A list containing `criticalValues` which are the bootstrapped critical values, `testStatistic` the test statistic of the jump test, `dimensions` which are the dimensions of the jump matrix `marketJumpDetections` the jumps detected in the market prices, `stockJumpDetections` the co-jumps detected in the individual stock prices, and `jumpIndices` which are the indices of the detected jumps.

### Author(s)

Emil Sjoerup, based on Matlab code provided by Li et al. (2019)

### References

Li, j., Todorov, V., Tauchen, G., and Lin, H. (2019). Rank Tests at Jump Events. *Journal of Business & Economic Statistics*, 37, 312-321.

---

rAVGCov

*Realized covariances via subsample averaging*

---

### Description

Calculates realized variances via averaging across partially overlapping grids, first introduced by Zhang et al. (2005). This estimator is basically an average across different `rCov` estimates that start at different points in time, see details below.

### Usage

```
rAVGCov(
  rData,
  cor = FALSE,
  alignBy = "minutes",
  alignPeriod = 5,
  k = 1,
  makeReturns = FALSE,
  ...
)
```

### Arguments

<code>rData</code>	an <code>xts</code> or <code>data.table</code> object containing returns or prices, possibly for multiple assets over multiple days.
<code>cor</code>	boolean, in case it is <code>TRUE</code> , and the input data is multivariate, the correlation is returned instead of the covariance matrix. <code>FALSE</code> by default.

alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
k	numeric denoting which horizon to use for the subsamples. This can be a fraction as long as $k$ is a divisor of alignPeriod default is 1.
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	used internally, do not change.

### Details

Suppose that in period  $t$ , there are  $N$  equispaced returns  $r_{i,t}$  and let  $\Delta$  be equal to alignPeriod. For  $i \geq \Delta$ , we define the subsampled  $\Delta$ -period return as

$$\tilde{r}_{t,i} = \sum_{k=0}^{\Delta-1} r_{t,i-k}.$$

Now define  $N^*(j) = N/\Delta$  if  $j = 0$  and  $N^*(j) = N/\Delta - 1$  otherwise. The  $j$ -th component of the rAVGCov estimator is given by

$$RV_t^j = \sum_{i=1}^{N^*(j)} \tilde{r}_{t,j+i\Delta}^2.$$

Now taking the average across the different  $RV_t^j$ ,  $j = 0, \dots, \Delta - 1$ , defines the rAVGCov estimator. The multivariate version follows analogously.

Note that Liu et al. (2015) show that rAVGCov is not only theoretically but also empirically a more reliable estimator than rCov.

### Value

in case the input is and contains data from one day, an  $N$  by  $N$  matrix is returned. If the data is a univariate xts object with multiple days, an xts is returned. If the data is multivariate and contains multiple days (xts or data.table), the function returns a list containing  $N$  by  $N$  matrices. Each item in the list has a name which corresponds to the date for the matrix.

### Author(s)

Scott Payseur, Onno Kleen, and Emil Sjoerup.

### References

- Liu, L. Y., Patton, A. J., Sheppard, K. (2015). Does anything beat 5-minute RV? A comparison of realized measures across multiple asset classes. *Journal of Econometrics*, 187, 293-311.
- Zhang, L., Mykland, P. A., and Ait-Sahalia, Y. (2005). A tale of two time scales: Determining integrated volatility with noisy high-frequency data. *Journal of the American Statistical Association*, 100, 1394-1411.

**See Also**

[ICov](#) for a list of implemented estimators of the integrated covariance.

**Examples**

```
# Average subsampled realized variance/covariance aligned at one minute returns at
# 5 sub-grids (5 minutes).

# Univariate subsampled realized variance
rvAvgSub <- rAVGCov(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
                  makeReturns = TRUE)
rvAvgSub

# Multivariate subsampled realized variance
rvAvgCovSub <- rAVGCov(rData = sampleOneMinuteData[1:391], makeReturns = TRUE)
rvAvgCovSub
```

rBACov

*rBACov***Description**

The Beta Adjusted Covariance (BAC) equals the pre-estimator plus a minimal adjustment matrix such that the covariance-implied stock-ETF beta equals a target beta.

The BAC estimator works by applying a minimum correction factor to a pre-estimated covariance matrix such that a target beta derived from the ETF is reached.

Let

$$\bar{\beta}$$

denote the implied beta derived from the pre-estimator, and

$$\beta_{\bullet}$$

denote the target beta, then the correction factor is calculated as:

$$L(\bar{\beta} - \beta_{\bullet}),$$

where

$$L = \left( I_{d^2} - \frac{1}{2} Q \right) \bar{W}' \left( I_{d^2} \left( \sum_{k=1}^d \frac{\sum_{m=1}^{n_k} \left( w_{t_{m-1}}^k \right)^2}{n_k} \right) - \frac{\bar{W} Q \bar{W}'}{2} \right)^{-1},$$

where  $d$  is the number of assets in the ETF, and  $n_k$  is the number of trades in the  $k$ th asset, and

$$\bar{W}^k = \left( 0'_{(k-1)d}, \frac{1}{n_1} \sum_{m=1}^{n_1} w_{t_{m-1}}^1, \dots, \frac{1}{n_d} \sum_{m=1}^{n_d} w_{t_{m-1}}^d, 0'_{(d-k)d} \right),$$

where  $w_{t_{m-1}}^k$  is the weight of the  $k$ th asset in the ETF.

and

$$\mathcal{Q}^{(i-1)d+j}$$

is defined by the following two cases:

$$\begin{pmatrix} 0'_{(i-1)d+j-1}, 1, 0'_{(d-i+1)d-j} \end{pmatrix} + \begin{pmatrix} 0'_{(j-1)d+i-1}, -1, 0'_{(d-j+1)d-i} \end{pmatrix} \quad \text{if } i \neq j;$$

$$0'_{d^2} \quad \text{otherwise.}$$

$\bar{W}^k$  has dimensions  $d \times d^2$  and  $\mathcal{Q}^{(i-1)d+j}$  has dimensions  $d^2 \times d^2$ .

The Beta-Adjusted Covariance is then

$$\Sigma^{\text{BAC}} = \Sigma - L(\bar{\beta} - \beta_{\bullet}),$$

where  $\Sigma$  is the pre-estimated covariance matrix.

## Usage

```
rBACov(
  pData,
  shares,
  outstanding,
  nonEquity,
  ETFNAME = "ETF",
  unrestricted = TRUE,
  targetBeta = c("HY", "VAB", "expert"),
  expertBeta = NULL,
  preEstimator = "rCov",
  noiseRobustEstimator = rTSCov,
  noiseCorrection = FALSE,
  returnL = FALSE,
  ...
)
```

## Arguments

pData	a named list. Each list-item contains an xts or data.table object with the intraday price data of an ETF and its component stocks. xts objects are turned into data.tables
shares	a numeric with length corresponding to the number of component stocks in the ETF. The entries are the stock holdings of the ETF in the corresponding stock. The order of these entries should correspond to the order the stocks are listed in the list passed in the pData argument.
outstanding	number of shares outstanding of the ETF
nonEquity	aggregated value of the additional components (like cash, money-market funds, bonds, etc.) of the ETF which are not included in the components in pData.
ETFNAME	a character denoting which entry in the pData list is the ETF. Default is "ETF"
unrestricted	a logical denoting whether to use the unrestricted estimator, which is an extension that also affects the diagonal. Default is FALSE





```

0.02, -0.03, 0.05, -0.03,
0.04, 0.02, -0.03, 0.08), ncol = 4))
# We assume that the assets don't trade in a synchronous manner
w1 <- rets[sort(sample(1:nrow(rets), size = nrow(rets) * 0.5)), 1]
w2 <- rets[sort(sample(1:nrow(rets), size = nrow(rets) * 0.75)), 2]
w3 <- rets[sort(sample(1:nrow(rets), size = nrow(rets) * 0.65)), 3]
w4 <- rets[sort(sample(1:nrow(rets), size = nrow(rets) * 0.8)), 4]
w5 <- rnorm(nrow(rets) * 0.9, mean = 0, sd = 0.005)
timestamps1 <- seq(34200, 57600, length.out = length(w1))
timestamps2 <- seq(34200, 57600, length.out = length(w2))
timestamps3 <- seq(34200, 57600, length.out = length(w3))
timestamps4 <- seq(34200, 57600, length.out = length(w4))
timestamps5 <- seq(34200, 57600, length.out = length(w5))

w1 <- xts(w1 * c(0,sqrt(diff(timestamps1) / (max(timestamps1) - min(timestamps1))))),
as.POSIXct(timestamps1, origin = "1970-01-01"), tzzone = "UTC")
w2 <- xts(w2 * c(0,sqrt(diff(timestamps2) / (max(timestamps2) - min(timestamps2))))),
as.POSIXct(timestamps2, origin = "1970-01-01"), tzzone = "UTC")
w3 <- xts(w3 * c(0,sqrt(diff(timestamps3) / (max(timestamps3) - min(timestamps3))))),
as.POSIXct(timestamps3, origin = "1970-01-01"), tzzone = "UTC")
w4 <- xts(w4 * c(0,sqrt(diff(timestamps4) / (max(timestamps4) - min(timestamps4))))),
as.POSIXct(timestamps4, origin = "1970-01-01"), tzzone = "UTC")
w5 <- xts(w5 * c(0,sqrt(diff(timestamps5) / (max(timestamps5) - min(timestamps5))))),
as.POSIXct(timestamps5, origin = "1970-01-01"), tzzone = "UTC")

p1 <- exp(cumsum(w1))
p2 <- exp(cumsum(w2))
p3 <- exp(cumsum(w3))
p4 <- exp(cumsum(w4))

weights <- runif(4) * 1:4
weights <- weights / sum(weights)
p5 <- xts(rowSums(cbind(w1 * weights[1], w2 * weights[2], w3 * weights[3], w4 * weights[4]),
na.rm = TRUE),
index(cbind(p1, p2, p3, p4)))
p5 <- xts(cumsum(rowSums(cbind(p5, w5), na.rm = TRUE)), index(cbind(p5, w5)))

p5 <- exp(p5[sort(sample(1:length(p5), size = nrow(rets) * 0.9))])

BAC <- rBACov(pData = list(
"ETF" = p5, "STOCK 1" = p1, "STOCK 2" = p2, "STOCK 3" = p3, "STOCK 4" = p4
), shares = 1:4, outstanding = 1, nonEquity = 0, ETFNAME = "ETF",
unrestricted = FALSE, preEstimator = "rCov", noiseCorrection = FALSE,
returnL = FALSE, K = 2, J = 1)

# Noise robust version of the estimator
noiseRobustBAC <- rBACov(pData = list(
"ETF" = p5, "STOCK 1" = p1, "STOCK 2" = p2, "STOCK 3" = p3, "STOCK 4" = p4
), shares = 1:4, outstanding = 1, nonEquity = 0, ETFNAME = "ETF",
unrestricted = FALSE, preEstimator = "rCov", noiseCorrection = TRUE,
noiseRobustEstimator = rHYCov, returnL = FALSE, K = 2, J = 1)

```

```

# Use the Variance Adjusted Beta method
# Also use a different pre-estimator.
VABBAC <- rBACov(pData = list(
  "ETF" = p5, "STOCK 1" = p1, "STOCK 2" = p2, "STOCK 3" = p3, "STOCK 4" = p4
), shares = 1:4, outstanding = 1, nonEquity = 0, ETFNAME = "ETF",
  unrestricted = FALSE, targetBeta = "VAB", preEstimator = "rHYov",
  noiseCorrection = FALSE, returnL = FALSE, Lin = FALSE, L = 0, K = 2, J = 1)

## End(Not run)

```

---

rBeta

*Realized beta*


---

### Description

Depending on users' choices of estimator (realized covariance (RCOVestimator) and realized variance (RVestimator)), the function returns the realized beta, defined as the ratio between both.

The realized beta is given by

$$\beta_{jm} = \frac{RCOVestimator_{jm}}{RVestimator_m}$$

in which

*RCOVestimator* : Realized covariance of asset *j* and market index *m*.

*RVestimator* : Realized variance of market index *m*.

### Usage

```

rBeta(
  rData,
  rIndex,
  RCOVestimator = "rCov",
  RVestimator = "rRVar",
  makeReturns = FALSE,
  ...
)

```

### Arguments

*rData* a xts object containing all returns in period *t* for one asset.

*rIndex* a xts object containing return in period *t* for an index.

*RCOVestimator* can be chosen among realized covariance estimators: "rCov", "rAVGCov", "rBPCov", "rHYCov", "rKernelCov", "rOWCov", "rRTSCov", "rThresholdCov" and "rTSCov" "rCov" by default.

RVestimator	can be chosen among realized variance estimators: "rRVar", "rMinRVar" and "rMedRVar". "rRVar" by default. In case of missing RVestimator, RCOVestimator function applying for rIndex will be used.
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	arguments passed to RCOVestimator and RVestimator

### Details

Suppose there are  $N$  equispaced returns on day  $t$  for the asset  $j$  and the index  $m$ . Denote  $r_{(j)i,t}$ ,  $r_{(m)i,t}$  as the  $i$ th return on day  $t$  for asset  $j$  and index  $m$  (with  $i = 1, \dots, N$ ).

By default, the RCov is used and the realized beta coefficient is computed as:

$$\hat{\beta}_{(jm)t} = \frac{\sum_{i=1}^N r_{(j)i,t} r_{(m)i,t}}{\sum_{i=1}^N r_{(m)i,t}^2}.$$

Note: The function does not support to calculate betas across multiple days.

### Value

numeric

### Author(s)

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

### References

Barndorff-Nielsen, O. E. and Shephard, N. (2004). Econometric analysis of realized covariation: high frequency based covariance, regression, and correlation in financial economics. *Econometrica*, 72, 885-925.

### Examples

```
## Not run:
library("xts")
a <- as.xts(sampleOneMinuteData[as.Date(DT) == "2001-08-04", list(DT, MARKET)])
b <- as.xts(sampleOneMinuteData[as.Date(DT) == "2001-08-04", list(DT, STOCK)])
rBeta(a, b, RCOVestimator = "rBPCov", RVestimator = "rMinRVar", makeReturns = TRUE)

## End(Not run)
```

rBPCov

*Realized bipower covariance***Description**

Calculate the Realized BiPower Covariance (rBPCov), defined in Barndorff-Nielsen and Shephard (2004).

Let  $r_{t,i}$  be an intraday  $N \times 1$  return vector and  $i = 1, \dots, M$  the number of intraday returns.

The rBPCov is defined as the process whose value at time  $t$  is the  $N$ -dimensional square matrix with  $k, q$ -th element equal to

$$\text{rBPCov}[k, q]_t = \frac{\pi}{8} \left( \sum_{i=2}^M |r_{(k)t,i} + r_{(q)t,i}| |r_{(k)t,i-1} + r_{(q)t,i-1}| - |r_{(k)t,i} - r_{(q)t,i}| |r_{(k)t,i-1} - r_{(q)t,i-1}| \right),$$

where  $r_{(k)t,i}$  is the  $k$ -th component of the return vector  $r_{i,t}$ .

**Usage**

```
rBPCov(
  rData,
  cor = FALSE,
  alignBy = NULL,
  alignPeriod = NULL,
  makeReturns = FALSE,
  makePsd = FALSE,
  ...
)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days
cor	boolean, in case it is TRUE, and the input data is multivariate, the correlation is returned instead of the covariance matrix. FALSE by default.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. E.g. to aggregate based on a 5-minute frequency, set alignPeriod to 5 and alignBy to "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
makePsd	boolean, in case it is TRUE, the positive definite version of rBPCov is returned. FALSE by default.
...	used internally, do not change.

**Value**

in case the input is and contains data from one day, an  $N$  by  $N$  matrix is returned. If the data is a univariate xts object with multiple days, an xts is returned. If the data is multivariate and contains multiple days (xts or data.table), the function returns a list containing  $N$  by  $N$  matrices. Each item in the list has a name which corresponds to the date for the matrix.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

Barndorff-Nielsen, O. E., and Shephard, N. (2004). Measuring the impact of jumps in multivariate price processes using bipower covariation. Discussion paper, Nuffield College, Oxford University.

**See Also**

[ICov](#) for a list of implemented estimators of the integrated covariance.

**Examples**

```
# Realized Bipower Variance/Covariance for a price series aligned
# at 5 minutes.

# Univariate:
rbpv <- rBPCov(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
              alignPeriod = 5, makeReturns = TRUE)

# Multivariate:
rbpc <- rBPCov(rData = sampleOneMinuteData, makeReturns = TRUE, makePsd = TRUE)
rbpc
```

---

rCholCov

*CholCov estimator*


---

**Description**

Positive semi-definite covariance estimation using the CholCov algorithm. The algorithm estimates the integrated covariance matrix by sequentially adding series and using ‘refreshTime’ to synchronize the observations. This is done in order of liquidity, which means that the algorithm uses more data points than most other estimation techniques.

**Usage**

```
rCholCov(
  pData,
  IVest = "rMRCov",
  COVest = "rMRCov",
  criterion = "squared duration",
  ...
)
```

### Arguments

pData	a list. Each list-item $i$ contains an xts object with the intraday price data (in levels) of stock $i$ for day $t$ . The order of the data does not matter as it will be sorted according to the criterion specified in the criterion argument
IVest	integrated variance estimator, default is "rMRCov". For a list of implemented estimators, use listCholCovEstimators().
COVest	covariance estimator, default is "rMRCov". For a list of implemented estimators, use listCholCovEstimators().
criterion	criterion to use for sorting the data according to liquidity. Possible values are "squared duration", "duration", "count", defaults to "squared duration".
...	additional arguments to pass to IVest and COVest. See details.

### Details

Additional arguments for IVest and COVest should be passed in the ... argument. For the rMRCov estimator, which is the default, the theta and delta parameters can be set. These default to 1 and 0.1 respectively.

The CholCov estimation algorithm is useful for estimating covariances of  $d$  series that are sampled asynchronously and with different liquidities. The CholCov estimation algorithm is as follows:

- First sort the series in terms of decreasing liquidity according to a liquidity criterion, such that series 1 is the most liquid, and series  $d$  the least.
- Step 1:  
Apply refresh-time on  $a = \{1\}$  to obtain the grid  $\tau^a$ .  
Estimate  $\hat{g}_{11}$  using an IV estimator on  $f_{\tau_j^a}^{(1)} = \hat{u}_{\tau_j^a}^{(1)}$ .
- Step 2:  
Apply refresh-time on  $b = \{1, 2\}$  to obtain the grid  $\tau^b$ .  
Estimate  $\hat{h}_{21}^b$  as the realized beta between  $f_{\tau_j^b}^{(1)}$  and  $\hat{u}_{\tau_j^b}^{(2)}$ . Set  $\hat{h}_{21} = \hat{h}_{21}^b$ .  
Estimate  $\hat{g}_{22}$  using an IV estimator on  $f_{\tau_j^b}^{(2)} = \hat{u}_{\tau_j^b}^{(2)} - \hat{h}_{21} f_{\tau_j^b}^{(1)}$ .
- Step 3:  
Apply refresh-time on  $c = \{1, 3\}$  to obtain the grid  $\tau^c$ .  
Estimate  $\hat{h}_{31}^c$  as the realized beta between  $f_{\tau_j^c}^{(1)}$  and  $\hat{u}_{\tau_j^c}^{(3)}$ . Set  $\hat{h}_{31} = \hat{h}_{31}^c$ .  
Apply refresh-time on  $d = \{1, 2, 3\}$  to obtain the grid  $\tau^d$ .  
Re-estimate  $\hat{h}_{21}^d$  at the new grid, such that the projections  $f_{\tau_j^d}^{(1)}$  and  $f_{\tau_j^d}^{(2)}$  are orthogonal.  
Estimate  $\hat{h}_{32}^d$  as the realized beta between  $f_{\tau_j^d}^{(2)}$  and  $\hat{u}_{\tau_j^d}^{(3)}$ . Set  $\hat{h}_{32} = \hat{h}_{32}^d$ .  
Estimate  $\hat{g}_{33}$  using an IV estimator on  $f_{\tau_j^d}^{(3)} = \hat{u}_{\tau_j^d}^{(3)} - \hat{h}_{32} f_{\tau_j^d}^{(2)} - \hat{h}_{31} f_{\tau_j^d}^{(1)}$ .
- Step 4 to d:  
Continue in the same fashion by sampling over  $1, \dots, k, l$  to estimate  $h_{lk}$  using the smallest possible set.  
Re-estimate the  $h_{nm}$  with  $m < n \leq k$  at every new grid to obtain orthogonal projections.  
Estimate the  $g_{kk}$  as the IV of projections based on the final estimates,  $\hat{h}$ .

**Value**

a list containing the covariance matrix "CholCov", and the Cholesky decomposition "L" and "G" such that  $L \times G \times L' = \text{CholCov}$ .

**Author(s)**

Emil Sjoerup

**References**

Boudt, K., Laurent, S., Lunde, A., Quaedvlieg, R., and Sauri, O. (2017). Positive semidefinite integrated covariance estimation, factorizations and asynchronicity. *Journal of Econometrics*, 196, 347-367.

**See Also**

[ICov](#) for a list of implemented estimators of the integrated covariance.

---

rCov

*Realized covariance*


---

**Description**

Function returns the Realized Covariation (rCov). Let  $r_{t,i}$  be an intraday  $N \times M$  return vector and  $i = 1, \dots, M$  the number of intraday returns.

Then, the rCov is given by

$$\text{rCov}_t = \sum_{i=1}^M r_{t,i} r'_{t,i}.$$

**Usage**

```
rCov(
  rData,
  cor = FALSE,
  alignBy = NULL,
  alignPeriod = NULL,
  makeReturns = FALSE,
  ...
)
```

**Arguments**

**rData** an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.

**cor** boolean, in case it is TRUE, and the input data is multivariate, the correlation is returned instead of the covariance matrix. FALSE by default.

alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	used internally, do not change.

**Value**

in case the input is and contains data from one day, an  $N \times N$  matrix is returned. If the data is a univariate xts object with multiple days, an xts is returned. If the data is multivariate and contains multiple days (xts or data.table), the function returns a list containing N by N matrices. Each item in the list has a name which corresponds to the date for the matrix.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**See Also**

[ICov](#) for a list of implemented estimators of the integrated covariance.

**Examples**

```
# Realized Variance/Covariance for prices aligned at 5 minutes.

# Univariate:
rv = rCov(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
          alignPeriod = 5, makeReturns = TRUE)
rv

# Multivariate:
rc = rCov(rData = sampleOneMinuteData, makeReturns = TRUE)
rc
```

---

refreshTime

*Synchronize (multiple) irregular timeseries by refresh time*


---

**Description**

This function implements the refresh time synchronization scheme proposed by Harris et al. (1995). It picks the so-called refresh times at which all assets have traded at least once since the last refresh time point. For example, the first refresh time corresponds to the first time at which all stocks have traded. The subsequent refresh time is defined as the first time when all stocks have traded again. This process is repeated until the end of one time series is reached.



**Usage**

```
refreshTime(pData, sort = FALSE, criterion = "squared duration")
```

**Arguments**

pData	a list. Each list-item contains an xts or a data.table object (with first column DT (datetime)) containing the original time series (one day only and typically a price series).
sort	logical determining whether to sort the index based on a criterion (will only sort descending; i.e., most liquid first). Default is FALSE.
criterion	character determining which criterion used. Currently supports "squared duration" and "duration". Default is "squared duration".

**Value**

An xts or data.table object containing the synchronized time series - depending on the input.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

**References**

Harris, F., T. McNish, Shoesmith, G., and Wood, R. (1995). Cointegration, error correction, and price discovery on informationally linked security markets. *Journal of Financial and Quantitative Analysis*, 30, 563-581.

**Examples**

```
# Suppose irregular timepoints:
start <- as.POSIXct("2010-01-01 09:30:00")
ta <- start + c(1,2,4,5,9)
tb <- start + c(1,3,6,7,8,9,10,11)

# Yielding the following timeseries:
a <- xts::as.xts(1:length(ta), order.by = ta)
b <- xts::as.xts(1:length(tb), order.by = tb)

# Calculate the synchronized timeseries:
refreshTime(list(a,b))
```

ReMeDI

*ReMeDI***Description**

This function estimates the auto-covariance of market-microstructure noise

Let the observed price  $Y_t$  be given as  $Y_t = X_t + \varepsilon_t$ , where  $X_t$  is the efficient price and  $\varepsilon_t$  is the market microstructure noise

The estimator of the  $l$ 'th lag of the market microstructure is defined as:

$$\hat{R}_{t,l}^n = \frac{1}{n_t} \sum_{i=2k_n}^{n_t-k_n-l} (Y_{i+l}^n - Y_{i+l+k_n}^n) (Y_i^n - Y_{i-2k_n}^n),$$

where  $k_n$  is a tuning parameter. In the function `knChooseReMeDI`, we provide a function to estimate the optimal  $k_n$  parameter.

**Usage**

```
ReMeDI(pData, kn = 1, lags = 1, makeCorrelation = FALSE)
```

**Arguments**

<code>pData</code>	<code>xts</code> or <code>data.table</code> containing the log-prices of the asset
<code>kn</code>	numeric of length 1 determining the tuning parameter <code>kn</code> this controls the lengths of the non-overlapping interval in the ReMeDI estimation
<code>lags</code>	numeric containing integer values indicating the lags for which to estimate the (co)variance
<code>makeCorrelation</code>	logical indicating whether to transform the autocovariances into autocorrelations. The estimate of variance is imprecise and thus, constructing the correlation like this may show correlations that fall outside $(-1, 1)$ .

**Note**

We Thank Merrick Li for contributing his Matlab code for this estimator.

**Author(s)**

Emil Sjoerup.

**References**

Li, M. and Linton, O. (2021). A ReMeDI for microstructure noise. *Econometrica*, forthcoming

**Examples**

```

remed <- ReMeDI(sampleTData[as.Date(DT) == "2018-01-02", ], kn = 2, lags = 1:8)
# We can also use the algorithm for choosing the kn tuning parameter
optimalKn <- knChooseReMeDI(sampleTData[as.Date(DT) == "2018-01-02", ],
                             knMax = 10, tol = 0.05, size = 3,
                             lower = 2, upper = 5, plot = TRUE)
optimalKn
remed <- ReMeDI(sampleTData[as.Date(DT) == "2018-01-02", ], kn = optimalKn, lags = 1:8)

```

---

ReMeDIAsymptoticVariance

*Asymptotic variance of ReMeDI estimator*


---

**Description**

Estimates the asymptotic variance of the ReMeDI estimator.

**Usage**

```
ReMeDIAsymptoticVariance(pData, kn, lags, phi, i)
```

**Arguments**

pData	xts or data.table containing the log-prices of the asset
kn	numerical value determining the tuning parameter kn this controls the lengths of the non-overlapping interval in the ReMeDI estimation
lags	numeric containing integer values indicating the lags for which to estimate the (co)variance
phi	tuning parameter phi
i	tuning parameter i

**Details**

Some notation is needed for the estimator of the asymptotic covariance of the ReMeDI estimator. Let

$$\delta(n, i) = t_i^n - t_{t-1}^n, i \geq 1,$$

$$\hat{\delta}_t^n = \left( \frac{k_n \delta(n, i + 1 + k_n) - t_{i+2+2k_n}^n + t_{i+2+k_n}^n}{(t_{i+k_n}^n - t_i^n) \vee \phi_n} \right)^2,$$

$$U(1)_t^n = \sum_{i=0}^{n_t - \omega(1)_n} \hat{\delta}_i^n,$$

$$U(2, j)_t^n = \sum_{i=0}^{n_t - \omega(2)_n} \hat{\delta}_i^n \Delta_j(Y)_{i+\omega(2)_n}^n,$$

$$\begin{aligned}
U(3, \mathbf{j}, \mathbf{j}')_t^n &= \sum_{i=0}^{n_t - \omega(3)_n} \hat{\delta}_i^n \Delta_{\mathbf{j}}(Y)_{i+\omega(3)_2}^n \Delta_{\mathbf{j}'}(Y)_{i+\omega(3)_3}^n, \\
U(4; \mathbf{j}, \mathbf{j}')_t^n &= - \sum_{i=2^{q-1}k_n}^{n_t - \omega(4)_n} \Delta_{\mathbf{j}}(Y) \Delta_{\mathbf{j}'}(Y)_{i+\omega(3)_3}^n, \\
U(5, k; \mathbf{j}, \mathbf{j}')_t^n &= \sum_{Q_q \in \mathcal{Q}_q} \sum_{i=2^e(Q_q)k_n}^{n_t - \omega(5)_n} \Delta_{\mathbf{j}_{Q_q \oplus (j'_{Q_q}, (+k))}}(Y)_i^n \prod_{\ell: \ell \in Q_q^c} \Delta_{(j_{\ell}, j'_{\ell} + k)}(Y)_{i+\omega(5)_{\ell+1}}^n, \\
U(6, k; \mathbf{j}, \mathbf{j}') &= \sum_{j_{\ell} \in \mathbf{j}, j'_{\ell'} \in \mathbf{j}'} \sum_{i=2k_n}^{n_t - \omega(6)_n} \Delta_{(j_{\ell}, j'_{\ell'} + k)}(Y)_i^n \Delta_{\mathbf{j}-\ell}(Y)_{i+\omega(6)_2}^n \Delta_{\mathbf{j}'-\ell'}(Y)_{i+\omega(6)_3}^n \\
&\quad - \sum_{j_{\ell} \in \mathbf{j}} \sum_{i=2^q k_n}^{n_t - \omega'(6)_n} \Delta_{\{j_{\ell}\} \oplus \mathbf{j}'(+k)}(Y)_i^n \Delta_{\mathbf{j}-\ell}(Y)_{i+\omega'(6)_2}^n \\
&\quad - \sum_{j'_{\ell'} \in \mathbf{j}'} \sum_{i=2^q k_n}^{n_t - \omega''(6)_n} \Delta_{\{j'_{\ell'}\} \oplus \mathbf{j}}(Y)_i^n \Delta_{\mathbf{j}'-\ell'}(Y)_{i+\omega''(6)_2}^n, \\
U(7, k; \mathbf{j}, \mathbf{j}')_t^n &= \text{ReMeDI}(\mathbf{j} \oplus \mathbf{j}'(+k))_t^n, \\
U(k; \mathbf{j}, \mathbf{j}')_t^n &= \sum_{\ell=5}^7 U(\ell, k; \mathbf{j}, \mathbf{j}')_t^n, \\
U(k; \mathbf{j}, \mathbf{j}')_t^n &= \sum_{\ell=5}^7 U(\ell, k; \mathbf{j}, \mathbf{j}')_t^n,
\end{aligned}$$

Where the indices are given by:

$$\begin{aligned}
\omega(1)_n &= 2 + 2k_n, \quad \omega(2)_2^n = 2 + (3 + 2^{q-1})k_n, \quad \omega(2)_n = \omega(2)_2^n + j_1 + k_n, \\
\omega(3)_2^n &= 2 + (3 + 2^{q-1})k_n, \quad \omega(3)_3^n = 2 + (5 + 2^{q-1} + 2^{q'-1})k_n + j_1, \\
\omega(3)_n &= \omega(3)_3^n + j'_1 + k_n, \quad \omega(4)_2^n = 2k_n + q'_n + j_1, \quad \omega(4)_n = \omega(4)_2^n + j'_1 + k_n, \\
e(Q_q) &= (2|Q_q| + q' - q - 1) \vee 1, \quad \omega(5)_{\ell+1}^n = 4\ell k_n + \sum_{\ell'=1}^{\ell} j_{\ell'} \vee (j'_{\ell} + k) \text{ for } \ell \geq 1, \\
\omega(5)_n &= \omega(5)_{|Q_q^c|+1}^n + j_{|Q_q^c|} \vee (j_{|Q_q^c|} + k) + k_n,
\end{aligned}$$

$$\omega(6)_2^n = (2^{q-2} + 2)k_n + j_{\ell} \vee (j'_{\ell'} + k), \quad \omega(6)_3^n = (2^{q-2} + 2^{q'-2} + 2)k_n + j_1 + j_{\ell} \vee (j'_{\ell} + k),$$

$$\omega'(6)_2^n = (2^{q-2} + 2)k_n + j_{\ell} \vee (j'_1 + k), \quad \omega''(6)_2^n = (2^{q'-2} + 1)k_n + (j'_{\ell'} + k) \vee j_1,$$

$$\omega(6)_n = \omega(6)_3^n + j' + k_n, \quad \omega'(6)_n = \omega'(6)_2^n + j_1 + k_n, \quad \omega''(6)_n = \omega''(6)_2^n j'_1 + k_n,$$

The asymptotic variance estimator is then given by

$$\hat{\sigma}(\mathbf{j}, \mathbf{j}')_t^n = \frac{1}{n_t} \sum_{\ell=1}^3 \hat{\sigma}_\ell(\mathbf{j}, \mathbf{j}')_t^n,$$

where

$$\hat{\sigma}_1(\mathbf{j}, \mathbf{j}')_t^n = U(0; \mathbf{j}, \mathbf{j}') + \sum_{k=1}^{i_n} (U(k; \mathbf{j}, \mathbf{j}')_t^n) + (2i_n + 1) U(4; \mathbf{j}, \mathbf{j}')_t^n,$$

$$\hat{\sigma}_2(\mathbf{j}, \mathbf{j}')_t^n = U(3; \mathbf{j}, \mathbf{j}'),$$

$$\hat{\sigma}_3(\mathbf{j}, \mathbf{j}')_t^n = \frac{1}{n_t^2} \text{ReMeDI}(Y, \mathbf{j})_t^n \text{ReMeDI}(Y, \mathbf{j}')_t^n U(1)_t^n,$$

$$- \frac{1}{n_t} (\text{ReMeDI}(Y, \mathbf{j})_t^n U(2, \mathbf{j}')_t^n + \text{ReMeDI}(Y, \mathbf{j}')_t^n U(2, \mathbf{j})_t^n),$$

### Value

a list with components ReMeDI and asympVar containing the ReMeDI estimation and it's asymptotic variance respectively

### Note

We Thank Merrick Li for contributing his Matlab code for this estimator.

### Examples

```
kn <- knChooseReMeDI(sampleTDataEurope[, list(DT, PRICE)])
remedi <- ReMeDI(sampleTDataEurope[, list(DT, PRICE)], kn = kn, lags = 0:15)
asympVar <- ReMeDIAsymptoticVariance(sampleTDataEurope[, list(DT, PRICE)],
kn = kn, lags = 0:15, phi = 0.9, i = 2)
```

---

rHYCov

*Hayashi-Yoshida covariance*

---

### Description

Calculates the Hayashi-Yoshida Covariance estimator

**Usage**

```
rHYCov(
  rData,
  cor = FALSE,
  period = 1,
  alignBy = "seconds",
  alignPeriod = 1,
  makeReturns = FALSE,
  makePsd = TRUE,
  ...
)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
cor	boolean, in case it is TRUE, and the input data is multivariate, the correlation is returned instead of the covariance matrix. FALSE by default.
period	Sampling period
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
makePsd	boolean, in case it is TRUE, the positive definite version of rHYCov is returned. FALSE by default.
...	used internally. Do not set.

**Author(s)**

Scott Payseur and Emil Sjoerup.

**References**

Hayashi, T. and Yoshida, N. (2005). On covariance estimation of non-synchronously observed diffusion processes. *Bernoulli*, 11, 359-379.

**See Also**

[ICov](#) for a list of implemented estimators of the integrated covariance.

**Examples**

```
library("xts")
hy <- rHYCov(rData = as.xts(sampleOneMinuteData)["2001-08-05"],
            period = 5, alignBy = "minutes", alignPeriod = 5, makeReturns = TRUE)
```

---

rKernelCov	<i>Realized kernel estimator</i>
------------	----------------------------------

---

### Description

Realized covariance calculation using a kernel estimator. The different types of kernels available can be found using [listAvailableKernels](#).

### Usage

```
rKernelCov(
  rData,
  cor = FALSE,
  alignBy = NULL,
  alignPeriod = NULL,
  makeReturns = FALSE,
  kernelType = "rectangular",
  kernelParam = 1,
  kernelDOFadj = TRUE,
  ...
)
```

### Arguments

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days
cor	boolean, in case it is TRUE, and the input data is multivariate, the correlation is returned instead of the covariance matrix. FALSE by default.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod to 5 and alignBy to "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
kernelType	Kernel name.
kernelParam	Kernel parameter.
kernelDOFadj	Kernel degree of freedom adjustment.
...	used internally, do not change.

### Details

Let  $r_{t,i}$  be  $N$  returns in period  $t$ ,  $i = 1, \dots, N$ . The returns or prices do not have to be equidistant. The kernel estimator for  $H = \text{kernelParam}$  is given by

$$\gamma_0 + 2 \sum_{h=1}^H k\left(\frac{h-1}{H}\right) \gamma_h,$$

where  $k(x)$  is the chosen kernel function and

$$\gamma_h = \sum_{i=h}^N r_{t,i} \times r_{t,i-h}$$

is the empirical autocovariance function. The multivariate version employs the cross-covariances instead.

### Value

in case the input is and contains data from one day, an  $N$  by  $N$  matrix is returned. If the data is a univariate xts object with multiple days, an xts is returned. If the data is multivariate and contains multiple days (xts or data.table), the function returns a list containing  $N$  by  $N$  matrices. Each item in the list has a name which corresponds to the date for the matrix.

### Author(s)

Scott Payseur, Onno Kleen, and Emil Sjoerup.

### References

Barndorff-Nielsen, O. E., Hansen, P. R., Lunde, A., and Shephard, N. (2008). Designing realized kernels to measure the ex post variation of equity prices in the presence of noise. *Econometrica*, 76, 1481-1536.

Hansen, P. and Lunde, A. (2006). Realized variance and market microstructure noise. *Journal of Business and Economic Statistics*, 24, 127-218.

Zhou., B. (1996). High-frequency data and volatility in foreign-exchange rates. *Journal of Business & Economic Statistics*, 14, 45-52.

### See Also

[ICov](#) for a list of implemented estimators of the integrated covariance.

### Examples

```
# Univariate:
rvKernel <- rKernelCov(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
                      alignPeriod = 5, makeReturns = TRUE)
rvKernel

# Multivariate:
rcKernel <- rKernelCov(rData = sampleOneMinuteData, makeReturns = TRUE)
rcKernel
```



---

rKurt	<i>Realized kurtosis of highfrequency return series.</i>
-------	--

---

### Description

Calculate the realized kurtosis as defined in Amaya et al. (2015).

Assume there are  $N$  equispaced returns in period  $t$ . Let  $r_{t,i}$  be a return (with  $i = 1, \dots, N$ ) in period  $t$ . Then, rKurt is given by

$$\text{rKurt}_t = \frac{N \sum_{i=1}^N (r_{t,i})^4}{\left(\sum_{i=1}^N r_{t,i}^2\right)^2}.$$

### Usage

```
rKurt(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

### Arguments

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.

### Value

- In case the input is an xts object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in xts format, an xts will be returned.
- If the input data is a data.table object, the function returns a data.table with the same column names as the input data, containing the date and the realized measures.

### Author(s)

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

### References

Amaya, D., Christoffersen, P., Jacobs, K., and Vasquez, A. (2015). Does realized skewness and kurtosis predict the cross-section of equity returns? *Journal of Financial Economics*, 118, 135-167.

**Examples**

```
rk <- rKurt(sampleTData[, list(DT, PRICE)], alignBy = "minutes",
            alignPeriod = 5, makeReturns = TRUE)
rk
```

---

rMedRQ

*DEPRECATED*


---

**Description**

DEPRECATED USE [rMedRQuar](#)

**Usage**

```
rMedRQ(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

**Arguments**

rData	DEPRECATED USE <a href="#">rMedRQuar</a>
alignBy	DEPRECATED USE <a href="#">rMedRQuar</a>
alignPeriod	DEPRECATED USE <a href="#">rMedRQuar</a>
makeReturns	DEPRECATED USE <a href="#">rMedRQuar</a>

---

rMedRQuar

*An estimator of integrated quarticity from applying the median operator on blocks of three returns*


---

**Description**

Calculate the rMedRQ, defined in Andersen et al. (2012). Assume there are  $N$  equispaced returns  $r_{t,i}$  in period  $t$ ,  $i = 1, \dots, N$ . Then, the rMedRQ is given by

$$\text{rMedRQ}_t = \frac{3\pi N}{9\pi + 72 - 52\sqrt{3}} \left( \frac{N}{N-2} \right) \sum_{i=2}^{N-1} \text{med}(|r_{t,i-1}|, |r_{t,i}|, |r_{t,i+1}|)^4.$$

**Usage**

```
rMedRQuar(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod to 5 and alignBy to "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.

**Value**

- In case the input is an xts object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in xts format, an xts will be returned.
- If the input data is a data.table object, the function returns a data.table with the same column names as the input data, containing the date and the realized measures.

**Author(s)**

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75-93.

**Examples**

```
rq <- rMedRQuar(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
               alignPeriod = 5, makeReturns = TRUE)
rq
```

---

rMedRV

*DEPRECATED*


---

**Description**

DEPRECATED USE [rMedRVar](#)

**Usage**

```
rMedRV(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

**Arguments**

rData	DEPRECATED USE <a href="#">rMedRVar</a>
alignBy	DEPRECATED USE <a href="#">rMedRVar</a>
alignPeriod	DEPRECATED USE <a href="#">rMedRVar</a>
makeReturns	DEPRECATED USE <a href="#">rMedRVar</a>

---

rMedRVar	<i>rMedRVar</i>
----------	-----------------

---

**Description**

Calculate the rMedRVar, defined in Andersen et al. (2012). Let  $r_{t,i}$  be a return (with  $i = 1, \dots, M$ ) in period  $t$ . Then, the rMedRVar is given by

$$\text{rMedRVar}_t = \frac{\pi}{6 - 4\sqrt{3} + \pi} \left( \frac{M}{M-2} \right) \sum_{i=2}^{M-1} \text{med}(|r_{t,i-1}|, |r_{t,i}|, |r_{t,i+1}|)^2$$

**Usage**

```
rMedRVar(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE, ...)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	used internally, do not change.

**Details**

The rMedRVar belongs to the class of realized volatility measures in this package that use the series of high-frequency returns  $r_{t,i}$  of a day  $t$  to produce an ex post estimate of the realized volatility of that day  $t$ . rMedRVar is designed to be robust to price jumps. The difference between RV and rMedRVar is an estimate of the realized jump variability. Disentangling the continuous and jump components in RV can lead to more precise volatility forecasts, as shown in Andersen et al. (2012)

**Value**

- In case the input is an `xts` object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in `xts` format, an `xts` will be returned.
- If the input data is a `data.table` object, the function returns a `data.table` with the same column names as the input data, containing the date and the realized measures.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75-93.

**See Also**

[IVar](#) for a list of implemented estimators of the integrated variance.

**Examples**

```
medrv <- rMedRVar(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
                alignPeriod = 5, makeReturns = TRUE)
medrv
```

---

rMinRQ

*DEPRECATED*

---

**Description**

DEPRECATED USE [rMinRQuar](#)

**Usage**

```
rMinRQ(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

**Arguments**

<code>rData</code>	DEPRECATED USE <a href="#">rMinRQuar</a>
<code>alignBy</code>	DEPRECATED USE <a href="#">rMinRQuar</a>
<code>alignPeriod</code>	DEPRECATED USE <a href="#">rMinRQuar</a>
<code>makeReturns</code>	DEPRECATED USE <a href="#">rMinRQuar</a>

---

rMinRQuar	<i>An estimator of integrated quarticity from applying the minimum operator on blocks of two returns</i>
-----------	--

---

### Description

Calculate the rMinRQuar, defined in Andersen et al. (2012). Assume there are  $N$  equispaced returns  $r_{t,i}$  in period  $t, i = 1, \dots, N$ . Then, the rMinRQuar is given by

$$\text{rMinRQuar}_t = \frac{\pi N}{3\pi - 8} \left( \frac{N}{N-1} \right) \sum_{i=1}^{N-1} \min(|r_{t,i}|, |r_{t,i+1}|)^4$$

### Usage

```
rMinRQuar(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

### Arguments

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.

### Value

- In case the input is an xts object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in xts format, an xts will be returned.
- If the input data is a data.table object, the function returns a data.table with the same column names as the input data, containing the date and the realized measures.

### Author(s)

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup

### References

Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75-93.

**Examples**

```
rq <- rMinRQuar(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
               alignPeriod = 5, makeReturns = TRUE)
rq
```

---

rMinRV	<i>DEPRECATED</i>
--------	-------------------

---

**Description**

DEPRECATED USE [rMinRVar](#)

**Usage**

```
rMinRV(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

**Arguments**

rData	DEPRECATED USE <a href="#">rMinRVar</a>
alignBy	DEPRECATED USE <a href="#">rMinRVar</a>
alignPeriod	DEPRECATED USE <a href="#">rMinRVar</a>
makeReturns	DEPRECATED USE <a href="#">rMinRVar</a>

---

rMinRVar	<i>rMinRVar</i>
----------	-----------------

---

**Description**

Calculate the rMinRVar, defined in Andersen et al. (2009). Let  $r_{t,i}$  be a return (with  $i = 1, \dots, M$ ) in period  $t$ . Then, the rMinRVar is given by

$$\text{rMinRVar}_t = \frac{\pi}{\pi - 2} \left( \frac{M}{M - 1} \right) \sum_{i=1}^{M-1} \min(|r_{t,i}|, |r_{t,i+1}|)^2$$

**Usage**

```
rMinRVar(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE, ...)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	used internally, do not change.

**Value**

- In case the input is an xts object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in xts format, an xts will be returned.
- If the input data is a data.table object, the function returns a data.table with the same column names as the input data, containing the date and the realized measures.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Emil Sjoerup.

**References**

Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75-93.

**See Also**

[IVar](#) for a list of implemented estimators of the integrated variance.

**Examples**

```
minrv <- rMinRVar(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
                 alignPeriod = 5, makeReturns = TRUE)
minrv
```



---

rmLargeSpread	<i>Delete entries for which the spread is more than maxi times the median spread</i>
---------------	--

---

**Description**

Function deletes entries for which the spread is more than "maxi" times the median spread on that day.

**Usage**

```
rmLargeSpread(qData, maxi = 50, tz = NULL)
```

**Arguments**

qData	an xts or data.table object at least containing the columns "BID" and "OFR".
maxi	an integer. By default maxi = "50", which means that entries are deleted if the spread is more than 50 times the median spread on that day.
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. With the non-disk functionality, we attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC". In the on-disk functionality, if tz is not specified, the timezone used will be the system default.

**Value**

xts or data.table object depending on input.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

---

rmNegativeSpread	<i>Delete entries for which the spread is negative</i>
------------------	--

---

**Description**

Function deletes entries for which the spread is negative.

**Usage**

```
rmNegativeSpread(qData)
```

**Arguments**

qData            an xts object at least containing the columns "BID" and "OFR".

**Value**

data.table or xts object

**Author(s)**

Jonathan Cornelissen, Kris Boudt and Onno Kleen

**Examples**

```
rmNegativeSpread(sampleQDataRaw)
```

---

rmOutliersQuotes	<i>Remove outliers in quotes</i>
------------------	----------------------------------

---

**Description**

Delete entries for which the mid-quote is outlying with respect to surrounding entries.

**Usage**

```
rmOutliersQuotes(qData, maxi = 10, window = 50, type = "standard", tz = NULL)
```

**Arguments**

qData            a data.table or xts object at least containing the columns "BID" and "OFR".

maxi            an integer, indicating the maximum number of median absolute deviations allowed.

window         an integer, indicating the time window for which the "outlyingness" is considered.

type            should be "standard" or "advanced" (see details).

tz              fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. With the non-disk functionality, we attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC".

## Details

- If type = "standard": Function deletes entries for which the mid-quote deviated by more than "maxi" median absolute deviations from a rolling centered median (excluding the observation under consideration) of window observations.
- If type = "advanced": Function deletes entries for which the mid-quote deviates by more than "maxi" median absolute deviations from the value closest to the mid-quote of these three options:
  1. Rolling centered median (excluding the observation under consideration)
  2. Rolling median of the following window of observations
  3. Rolling median of the previous window of observations

The advantage of this procedure compared to the "standard" proposed by Barndorff-Nielsen et al. (2010) is that it will not incorrectly remove large price jumps. Therefore this procedure has been set as the default for removing outliers.

Note that the median absolute deviation is taken over the entire day. In case it is zero (which can happen if mid-quotes don't change much), the median absolute deviation is taken over a subsample without constant mid-quotes.

## Value

xts object or data.table depending on type of input.

## Author(s)

Jonathan Cornelissen and Kris Boudt.

## References

Barndorff-Nielsen, O. E., P. R. Hansen, A. Lunde, and N. Shephard (2009). Realized kernels in practice: Trades and quotes. *Econometrics Journal*, 12, C1-C32.

Brownlees, C.T., and Gallo, G.M. (2006). Financial econometric analysis at ultra-high frequency: Data handling concerns. *Computational Statistics & Data Analysis*, 51, 2232-2245.

---

rMPV

*DEPRECATED*

---

## Description

DEPRECATED USE [rMPVar](#)

## Usage

```
rMPV(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

**Arguments**

rData	DEPRECATED
alignBy	DEPRECATED
alignPeriod	DEPRECATED
makeReturns	DEPRECATED

---

rMPVar	<i>Realized multipower variation</i>
--------	--------------------------------------

---

**Description**

Calculate the Realized Multipower Variation rMPVar, defined in Andersen et al. (2012).

Assume there are  $N$  equispaced returns  $r_{t,i}$  in period  $t$ ,  $i = 1, \dots, N$ . Then, the rMPVar is given by

$$\text{rMPVar}_N(m, p) = d_{m,p} \frac{N^{p/2}}{N - m + 1} \sum_{i=1}^{N-m+1} |r_{t,i}|^{p/m} \dots |r_{t,i+m-1}|^{p/m}$$

in which

$$d_{m,p} = \mu_{p/m}^{-m};$$

$m$ : the window size of return blocks;

$p$ : the power of the variation;

and  $m > p/2$ .

**Usage**

```
rMPVar(
  rData,
  m = 2,
  p = 2,
  alignBy = NULL,
  alignPeriod = NULL,
  makeReturns = FALSE,
  ...
)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
m	the window size of return blocks. 2 by default.
p	the power of the variation. 2 by default.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"

alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	used internally, do not change.

**Value**

numeric

**Author(s)**

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75-93.

**See Also**

[IVar](#) for a list of implemented estimators of the integrated variance.

**Examples**

```
mpv <- rMPVar(sampleTData[, list(DT, PRICE)], m = 2, p = 3, alignBy = "minutes",
             alignPeriod = 5, makeReturns = TRUE)
mpv
```

---

rMRC

---

DEPRECATED rMRC

---

**Description**

DEPRECATED USE [rMRCov](#)

**Usage**

```
rMRC(pData, pairwise = FALSE, makePsd = FALSE, theta = 0.8, ...)
```

**Arguments**

pData	DEPRECATED USE <a href="#">rMRCov</a>
pairwise	DEPRECATED USE <a href="#">rMRCov</a>
makePsd	DEPRECATED USE <a href="#">rMRCov</a>
theta	DEPRECATED USE <a href="#">rMRCov</a>
...	DEPRECATED USE <a href="#">rMRCov</a>

---

rMRCov	<i>Modulated realized covariance</i>
--------	--------------------------------------

---

### Description

Calculate univariate or multivariate pre-averaged estimator, as defined in Hautsch and Podolskij (2013).

### Usage

```
rMRCov(
  pData,
  pairwise = FALSE,
  makePsd = FALSE,
  theta = 0.8,
  crossAssetNoiseCorrection = FALSE,
  ...
)
```

### Arguments

pData	a list. Each list-item contains an xts or data.table object with the intraday price data of a stock.
pairwise	boolean, should be TRUE when refresh times are based on pairs of assets. FALSE by default.
makePsd	boolean, in case it is TRUE, the positive definite version of rMRCov is returned. FALSE by default.
theta	a numeric controlling the preaveraging horizon. Defaults to 0.8 as recommended by Hautsch and Podolskij (2013)
crossAssetNoiseCorrection	a logical denoting whether to apply the bias correction term on the off-diagonals (covariance) terms. We set this to FALSE by default as noise is typically seen as independent across assets.
...	used internally, do not change.

### Details

In practice, market microstructure noise leads to a departure from the pure semimartingale model. We consider the process  $Y$  in period  $\tau$ :

$$Y_\tau = X_\tau + \epsilon_\tau,$$

where the observed  $d$  dimensional log-prices are the sum of underlying Brownian semimartingale process  $X$  and a noise term  $\epsilon_\tau$ .

$\epsilon_\tau$  is an *i.i.d.* process with  $X$ .

It is intuitive that under mean zero *i.i.d.* microstructure noise some form of smoothing of the observed log-price should tend to diminish the impact of the noise. Effectively, we are going to approximate a continuous function by an average of observations of  $Y$  in a neighborhood, the noise being averaged away.

Assume there is  $N$  equispaced returns in period  $\tau$  of a list (after refreshing data). Let  $r_{\tau_i}$  be a return (with  $i = 1, \dots, N$ ) of an asset in period  $\tau$ . Assume there is  $d$  assets.

In order to define the univariate pre-averaging estimator, we first define the pre-averaged returns as

$$\bar{r}_{\tau_j}^{(k)} = \sum_{h=1}^{k_N-1} g\left(\frac{h}{k_N}\right) r_{\tau_{j+h}}^{(k)}$$

where  $g$  is a non-zero real-valued function  $g : [0, 1] \rightarrow R$  given by  $g(x) = \min(x, 1 - x)$ .  $k_N$  is a sequence of integers satisfying  $k_N = \lfloor \theta N^{1/2} \rfloor$ . We use  $\theta = 0.8$  as recommended in Hautsch and Podolskij (2013). The pre-averaged returns are simply a weighted average over the returns in a local window. This averaging diminishes the influence of the noise. The order of the window size  $k_n$  is chosen to lead to optimal convergence rates. The pre-averaging estimator is then simply the analogue of the realized variance but based on pre-averaged returns and an additional term to remove bias due to noise

$$\hat{C} = \frac{N^{-1/2}}{\theta\psi_2} \sum_{i=0}^{N-k_N+1} (\bar{r}_{\tau_i})^2 - \frac{\psi_1^{k_N} N^{-1}}{2\theta^2\psi_2^{k_N}} \sum_{i=0}^N r_{\tau_i}^2$$

with

$$\begin{aligned} \psi_1^{k_N} &= k_N \sum_{j=1}^{k_N} \left( g\left(\frac{j+1}{k_N}\right) - g\left(\frac{j}{k_N}\right) \right)^2, \\ \psi_2^{k_N} &= \frac{1}{k_N} \sum_{j=1}^{k_N-1} g^2\left(\frac{j}{k_N}\right), \\ \psi_2 &= \frac{1}{12} \end{aligned}$$

The multivariate counterpart is very similar. The estimator is called the Modulated Realized Covariance (rMRCov) and is defined as

$$\text{MRC} = \frac{N}{N - k_N + 2} \frac{1}{\psi_2 k_N} \sum_{i=0}^{N-k_N+1} \bar{\mathbf{r}}_{\tau_i} \cdot \bar{\mathbf{r}}_{\tau_i}' - \frac{\psi_1^{k_N}}{\theta^2 \psi_2^{k_N}} \hat{\Psi}$$

where  $\hat{\Psi}_N = \frac{1}{2N} \sum_{i=1}^N \mathbf{r}_{\tau_i} (\mathbf{r}_{\tau_i})'$ . It is a bias correction to make it consistent. However, due to this correction, the estimator is not ensured PSD. An alternative is to slightly enlarge the bandwidth such that  $k_N = \lfloor \theta N^{1/2+\delta} \rfloor$ .  $\delta = 0.1$  results in a consistent estimate without the bias correction and a PSD estimate, in which case:

$$\text{MRC}^\delta = \frac{N}{N - k_N + 2} \frac{1}{\psi_2 k_N} \sum_{i=0}^{N-k_N+1} \bar{\mathbf{r}}_i \cdot \bar{\mathbf{r}}_i'$$

## Value

A  $d \times d$  covariance matrix.

**Author(s)**

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

Hautsch, N., and Podolskij, M. (2013). Preaveraging-based estimation of quadratic variation in the presence of noise and jumps: theory, implementation, and empirical Evidence. *Journal of Business & Economic Statistics*, 31, 165-183.

**See Also**

[ICov](#) for a list of implemented estimators of the integrated covariance.

**Examples**

```
## Not run:
library("xts")
# Note that this ought to be tick-by-tick data and this example is only to show the usage.
a <- list(as.xts(sampleOneMinuteData[as.Date(DT) == "2001-08-04", list(DT, MARKET)]),
          as.xts(sampleOneMinuteData[as.Date(DT) == "2001-08-04", list(DT, STOCK)]))
rMRCov(a, pairwise = TRUE, makePsd = TRUE)

# We can also add use data.tables and use a named list to convey asset names
a <- list(foo = sampleOneMinuteData[as.Date(DT) == "2001-08-04", list(DT, MARKET)],
          bar = sampleOneMinuteData[as.Date(DT) == "2001-08-04", list(DT, STOCK)])
rMRCov(a, pairwise = TRUE, makePsd = TRUE)

## End(Not run)
```

---

```
rmTradeOutliersUsingQuotes
```

*Delete transactions with unlikely transaction prices*

---

**Description**

Function deletes entries with prices that are above the ask plus the bid-ask spread. Similar for entries with prices below the bid minus the bid-ask spread.

**Usage**

```
rmTradeOutliersUsingQuotes(
  tData,
  qData,
  lagQuotes = 0,
  nSpreads = 1,
  BFM = FALSE,
```



```

    backwardsWindow = 3600,
    forwardsWindow = 0.5,
    plot = FALSE,
    ...
)

```

### Arguments

tData	a data.table or xts object containing the time series data, with at least the column "PRICE", containing the transaction price.
qData	a data.table or xts object containing the time series data with at least the columns "BID" and "OFR", containing the bid and ask prices.
lagQuotes	numeric, number of seconds the quotes are registered faster than the trades (should be round and positive). Default is 0. For older datasets, i.e. before 2010, it may be a good idea to set this to e.g. 2. See Vergote (2005)
nSpreads	numeric of length 1 denotes how far above the offer and below bid we allow outliers to be. Trades are filtered out if they are MORE THAN nSpread * spread above (below) the offer (bid)
BFM	a logical determining whether to conduct 'Backwards - Forwards matching' of trades and quotes. The algorithm tries to match trades that fall outside the bid - ask and first tries to match a small window forwards and if this fails, it tries to match backwards in a bigger window. The small window is a tolerance for inaccuracies in the timestamps of bids and asks. The backwards window allow for matching of late reported trades, i.e. block trades.
backwardsWindow	a numeric denoting the length of the backwards window. Default is 3600, corresponding to one hour.
forwardsWindow	a numeric denoting the length of the forwards window. Default is 0.5, corresponding to one half second.
plot	a logical denoting whether to visualize the forwards, backwards, and unmatched trades in a plot.
...	used internally

### Details

Note: in order to work correctly, the input data of this function should be cleaned trade (tData) and quote (qData) data respectively. In older high frequency datasets the trades frequently lag the quotes. In newer datasets this tends to happen only during extreme market activity when exchange networks are at maximum capacity.

### Value

xts or data.table object depending on input.

### Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

## References

- Vergote, O. (2005). How to match trades and quotes for NYSE stocks? K.U.Leuven working paper.
- Christensen, K., Oomen, R. C. A., Podolskij, M. (2014): Fact or Friction: Jumps at ultra high frequency. *Journal of Financial Economics*, 144, 576-599

---

rOWCov	<i>Realized outlyingness weighted covariance</i>
--------	--

---

## Description

Calculate the Realized Outlyingness Weighted Covariance (rOWCov), defined in Boudt et al. (2008).

Let  $r_{t,i}$ , for  $i = 1, \dots, M$  be a sample of  $M$  high-frequency ( $N \times 1$ ) return vectors and  $d_{t,i}$  their outlyingness given by the squared Mahalanobis distance between the return vector and zero in terms of the reweighted MCD covariance estimate based on these returns.

Then, the rOWCov is given by

$$\text{rOWCov}_t = c_w \frac{\sum_{i=1}^M w(d_{t,i}) r_{t,i} r'_{t,i}}{\frac{1}{M} \sum_{i=1}^M w(d_{t,i})},$$

The weight  $w_{i,\Delta}$  is one if the multivariate jump test statistic for  $r_{i,\Delta}$  in Boudt et al. (2008) is less than the 99.9% percentile of the chi-square distribution with  $N$  degrees of freedom and zero otherwise. The scalar  $c_w$  is a correction factor ensuring consistency of the rOWCov for the Integrated Covariance, under the Brownian Semimartingale with Finite Activity Jumps model.

## Usage

```
rOWCov(
  rData,
  cor = FALSE,
  alignBy = NULL,
  alignPeriod = NULL,
  makeReturns = FALSE,
  seasadjR = NULL,
  wFunction = "HR",
  alphaMCD = 0.75,
  alpha = 0.001,
  ...
)
```

## Arguments

- |       |  |
|-------|--|
| rData | a ( $M \times N$ ) xts object containing the $N$ return series over period $t$ , with $M$ observations during $t$ .                              |
| cor   | boolean, in case it is TRUE, and the input data is multivariate, the correlation is returned instead of the covariance matrix. FALSE by default. |

alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
seasadjR	a ( $M \times N$ ) xts object containing the seasonally adjusted returns. This is an optional argument.
wFunction	determines whether a zero-one weight function (one if no jump is detected based on $d_{t,i}$ and 0 otherwise) or Soft Rejection ("SR") weight function is to be used. By default a zero-one weight function (wFunction = "HR") is used.
alphaMCD	a numeric parameter, controlling the size of the subsets over which the determinant is minimized. Allowed values are between 0.5 and 1 and the default is 0.75. See Boudt et al. (2008) or the covMcd function in the <a href="#">robustbase</a> package.
alpha	is a parameter between 0 and 0.5, that determines the rejection threshold value (see Boudt et al. (2008) for details).
...	used internally, do not change.

### Details

Advantages of the rOWCov compared to the [rBPCov](#) include a higher statistical efficiency, positive semi-definiteness and affine equi-variance. However, the rOWCov suffers from a curse of dimensionality. The rOWCov gives a zero weight to a return vector if at least one of the components is affected by a jump. In the case of independent jump occurrences, the average proportion of observations with at least one component being affected by jumps increases fast with the dimension of the series. This means that a potentially large proportion of the returns receives a zero weight, due to which the rOWCov can have a low finite sample efficiency in higher dimensions.

### Value

an  $N \times N$  matrix

### Author(s)

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

### References

Boudt, K., Croux, C., and Laurent, S. (2008). Outlyingness weighted covariation. *Journal of Financial Econometrics*, 9, 657–684.

### See Also

[ICov](#) for a list of implemented estimators of the integrated covariance.

**Examples**

```
## Not run:
library("xts")
# Realized Outlyingness Weighted Variance/Covariance for prices aligned
# at 1 minutes.

# Univariate:
row <- rOWCov(rData = as.xts(sampleOneMinuteData[as.Date(DT) == "2001-08-04",
list(DT, MARKET)]), makeReturns = TRUE)
row

# Multivariate:
rowc <- rOWCov(rData = as.xts(sampleOneMinuteData[as.Date(DT) == "2001-08-04",]),
makeReturns = TRUE)
rowc

## End(Not run)
```

rQPVar

*Realized quad-power variation of intraday returns***Description**

Calculate the realized quad-power variation, defined in Andersen et al. (2012).

Assume there are  $N$  equispaced returns  $r_{t,i}$  in period  $t$ ,  $i = 1, \dots, N$ . Then, the rQPVar is given by

$$\text{rQPVar}_t = N * \frac{N}{N-3} \left( \frac{\pi^2}{4} \right)^{-4} (|r_{t,i}| |r_{t,i-1}| |r_{t,i-2}| |r_{t,i-3}|)$$

**Usage**

```
rQPVar(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE, ...)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	used internally, do not change.

**Value**

- In case the input is an `xts` object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in `xts` format, an `xts` will be returned.
- If the input data is a `data.table` object, the function returns a `data.table` with the same column names as the input data, containing the date and the realized measures.

**Author(s)**

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup

**References**

Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75-93.

**See Also**

[IVar](#) for a list of implemented estimators of the integrated variance.

**Examples**

```
qpV <- rQPVar(rData= sampleTData[, list(DT, PRICE)], alignBy= "minutes",
             alignPeriod =5, makeReturns= TRUE)
qpV
```

---

rQuar	<i>Realized quarticity</i>
-------	----------------------------

---

**Description**

Calculate the realized quarticity (`rQuar`), defined in Andersen et al. (2012).

Assume there are  $N$  equispaced returns  $r_{t,i}$  in period  $t$ ,  $i = 1, \dots, N$ .

Then, the `rQuar` is given by

$$\text{rQuar}_t = \frac{N}{3} \sum_{i=1}^N (r_{t,i}^4)$$

**Usage**

```
rQuar(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.

**Value**

- In case the input is an xts object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in xts format, an xts will be returned.
- If the input data is a data.table object, the function returns a data.table with the same column names as the input data, containing the date and the realized measures.

**Author(s)**

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75-93.

**Examples**

```
rq <- rQuar(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
           alignPeriod = 5, makeReturns = TRUE)
rq
```

---

rRTSCov

*Robust two time scale covariance estimation*


---

**Description**

Calculate the robust two time scale covariance matrix proposed in Boudt and Zhang (2010). Unlike the rOWCov, but similarly to the rThresholdCov, the rRTSCov uses univariate jump detection rules to truncate the effect of jumps on the covariance estimate. By the use of two time scales, this covariance estimate is not only robust to price jumps, but also to microstructure noise and non-synchronous trading.

**Usage**

```

rRTSCov(
  pData,
  cor = FALSE,
  startIV = NULL,
  noisevar = NULL,
  K = 300,
  J = 1,
  KCov = NULL,
  JCov = NULL,
  KVar = NULL,
  JVar = NULL,
  eta = 9,
  makePsd = FALSE,
  ...
)

```

**Arguments**

<code>pData</code>	a list. Each list-item $i$ contains an <code>xts</code> object with the intraday price data of stock $i$ for day $t$ .
<code>cor</code>	boolean, in case it is TRUE, and the input data is multivariate, the correlation is returned instead of the covariance matrix. FALSE by default.
<code>startIV</code>	vector containing the first step estimates of the integrated variance of the assets, needed in the truncation. Is NULL by default.
<code>noisevar</code>	vector containing the estimates of the noise variance of the assets, needed in the truncation. Is NULL by default.
<code>K</code>	positive integer, slow time scale returns are computed on prices that are $K$ steps apart.
<code>J</code>	positive integer, fast time scale returns are computed on prices that are $J$ steps apart.
<code>KCov</code>	positive integer, for the extradiagonal covariance elements the slow time scale returns are computed on prices that are $K$ steps apart.
<code>JCov</code>	positive integer, for the extradiagonal covariance elements the fast time scale returns are computed on prices that are $J$ steps apart.
<code>KVar</code>	vector of positive integers, for the diagonal variance elements the slow time scale returns are computed on prices that are $K$ steps apart.
<code>JVar</code>	vector of positive integers, for the diagonal variance elements the fast time scale returns are computed on prices that are $J$ steps apart.
<code>eta</code>	positive real number, squared standardized high-frequency returns that exceed $\eta$ are detected as jumps.
<code>makePsd</code>	boolean, in case it is TRUE, the positive definite version of <code>rRTSCov</code> is returned. FALSE by default.
<code>...</code>	used internally, do not change.

### Details

The rRTSCov requires the tick-by-tick transaction prices. (Co)variances are then computed using log-returns calculated on a rolling basis on stock prices that are  $K$  (slow time scale) and  $J$  (fast time scale) steps apart.

The diagonal elements of the rRTSCov matrix are the variances, computed for log-price series  $X$  with  $n$  price observations at times  $\tau_1, \tau_2, \dots, \tau_n$  as follows:

$$\left(1 - \frac{\bar{n}_K}{\bar{n}_J}\right)^{-1} (\{X, X\}_T^{(K)*} - \frac{\bar{n}_K}{\bar{n}_J} \{X, X\}_T^{(J)*}),$$

where  $\bar{n}_K = (n - K + 1)/K$ ,  $\bar{n}_J = (n - J + 1)/J$  and

$$\{X, X\}_T^{(K)*} = \frac{c_\eta^* \sum_{i=1}^{n-K+1} (X_{t_{i+K}} - X_{t_i})^2 I_X^K(i; \eta)}{K \frac{1}{n-K+1} \sum_{i=1}^{n-K+1} I_X^K(i; \eta)}.$$

The constant  $c_\eta$  adjusts for the bias due to the thresholding and  $I_X^K(i; \eta)$  is a jump indicator function that is one if

$$\frac{(X_{t_{i+K}} - X_{t_i})^2}{\left(\int_{t_i}^{t_{i+K}} \sigma_s^2 ds + 2\sigma_{\varepsilon_X}^2\right)} \leq \eta$$

and zero otherwise. The elements in the denominator are the integrated variance (estimated recursively) and noise variance (estimated by the method in Zhang et al, 2005).

The extradiagonal elements of the rRTSCov are the covariances. For their calculation, the data is first synchronized by the refresh time method proposed by Harris et al (1995). It uses the function `refreshTime` to collect first the so-called refresh times at which all assets have traded at least once since the last refresh time point. Suppose we have two log-price series:  $X$  and  $Y$ . Let  $\Gamma = \{\tau_1, \tau_2, \dots, \tau_{N_X^*}\}$  and  $\Theta = \{\theta_1, \theta_2, \dots, \theta_{N_Y^*}\}$  be the set of transaction times of these assets. The first refresh time corresponds to the first time at which both stocks have traded, i.e.  $\phi_1 = \max(\tau_1, \theta_1)$ . The subsequent refresh time is defined as the first time when both stocks have again traded, i.e.  $\phi_{j+1} = \max(\tau_{N_{\phi_j}^X} + 1, \theta_{N_{\phi_j}^Y} + 1)$ . The complete refresh time sample grid is  $\Phi = \{\phi_1, \phi_2, \dots, \phi_{M_N+1}\}$ , where  $M_N$  is the total number of paired returns. The sampling points of asset  $X$  and  $Y$  are defined to be  $t_i = \max\{\tau \in \Gamma : \tau \leq \phi_i\}$  and  $s_i = \max\{\theta \in \Theta : \theta \leq \phi_i\}$ .

Given these refresh times, the covariance is computed as follows:

$$c_N (\{X, Y\}_T^{(K)} - \frac{\bar{n}_K}{\bar{n}_J} \{X, Y\}_T^{(J)}),$$

where

$$\{X, Y\}_T^{(K)} = \frac{1}{K} \frac{\sum_{i=1}^{M_N-K+1} c_i (X_{t_{i+K}} - X_{t_i})(Y_{s_{i+K}} - Y_{s_i}) I_X^K(i; \eta) I_Y^K(i; \eta)}{\frac{1}{M_N-K+1} \sum_{i=1}^{M_N-K+1} I_X^K(i; \eta) I_Y^K(i; \eta)},$$

with  $I_X^K(i; \eta)$  the same jump indicator function as for the variance and  $c_N$  a constant to adjust for the bias due to the thresholding.

Unfortunately, the rRTSCov is not always positive semidefinite. By setting the argument `makePsd = TRUE`, the function `makePsd` is used to return a positive semidefinite matrix. This function replaces the negative eigenvalues with zeroes.



**Value**

an  $N \times N$  matrix

**Author(s)**

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

Boudt K. and Zhang, J. 2010. Jump robust two time scale covariance estimation and realized volatility budgets. Mimeo.

Harris, F., McInish, T., Shoesmith, G., and Wood, R. (1995). Cointegration, error correction, and price discovery on informationally linked security markets. *Journal of Financial and Quantitative Analysis*, 30, 563-581.

Zhang, L., Mykland, P. A., and Ait-Sahalia, Y. (2005). A tale of two time scales: Determining integrated volatility with noisy high-frequency data. *Journal of the American Statistical Association*, 100, 1394-1411.

**See Also**

[ICov](#) for a list of implemented estimators of the integrated covariance.

**Examples**

```
## Not run:
library(xts)
set.seed(123)
start <- strptime("1970-01-01", format = "%Y-%m-%d", tz = "UTC")
timestamps <- start + seq(34200, 57600, length.out = 23401)

dat <- cbind(rnorm(23401) * sqrt(1/23401), rnorm(23401) * sqrt(1/23401))

dat <- exp(cumsum(xts(dat, timestamps)))
price1 <- dat[,1]
price2 <- dat[,2]
rcRTS <- rRTSCov(pData = list(price1, price2))
# Note: List of prices as input
rcRTS

## End(Not run)
```

**Description**

Calculates the daily Realized Variance. Let  $r_{t,i}$  be an intraday return vector with  $i = 1, \dots, M$  number of intraday returns.

Then, the realized variance is given by

$$\text{RVar}_t = \sum_{i=1}^M r_{t,i}^2$$

**Usage**

```
rRVar(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE, ...)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	used internally, do not change.

**Value**

- In case the input is an xts object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in xts format, an xts will be returned.
- If the input data is a data.table object, the function returns a data.table with the same column names as the input data, containing the date and the realized measures.

**See Also**

[IVar](#) for a list of implemented estimators of the integrated variance.

**Examples**

```
rv <- rRVar(sampleOneMinuteData, makeReturns = TRUE)
plot(rv[, DT], rv[, MARKET], xlab = "Date", ylab = "Realized Variance", type = "l")
```

rSemiCov

*Realized semicovariance***Description**

Calculate the Realized Semicovariances (rSemiCov). Let  $r_{t,i}$  be an intraday  $M \times N$  return matrix and  $i = 1, \dots, M$  the number of intraday returns. Then, let  $r_{t,i}^+ = \max(r_{t,i}, 0)$  and  $r_{t,i}^- = \min(r_{t,i}, 0)$ .

Then, the realized semicovariance is given by the following three matrices:

$$\begin{aligned} \text{pos}_t &= \sum_{i=1}^M r_{t,i}^+ r_{t,i}^{+'} \\ \text{neg}_t &= \sum_{i=1}^M r_{t,i}^- r_{t,i}^{-'} \\ \text{mixed}_t &= \sum_{i=1}^M (r_{t,i}^+ r_{t,i}^{-'} + r_{t,i}^- r_{t,i}^{+'}) \end{aligned}$$

The mixed covariance matrix will have 0 on the diagonal. From these three matrices, the realized covariance can be constructed as  $\text{pos} + \text{neg} + \text{mixed}$ . The concordant semicovariance matrix is  $\text{pos} + \text{neg}$ . The off-diagonals of the concordant matrix is always positive, while for the mixed matrix, it is always negative.

**Usage**

```
rSemiCov(
  rData,
  cor = FALSE,
  alignBy = NULL,
  alignPeriod = NULL,
  makeReturns = FALSE
)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
cor	boolean, in case it is TRUE, and the input data is multivariate, the correlation is returned instead of the covariance matrix. FALSE by default.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.

**Details**

In the case that `cor` is `TRUE`, the mixed matrix will be an  $N \times N$  matrix filled with `NA` as mapping the mixed covariance matrix into correlation space is impossible due to the 0-diagonal.

**Value**

In case the data consists of one day a list of five  $N \times N$  matrices are returned. These matrices are named `mixed`, `positive`, `negative`, `concordant`, and `rCov`. The latter matrix corresponds to the realized covariance estimator and is thus named like the function `rCov`. In case the data spans more than one day, the list for each day will be put into another list named according to the date of the estimates.

**Author(s)**

Emil Sjoerup.

**References**

Bollerslev, T., Li, J., Patton, A. J., and Quaedvlieg, R. (2020). Realized semicovariances. *Econometrica*, 88, 1515-1551.

**See Also**

[ICov](#) for a list of implemented estimators of the integrated covariance.

**Examples**

```
# Realized semi-variance/semi-covariance for prices aligned
# at 5 minutes.

# Univariate:
rSVar = rSemiCov(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
                alignPeriod = 5, makeReturns = TRUE)

rSVar
## Not run:
library("xts")
# Multivariate multi day:
rSC <- rSemiCov(sampleOneMinuteData, makeReturns = TRUE) # rSC is a list of lists
# We extract the covariance between stock 1 and stock 2 for all three covariances.
mixed <- sapply(rSC, function(x) x[["mixed"]][1,2])
neg <- sapply(rSC, function(x) x[["negative"]][1,2])
pos <- sapply(rSC, function(x) x[["positive"]][1,2])
covariances <- xts(cbind(mixed, neg, pos), as.Date(names(rSC)))
colnames(covariances) <- c("mixed", "neg", "pos")
# We make a quick plot of the different covariances
plot(covariances)
addLegend(lty = 1) # Add legend so we can distinguish the series.

## End(Not run)
```

---

rSkew	<i>Realized skewness</i>
-------	--------------------------

---

### Description

Calculate the realized skewness, defined in Amaya et al. (2015).

Assume there are  $N$  equispaced returns in period  $t$ . Let  $r_{t,i}$  be a return (with  $i = 1, \dots, N$ ) in period  $t$ . Then, rSkew is given by

$$\text{rSkew}_t = \frac{\sqrt{N} \sum_{i=1}^N (r_{t,i})^3}{(\sum r_{i,t}^2)^{3/2}}.$$

### Usage

```
rSkew(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

### Arguments

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.

### Value

- In case the input is an xts object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in xts format, an xts will be returned.
- If the input data is a data.table object, the function returns a data.table with the same column names as the input data, containing the date and the realized measures.

### Author(s)

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

### References

Amaya, D., Christoffersen, P., Jacobs, K., and Vasquez, A. (2015). Does realized skewness and kurtosis predict the cross-section of equity returns? *Journal of Financial Economics*, 118, 135-167.

**Examples**

```
rs <- rSkew(sampleTData[, list(DT, PRICE)],alignBy ="minutes", alignPeriod =5,
           makeReturns = TRUE)
rs
```

rSV

*DEPRECATED***Description**DEPRECATED USE [rSVar](#)**Usage**

```
rSV(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

**Arguments**

rData	DEPRECATED USE <a href="#">rSVar</a>
alignBy	DEPRECATED USE <a href="#">rSVar</a>
alignPeriod	DEPRECATED USE <a href="#">rSVar</a>
makeReturns	DEPRECATED USE <a href="#">rSVar</a>

rSVar

*Realized semivariance of highfrequency return series***Description**

Calculate the realized semivariances, defined in Barndorff-Nielsen et al. (2008).

Function returns two outcomes:

1. Downside realized semivariance
2. Upside realized semivariance.

Assume there are  $N$  equispaced returns  $r_{t,i}$  in period  $t$ ,  $i = 1, \dots, N$ .

Then, the rSVar is given by

$$\text{rSV}_{\text{downside}_t} = \sum_{i=1}^N (r_{t,i})^2 \times I[r_{t,i} < 0]$$

$$\text{rSV}_{\text{upside}_t} = \sum_{i=1}^N (r_{t,i})^2 \times I[r_{t,i} > 0]$$

**Usage**

```
rSVar(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE, ...)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.
...	used internally

**Value**

list with two entries, the realized positive and negative semivariances

**Author(s)**

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

Barndorff-Nielsen, O. E., Kinnebrock, S., and Shephard N. (2010). *Measuring downside risk: realised semivariance*. In: Volatility and Time Series Econometrics: Essays in Honor of Robert F. Engle, (Edited by Bollerslev, T., Russell, J., and Watson, M.), 117-136. Oxford University Press.

**See Also**

[IVar](#) for a list of implemented estimators of the integrated variance.

**Examples**

```
sv <- rSVar(sampleTData[, list(DT, PRICE)], alignBy = "minutes",  
           alignPeriod = 5, makeReturns = TRUE)  
sv
```

---

rThresholdCov	<i>Threshold Covariance</i>
---------------	-----------------------------

---

### Description

Calculate the threshold covariance matrix proposed in Gobbi and Mancini (2009). Unlike the `rOWCov`, the `rThresholdCov` uses univariate jump detection rules to truncate the effect of jumps on the covariance estimate. As such, it remains feasible in high dimensions, but it is less robust to small cojumps.

Let  $r_{t,i}$  be an intraday  $N \times 1$  return vector of  $N$  assets where  $i = 1, \dots, M$  and  $M$  being the number of intraday returns.

Then, the  $k, q$ -th element of the threshold covariance matrix is defined as

$$\text{thresholdcov}[k, q]_t = \sum_{i=1}^M r_{(k)t,i} \mathbf{1}_{\{r_{(k)t,i}^2 \leq TR_M\}} r_{(q)t,i} \mathbf{1}_{\{r_{(q)t,i}^2 \leq TR_M\}},$$

with the threshold value  $TR_M$  set to  $9\Delta^{-1}$  times the daily realized bi-power variation of asset  $k$ , as suggested in Jacod and Todorov (2009).

### Usage

```
rThresholdCov(
  rData,
  cor = FALSE,
  alignBy = NULL,
  alignPeriod = NULL,
  makeReturns = FALSE,
  ...
)
```

### Arguments

<code>rData</code>	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
<code>cor</code>	boolean, in case it is TRUE, and the input data is multivariate, the correlation is returned instead of the covariance matrix. FALSE by default.
<code>alignBy</code>	character, indicating the time scale in which <code>alignPeriod</code> is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
<code>alignPeriod</code>	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set <code>alignPeriod = 5</code> and <code>alignBy = "minutes"</code> .
<code>makeReturns</code>	boolean, should be TRUE when <code>rData</code> contains prices instead of returns. FALSE by default.
<code>...</code>	used internally, do not change.



**Value**

in case the input is and contains data from one day, an  $N \times N$  matrix is returned. If the data is a univariate xts object with multiple days, an xts is returned. If the data is multivariate and contains multiple days (xts or data.table), the function returns a list containing  $N \times N$  matrices. Each item in the list has a name which corresponds to the date for the matrix.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

- Barndorff-Nielsen, O. and Shephard, N. (2004). Measuring the impact of jumps in multivariate price processes using bipower covariation. Discussion paper, Nuffield College, Oxford University.
- Jacod, J. and Todorov, V. (2009). Testing for common arrival of jumps in discretely-observed multidimensional processes. *Annals of Statistics*, 37, 1792-1838.
- Mancini, C. and Gobbi, F. (2012). Identifying the Brownian covariation from the co-jumps given discrete observations. *Econometric Theory*, 28, 249-273.

**See Also**

[ICov](#) for a list of implemented estimators of the integrated covariance.

**Examples**

```
# Realized threshold Variance/Covariance:
# Multivariate:
## Not run:
library("xts")
set.seed(123)
start <- strptime("1970-01-01", format = "%Y-%m-%d", tz = "UTC")
timestamps <- start + seq(34200, 57600, length.out = 23401)

dat <- cbind(rnorm(23401) * sqrt(1/23401), rnorm(23401) * sqrt(1/23401))

dat <- exp(cumsum(xts(dat, timestamps)))
rcThreshold <- rThresholdCov(dat, alignBy = "minutes", alignPeriod = 1, makeReturns = TRUE)
rcThreshold

## End(Not run)
```

**Description**

Calculate the rTPQuar, defined in Andersen et al. (2012).

Assume there are  $N$  equispaced returns  $r_{t,i}$  in period  $t$ ,  $i = 1, \dots, N$ . Then, the rTPQuar is given by

$$\text{rTPQuar}_t = N \frac{N}{N-2} \left( \frac{\Gamma(0.5)}{2^{2/3} \Gamma(7/6)} \right)^3 \sum_{i=3}^N (|r_{t,i}|^{4/3} |r_{t,i-1}|^{4/3} |r_{t,i-2}|^{4/3})$$

**Usage**

```
rTPQuar(rData, alignBy = NULL, alignPeriod = NULL, makeReturns = FALSE)
```

**Arguments**

rData	an xts or data.table object containing returns or prices, possibly for multiple assets over multiple days.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "secs", "seconds", "mins", "minutes", "hours".
alignPeriod	positive numeric, indicating the number of periods to aggregate over. For example, to aggregate based on a 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
makeReturns	boolean, should be TRUE when rData contains prices instead of returns. FALSE by default.

**Value**

- In case the input is an xts object with data from one day, a numeric of the same length as the number of assets.
- If the input data spans multiple days and is in xts format, an xts will be returned.
- If the input data is a data.table object, the function returns a data.table with the same column names as the input data, containing the date and the realized measures.

**Author(s)**

Giang Nguyen, Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

**References**

Andersen, T. G., Dobrev, D., and Schaumburg, E. (2012). Jump-robust volatility estimation using nearest neighbor truncation. *Journal of Econometrics*, 169, 75-93.

**Examples**

```
tpq <- rTPQuar(rData = sampleTData[, list(DT, PRICE)], alignBy = "minutes",
              alignPeriod = 5, makeReturns = TRUE)
tpq
```

rTSCov

*Two time scale covariance estimation***Description**

Calculate the two time scale covariance matrix proposed in Zhang et al. (2005) and Zhang (2010). By the use of two time scales, this covariance estimate is robust to microstructure noise and non-synchronic trading.

**Usage**

```
rTSCov(
  pData,
  cor = FALSE,
  K = 300,
  J = 1,
  KCov = NULL,
  JCov = NULL,
  KVar = NULL,
  JVar = NULL,
  makePsd = FALSE,
  ...
)
```

**Arguments**

pData	a list. Each list-item $i$ contains an <code>xts</code> object with the intraday price data of stock $i$ for day $t$ .
cor	boolean, in case it is TRUE, and the input data is multivariate, the correlation is returned instead of the covariance matrix. FALSE by default.
K	positive integer, slow time scale returns are computed on prices that are K steps apart.
J	positive integer, fast time scale returns are computed on prices that are J steps apart.
KCov	positive integer, for the extradiagonal covariance elements the slow time scale returns are computed on prices that are K steps apart.
JCov	positive integer, for the extradiagonal covariance elements the fast time scale returns are computed on prices that are J steps apart.
KVar	vector of positive integers, for the diagonal variance elements the slow time scale returns are computed on prices that are K steps apart.
JVar	vector of positive integers, for the diagonal variance elements the fast time scale returns are computed on prices that are J steps apart.
makePsd	boolean, in case it is TRUE, the positive definite version of rTSCov is returned. FALSE by default.
...	used internally, do not change.

### Details

The rTSCov requires the tick-by-tick transaction prices. (Co)variances are then computed using log-returns calculated on a rolling basis on stock prices that are  $K$  (slow time scale) and  $J$  (fast time scale) steps apart.

The diagonal elements of the rTSCov matrix are the variances, computed for log-price series  $X$  with  $n$  price observations at times  $\tau_1, \tau_2, \dots, \tau_n$  as follows:

$$\left(1 - \frac{\bar{n}_K}{\bar{n}_J}\right)^{-1} ([X, X]_T^{(K)} - \frac{\bar{n}_K}{\bar{n}_J} [X, X]_T^{(J)})$$

where  $\bar{n}_K = (n - K + 1)/K$ ,  $\bar{n}_J = (n - J + 1)/J$  and

$$[X, X]_T^{(K)} = \frac{1}{K} \sum_{i=1}^{n-K+1} (X_{t_{i+K}} - X_{t_i})^2.$$

The extradiagonal elements of the rTSCov are the covariances. For their calculation, the data is first synchronized by the refresh time method proposed by Harris et al (1995). It uses the function `refreshTime` to collect first the so-called refresh times at which all assets have traded at least once since the last refresh time point. Suppose we have two log-price series:  $X$  and  $Y$ . Let  $\Gamma = \{\tau_1, \tau_2, \dots, \tau_{N_T^x}\}$  and  $\Theta = \{\theta_1, \theta_2, \dots, \theta_{N_T^y}\}$  be the set of transaction times of these assets. The first refresh time corresponds to the first time at which both stocks have traded, i.e.  $\phi_1 = \max(\tau_1, \theta_1)$ . The subsequent refresh time is defined as the first time when both stocks have again traded, i.e.  $\phi_{j+1} = \max(\tau_{N_{\phi_j}^x+1}, \theta_{N_{\phi_j}^y+1})$ . The complete refresh time sample grid is  $\Phi = \{\phi_1, \phi_2, \dots, \phi_{M_N+1}\}$ , where  $M_N$  is the total number of paired returns. The sampling points of asset  $X$  and  $Y$  are defined to be  $t_i = \max\{\tau \in \Gamma : \tau \leq \phi_i\}$  and  $s_i = \max\{\theta \in \Theta : \theta \leq \phi_i\}$ .

Given these refresh times, the covariance is computed as follows:

$$c_N([X, Y]_T^{(K)} - \frac{\bar{n}_K}{\bar{n}_J} [X, Y]_T^{(J)}),$$

where

$$[X, Y]_T^{(K)} = \frac{1}{K} \sum_{i=1}^{M_N-K+1} (X_{t_{i+K}} - X_{t_i})(Y_{s_{i+K}} - Y_{s_i}).$$

Unfortunately, the rTSCov is not always positive semidefinite. By setting the argument `makePsd = TRUE`, the function `makePsd` is used to return a positive semidefinite matrix. This function replaces the negative eigenvalues with zeroes.

### Value

in case the input is and contains data from one day, an N by N matrix is returned. If the data is a univariate xts object with multiple days, an xts is returned. If the data is multivariate and contains multiple days (xts or data.table), the function returns a list containing N by N matrices. Each item in the list has a name which corresponds to the date for the matrix.

### Author(s)

Jonathan Cornelissen, Kris Boudt, and Emil Sjoerup.

## References

Harris, F., McInish, T., Shoesmith, G., and Wood, R. (1995). Cointegration, error correction, and price discovery on informationally linked security markets. *Journal of Financial and Quantitative Analysis*, 30, 563-581.

Zhang, L., Mykland, P. A., and Ait-Sahalia, Y. (2005). A tale of two time scales: Determining integrated volatility with noisy high-frequency data. *Journal of the American Statistical Association*, 100, 1394-1411.

Zhang, L. (2011). Estimating covariation: Epps effect, microstructure noise. *Journal of Econometrics*, 160, 33-47.

## See Also

[ICov](#) for a list of implemented estimators of the integrated covariance.

## Examples

```
# Robust Realized two timescales Variance/Covariance
# Multivariate:
## Not run:
library(xts)
set.seed(123)
start <- strptime("1970-01-01", format = "%Y-%m-%d", tz = "UTC")
timestamps <- start + seq(34200, 57600, length.out = 23401)

dat <- cbind(rnorm(23401) * sqrt(1/23401), rnorm(23401) * sqrt(1/23401))

dat <- exp(cumsum(xts(dat, timestamps)))
price1 <- dat[,1]
price2 <- dat[,2]
rcovts <- rtSCov(pData = list(price1, price2))
# Note: List of prices as input
rcovts

## End(Not run)
```

---

 RV

 DEPRECATED DEPRECATED USE [rRVar](#)


---

## Description

DEPRECATED DEPRECATED USE [rRVar](#)

## Usage

```
RV(rData)
```

## Arguments

rData                    DEPRECATED USE [rRVar](#)

---

salesCondition      *salesCondition is deprecated. Use tradesCondition instead.*

---

### Description

[salesCondition](#) is deprecated. Use [tradesCondition](#) instead.

### Usage

```
salesCondition(
  tData,
  validConds = c("", "@", "E", "@E", "F", "FI", "@F", "@FI", "I", "@I")
)
```

### Arguments

tData              [salesCondition](#) is deprecated. Use [tradesCondition](#) instead.

validConds        [salesCondition](#) is deprecated. Use [tradesCondition](#) instead.

---

sampleMultiTradeData    *Multivariate tick by tick data*

---

### Description

Cleaned Tick by tick data for a sector ETF, called ETF and two stock components of that ETF, these stocks are named AAA and BBB.

### Usage

```
sampleMultiTradeData
```

### Format

A data.table object

---

sampleOneMinuteData	<i>One minute data</i>
---------------------	------------------------

---

**Description**

One minute data price of one stock and a market proxy. This is data from the US market.

**Usage**

```
sampleOneMinuteData
```

**Format**

A data.table object

---

sampleQData	<i>Sample of cleaned quotes for stock XXX for 2 days measured in microseconds</i>
-------------	---

---

**Description**

A data.table object containing the quotes for the pseudonymized stock XXX for 2 days. This is the cleaned version of the data sample [sampleQDataRaw](#), using quotesCleanup.

**Usage**

```
sampleQData
```

**Format**

data.table object

**Examples**

```
## Not run:  
# The code to create the sampleQData dataset from raw data is  
sampleQData <- quotesCleanup(qDataRaw = sampleQDataRaw,  
                             exchanges = "N", type = "standard", report = FALSE)  
  
## End(Not run)
```

---

sampleQDataRaw	<i>Sample of raw quotes for stock XXX for 2 days measured in microseconds</i>
----------------	---

---

**Description**

A data.table object containing the raw quotes the pseudonymized stock XXX for 2 days, in the typical NYSE TAQ database format.

**Usage**

```
sampleQDataRaw
```

**Format**

```
data.table object
```

---

sampleTData	<i>Sample of cleaned trades for stock XXX for 2 days</i>
-------------	--

---

**Description**

A data.table object containing the trades for the pseudonymized stock XXX for 2 days, in the typical NYSE TAQ database format. This is the cleaned version of the data sample [sampleTDataRaw](#), using [tradesCleanupUsingQuotes](#).

**Usage**

```
sampleTData
```

**Format**

A data.table object.

**Examples**

```
## Not run:
# The code to create the sampleTData dataset from raw data is
sampleQData <- quotesCleanup(qDataRaw = sampleQDataRaw,
                             exchanges = "N", type = "standard", report = FALSE)

tradesAfterFirstCleaning <- tradesCleanup(tDataRaw = sampleTDataRaw,
                                           exchanges = "N", report = FALSE)

sampleTData <- tradesCleanupUsingQuotes(
  tData = tradesAfterFirstCleaning,
  qData = sampleQData,
```



```

lagQuotes = 0)[, c("DT", "EX", "SYMBOL", "PRICE", "SIZE")]
# Only some columns are included. These are the ones that were historically included.

# For most applications, we recommend aggregating the data at a high frequency
# For example, every second.
aggregated <- aggregatePrice(sampleTData[, list(DT, PRICE)],
                             alignBy = "seconds", alignPeriod = 1)
acf(diff(aggregated[as.Date(DT) == "2018-01-02", PRICE]))
acf(diff(aggregated[as.Date(DT) == "2018-01-03", PRICE]))

signature <- function(x, q){
  res <- x[, (rCov(diff(log(PRICE), lag = q, differences = 1))/q), by = as.Date(DT)]
  return(res[[2]])
}
rvAgg <- matrix(nrow = 100, ncol = 2)
for(i in 1:100) rvAgg[i, ] <- signature(aggregated, i)
plot(rvAgg[,1], type = "l")
plot(rvAgg[,2], type = "l")

## End(Not run)

```

---

sampleTDataEurope	<i>European data</i>
-------------------	----------------------

---

**Description**

Trade data of one stock on one day in the European stock market.

**Usage**

```
sampleTDataEurope
```

**Format**

A data.table object

---

sampleTDataRaw	<i>Sample of raw trades for stock XXX for 2 days</i>
----------------	--

---

**Description**

An imaginary data.table object containing the raw trades the pseudonymized stock XXX for 2 days, in the typical NYSE TAQ database format.

**Usage**

```
sampleTDataRaw
```

**Format**

A data.table object.

---

selectExchange	<i>Retain only data from a single stock exchange</i>
----------------	--

---

**Description**

Filter raw trade data to only contain specified exchanges

**Usage**

```
selectExchange(data, exch = "N")
```

**Arguments**

- |      |  |
|------|--|
| data | an xts or data.table object containing the time series data. The object should have a column "EX", indicating the exchange by its symbol.  |
| exch | The (vector of) symbol(s) of the stock exchange(s) that should be selected. By default the NYSE is chosen (exch = "N"). Other exchange symbols are: <ul style="list-style-type: none"><li>• A: AMEX</li><li>• N: NYSE</li><li>• B: Boston</li><li>• P: Arca</li><li>• C: NSX</li><li>• T/Q: NASDAQ</li><li>• D: NASD ADF and TRF</li><li>• X: Philadelphia</li><li>• I: ISE</li><li>• M: Chicago</li><li>• W: CBOE</li><li>• Z: BATS</li></ul> |

**Value**

xts or data.table object depending on input.

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

---

spotDrift	<i>Spot Drift Estimation</i>
-----------	------------------------------

---

### Description

Function used to estimate the spot drift of intraday (tick) stock prices/returns

### Usage

```
spotDrift(
  data,
  method = "mean",
  alignBy = "minutes",
  alignPeriod = 5,
  marketOpen = "09:30:00",
  marketClose = "16:00:00",
  tz = NULL,
  ...
)
```

### Arguments

data	Can be one of two input types, xts or data.table. It is assumed that the input comprises prices in levels.
method	Which method to be used to estimate the spot-drift. Currently, three methods are available, rolling mean and median as well as the kernel method of Christensen et al. (2018). The kernel is a left hand exponential kernel that will weigh newer observations more heavily than older observations.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	How often should the estimation take place? If alignPeriod is 5 the estimation will be done every fifth unit of alignBy.
marketOpen	Opening time of the market, standard is "09:30:00".
marketClose	Closing time of the market, standard is "16:00:00".
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. We attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC".
...	Additional arguments for the individual methods. See 'Details'.

### Details

The additional arguments for the mean and median methods are:

- periods for the rolling window length which is 5 by default.

- align controls the alignment. The default is "right".

For the kernel mean estimator, the arguments meanBandwidth can be used to control the bandwidth of the drift estimator and the preAverage argument, which can be used to control the pre-averaging horizon. These arguments default to 300 and 5 respectively.

The following estimation methods can be specified in method:

**Rolling window mean ("mean")**

Estimates the spot drift by applying a rolling mean over returns.

$$\hat{\mu}_t = \sum_{t=k}^T \text{mean}(r_{t-k:t}),$$

where  $k$  is the argument periods. Parameters:

- periods how big the window for the estimation should be. The estimator will have periods NAs at the beginning of each trading day.
- align alignment method for returns. Defaults to "left", which includes only past data, but other choices, "center" and "right" are available. Warning: These values includes future data.

Outputs:

- mu a matrix containing the spot drift estimates

**Rolling window median ("median")**

Estimates the spot drift by applying a rolling mean over returns.

$$\hat{\mu}_t = \sum_{t=k}^T \text{median}(r_{t-k:t}),$$

where  $k$  is the argument periods. Parameters:

- periods How big the window for the estimation should be. The estimator will have periods NAs at the beginning of each trading day.
- align Alignment method for returns. Defaults to "left", which includes only past data, but other choices, "center" and "right" are available. These values includes FUTURE DATA, so beware!

Outputs:

- mu a matrix containing the spot drift estimates

**kernel spot drift estimator ("kernel")**

$$dX_t = \mu_t dt + \sigma_t dW_t + dJ_t,$$

where  $\mu_t$ ,  $\sigma_t$ , and  $J_t$  are the spot drift, the spot volatility, and a jump process respectively. However, due to microstructure noise, the observed log-price is

$$Y_t = X_t + \varepsilon_t$$

In order to robustify the results to the presence of market microstructure noise, the pre-averaged returns are used:

$$\Delta_i^n \bar{Y} = \sum_{j=1}^{k_n-1} g_j^n \Delta_{i+j}^n Y,$$

where  $g(\cdot)$  is a weighting function,  $\min(x, 1-x)$ , and  $k_n$  is the pre-averaging horizon. The spot drift estimator is then:

$$\hat{\mu}_t^n = \sum_{i=1}^{n-k_n+2} K\left(\frac{t_{i-1}-t}{h_n}\right) \Delta_{i-1}^n \bar{Y},$$

The kernel estimation method has the following parameters:

- `preAverage` a positive integer denoting the length of pre-averaging window for the log-prices. Default is 5
- `meanBandwidth` an integer denoting the bandwidth for the left-sided exponential kernel for the mean. Default is 300L

Outputs:

- `mu` a matrix containing the spot drift estimates

## Value

An object of class "spotDrift" containing at least the estimated spot drift process. Input on what this class should contain and methods for it is welcome.

## Author(s)

Emil Sjoerup.

## References

Christensen, K., Oomen, R., and Reno, R. (2020) The drift burst hypothesis. *Journal of Econometrics*. Forthcoming.

## Examples

```
# Example 1: Rolling mean and median estimators for 2 days
meandrift <- spotDrift(data = sampleTData, alignPeriod = 1)
mediandrift <- spotDrift(data = sampleTData, method = "median",
                        alignBy = "seconds", alignPeriod = 30, tz = "EST")

plot(meandrift)
plot(mediandrift)
## Not run:
# Example 2: Kernel based estimator for one day with data.table format
price <- sampleTData[as.Date(DT) == "2018-01-02", list(DT, PRICE)]
kernelndrift <- spotDrift(sampleTDataEurope, method = "driftKernel",
                        alignBy = "minutes", alignPeriod = 1)

plot(kernelndrift)

## End(Not run)
```

---

spotVol *Spot volatility estimation*

---

### Description

Estimates a wide variety of spot volatility estimators.

### Usage

```
spotVol(
  data,
  method = "detPer",
  alignBy = "minutes",
  alignPeriod = 5,
  marketOpen = "09:30:00",
  marketClose = "16:00:00",
  tz = "GMT",
  ...
)
```

### Arguments

data	Can be one of two input types, xts or data.table. It is assumed that the input comprises prices in levels. Irregularly spaced observations are allowed. They will be aggregated to the level specified by parameters alignBy and alignPeriod.
method	specifies which method will be used to estimate the spot volatility. Valid options are "detPer", "stochPer", "kernel", "piecewise", "garch", "RM", "PARM". See 'Details' below for explanation and parameters to use in each of the methods.
alignBy	character, indicating the time scale in which alignPeriod is expressed. Possible values are: "ticks", "secs", "seconds", "mins", "minutes", "hours"
alignPeriod	positive integer, indicating the number of periods to aggregate over. For example, to aggregate an xts object to the 5-minute frequency, set alignPeriod = 5 and alignBy = "minutes".
marketOpen	the market opening time. This should be in the time zone specified by tz. By default, marketOpen = "09:30:00".
marketClose	the market closing time. This should be in the time zone specified by tz. By default, marketClose = "16:00:00".
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: tz = NULL. We attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use tz if specified, and if it is not specified, we use "UTC"
...	method-specific parameters (see 'Details' below).

## Details

The following estimation methods can be specified in method:

### Deterministic periodicity method ("detPer")

Parameters:

- **dailyVol** A string specifying the estimation method for the daily component  $s_t$ . Possible values are "rBPCov", "rRVar", "rMedRVar". "rBPCov" by default.
- **periodicVol** A string specifying the estimation method for the component of intraday volatility, that depends in a deterministic way on the intraday time at which the return is observed. Possible values are "SD", "WSD", "TML", "OLS". See Boudt et al. (2011) for details. Default = "TML".
- **P1** A positive integer corresponding to the number of cosine terms used in the flexible Fourier specification of the periodicity function, see Andersen et al. (1997) for details. Default = 5.
- **P2** Same as P1, but for the sine terms. Default = 5.
- **dummies** Boolean: in case it is TRUE, the parametric estimator of periodic standard deviation specifies the periodicity function as the sum of dummy variables corresponding to each intraday period. If it is FALSE, the parametric estimator uses the flexible Fourier specification. Default is FALSE.

Outputs (see 'Value' for a full description of each component):

- spot
- daily
- periodic

Let there be  $T$  days of  $N$  equally-spaced log-returns  $r_{i,t}$ ,  $i = 1, \dots, N$  and  $t = 1, \dots, T$ . In case of method = "detPer", the returns are modeled as

$$r_{i,t} = f_i s_t u_{i,t}$$

with independent  $u_{i,t} \sim \mathcal{N}(0, 1)$ . The spot volatility is decomposed into a deterministic periodic factor  $f_i$  (identical for every day in the sample) and a daily factor  $s_t$  (identical for all observations within a day). Both components are then estimated separately, see Taylor and Xu (1997) and Andersen and Bollerslev (1997). The jump robust versions by Boudt et al. (2011) have also been implemented.

If periodicVol = "SD", we have

$$\hat{f}_i^{SD} = \frac{SD_i}{\sqrt{\frac{1}{[\lambda/\Delta]} \sum_{j=1}^N SD_j^2}}$$

with  $\Delta = 1/N$ , cross-daily averages  $SD_i = \sqrt{1/T \sum_{t=1}^T r_{i,t}^2}$ , and  $\lambda$  being the length of the intraday time intervals.

If periodicVol = "WSD", we have another nonparametric estimator that is robust to jumps in contrast to periodicVol = "SD". The definition of this estimator can be found in Boudt et al. (2011, Eqs. 2.9-2.12).

The estimates when `periodicVol = "OLS"` and `periodicVol = "TML"` are based on the regression equation

$$\log \left| \frac{1}{T} \sum_{t=1}^T r_{i,t} \right| - c = \log f_i + \varepsilon_i$$

with *i.i.d.* zero-mean error term  $\varepsilon_i$  and  $c = -0.63518$ . `periodicVol = "OLS"` employs ordinary-least-squares estimation and `periodicVol = "TML"` truncated maximum-likelihood estimation (see Boudt et al., 2011, Section 2.2, for further details).

### Stochastic periodicity method ("stochPer")

Parameters:

- `P1`: A positive integer corresponding to the number of cosine terms used in the flexible Fourier specification of the periodicity function. Default = 5.
- `P2`: Same as `P1`, but for the sine terms. Default = 5.
- `init`: A named list of initial values to be used in the optimization routine ("BFGS" in `optim`). Default = `list(sigma = 0.03, sigma_mu = 0.005, sigma_h = 0.005, sigma_k = 0.05, phi = 0.2, rho = 0.98, mu = c(2, -0.5), delta_c = rep(0, max(1, P1)), delta_s = rep(0, max(1, P2)))`. The naming of the parameters follows Beltratti and Morana (2001), the corresponding model equations are listed below. `init` can contain any number of these parameters. For parameters not specified in `init`, the default initial value will be used.
- `control`: A list of options to be passed down to `optim`.

Outputs (see 'Value' for a full description of each component):

- `spot`
- `par`

This method by Beltratti and Morana (2001) assumes the periodicity factor to be stochastic. The spot volatility estimation is split into four components: a random walk, an autoregressive process, a stochastic cyclical process and a deterministic cyclical process. The model is estimated using a quasi-maximum likelihood method based on the Kalman Filter. The package `FKF` is used to apply the Kalman filter. In addition to the spot volatility estimates, all parameter estimates are returned.

The model for the intraday change in the return series is given by

$$r_{t,n} = \sigma_{t,n} \varepsilon_{t,n}, \quad t = 1, \dots, T; \quad n = 1, \dots, N,$$

where  $\sigma_{t,n}$  is the conditional standard deviation of the  $n$ -th interval of day  $t$  and  $\varepsilon_{t,n}$  is a *i.i.d.* mean-zero unit-variance process. The conditional standard deviations are modeled as

$$\sigma_{t,n} = \sigma \exp \left( \frac{\mu_{t,n} + h_{t,n} + c_{t,n}}{2} \right)$$

with  $\sigma$  being a scaling factor and  $\mu_{t,n}$  is the non-stationary volatility component

$$\mu_{t,n} = \mu_{t,n-1} + \xi_{t,n}$$

with independent  $\xi_{t,n} \sim \mathcal{N}(0, \sigma_\xi^2)$ .  $h_{t,n}$  is the stochastic stationary acyclical volatility component

$$h_{t,n} = \phi h_{t,n-1} + \nu_{t,n}$$



with independent  $\eta_{t,n} \sim \mathcal{N}(0, \sigma_\eta^2)$  and  $|\phi| \leq 1$ . The cyclical component is separated in two components:

$$c_{t,n} = c_{1,t,n} + c_{2,t,n}$$

The first component is written in state-space form,

$$\begin{pmatrix} c_{1,t,n} \\ c_{1,t,n}^* \end{pmatrix} = \rho \begin{pmatrix} \cos \lambda & \sin \lambda \\ -\sin \lambda & \cos \lambda \end{pmatrix} \begin{pmatrix} c_{1,t,n-1} \\ c_{1,t,n-1}^* \end{pmatrix} + \begin{pmatrix} \kappa_{1,t,n} \\ \kappa_{1,t,n}^* \end{pmatrix}$$

with  $0 \leq \rho \leq 1$  and  $\kappa_{1,t,n}, \kappa_{1,t,n}^*$  are mutually independent zero-mean normal random variables with variance  $\sigma_\kappa^2$ . All other parameters and the process  $c_{1,t,n}^*$  in the state-space representation are only of instrumental use and are not part of the return value which is why we won't introduce them in detail in this vignette; see Beltratti and Morana (2001, pp. 208-209) for more information.

The second component is given by

$$c_{2,t,n} = \mu_1 n_1 + \mu_2 n_2 + \sum_{p=2}^P (\delta_{cp} \cos(p\lambda) + \delta_{sp} \sin(p\lambda n))$$

with  $n_1 = 2n/(N+1)$  and  $n_2 = 6n^2/(N+1)/(N+2)$ .

### Nonparametric filtering ("kernel")

Parameters:

- type String specifying the type of kernel to be used. Options include "gaussian", "epanechnikov", "beta". Default = "gaussian".
- h Scalar or vector specifying bandwidth(s) to be used in kernel. If h is a scalar, it will be assumed equal throughout the sample. If it is a vector, it should contain bandwidths for each day. If left empty, it will be estimated. Default = NULL.
- est String specifying the bandwidth estimation method. Possible values include "cv", "quarticity". Method "cv" equals cross-validation, which chooses the bandwidth that minimizes the Integrated Square Error. "quarticity" multiplies the simple plug-in estimator by a factor based on the daily quarticity of the returns. est is obsolete if h has already been specified by the user. "cv" by default.
- lower Lower bound to be used in bandwidth optimization routine, when using cross-validation method. Default is  $0.1n^{-0.2}$ .
- upper Upper bound to be used in bandwidth optimization routine, when using cross-validation method. Default is  $n^{-0.2}$ .

Outputs (see 'Value' for a full description of each component):

- spot
- par

This method by Kristensen (2010) filters the spot volatility in a nonparametric way by applying kernel weights to the standard realized volatility estimator. Different kernels and bandwidths can be used to focus on specific characteristics of the volatility process.

Estimation results heavily depend on the bandwidth parameter  $h$ , so it is important that this parameter is well chosen. However, it is difficult to come up with a method that determines the optimal bandwidth for any kind of data or kernel that can be used. Although some estimation methods

are provided, it is advised that you specify  $h$  yourself, or make sure that the estimation results are appropriate.

One way to estimate  $h$ , is by using cross-validation. For each day in the sample,  $h$  is chosen as to minimize the Integrated Square Error, which is a function of  $h$ . However, this function often has multiple local minima, or no minima at all ( $h \rightarrow \infty$ ). To ensure a reasonable optimum is reached, strict boundaries have to be imposed on  $h$ . These can be specified by `lower` and `upper`, which by default are  $0.1n^{-0.2}$  and  $n^{-0.2}$  respectively, where  $n$  is the number of observations in a day.

When using the method "kernel", in addition to the spot volatility estimates, all used values of the bandwidth  $h$  are returned.

A formal definition of the estimator is too extensive for the context of this vignette. Please refer to Kristensen (2010) for more detailed information. Our parameter names are aligned with this reference.

### **Piecewise constant volatility ("piecewise")**

Parameters:

- `type` string specifying the type of test to be used. Options include "MDa", "MDb", "DM". See Fried (2012) for details. Default = "MDa".
- `m` number of observations to include in reference window. Default = 40.
- `n` number of observations to include in test window. Default = 20.
- `alpha` significance level to be used in tests. Note that the test will be executed many times (roughly equal to the total number of observations), so it is advised to use a small value for `alpha`, to avoid a lot of false positives. Default = 0.005.
- `volEst` string specifying the realized volatility estimator to be used in local windows. Possible values are "rBPCov", "rRVar", "rMedRVar". Default = "rBPCov".
- `online` boolean indicating whether estimations at a certain point  $t$  should be done online (using only information available at  $t - 1$ ), or ex post (using all observations between two change points). Default = TRUE.

Outputs (see 'Value' for a full description of each component):

- `spot`
- `cp`

This nonparametric method by Fried (2012) is a two-step approach and assumes the volatility to be piecewise constant over local windows. Robust two-sample tests are applied to detect changes in variability between subsequent windows. The spot volatility can then be estimated by evaluating regular realized volatility estimators within each local window. "MDa", "MDb" refer to different test statistics, see Section 2.2 in Fried (2012).

Along with the spot volatility estimates, this method will return the detected change points in the volatility level. When plotting a `spotVol` object containing `cp`, these change points will be visualized.

### **GARCH models with intraday seasonality ("garch")**

Parameters:

- `model` string specifying the type of test to be used. Options include "sGARCH", "eGARCH". See `ugarchspec` in the `rugarch` package. Default = "eGARCH".

- `garchorder` numeric value of length 2, containing the order of the GARCH model to be estimated. Default = `c(1, 1)`.
- `dist` string specifying the distribution to be assumed on the innovations. See `distribution.model` in `ugarchspec` for possible options. Default = "norm".
- `solver.control` list containing solver options. See `ugarchfit` for possible values. Default = `list()`.
- `P1` a positive integer corresponding to the number of cosine terms used in the flexible Fourier specification of the periodicity function. Default = 5.
- `P2` same as `P1`, but for the sinus terms. Default = 5.

Outputs (see 'Value' for a full description of each component):

- `spot`
- `ugarchfit`

Along with the spot volatility estimates, this method will return the `ugarchfit` object used by the `rugarch` package.

In this model, daily returns  $r_t$  based on intraday observations  $r_{i,t}, i = 1, \dots, N$  are modeled as

$$r_t = \sum_{i=1}^N r_{i,t} = \sigma_t \frac{1}{\sqrt{N}} \sum_{i=1}^N s_i Z_{i,t}.$$

with  $\sigma_t > 0$ , intraday seasonality  $s_i > 0$ , and  $Z_{i,t}$  being a zero-mean unit-variance error term.

The overall approach is as in Appendix B of Andersen and Bollerslev (1997). This method generates the external regressors  $s_i$  needed to model the intraday seasonality with a flexible Fourier form (Andersen and Bollerslev, 1997, Eqs. A.1-A.4). The `rugarch` package is then employed to estimate the specified intraday GARCH(1,1) model on the residuals  $r_{i,t}/s_i$ .

### Realized Measures ("RM")

This estimator takes trailing rolling window observations of intraday returns to estimate the spot volatility.

Parameters:

- `RM` string denoting which realized measure to use to estimate the local volatility. Possible values are: "rBPCov", "rMedRVar", "rMinRVar", "rCov", "rRVar". Default = "rBPCov".
- `lookBackPeriod` positive integer denoting the amount of sub-sampled returns to use for the estimation of the local volatility. Default is 10.
- `dontIncludeLast` logical indicating whether to omit the last return in the calculation of the local volatility. This is done in Lee-Mykland (2008) to produce jump-robust estimates of spot volatility. Setting this to TRUE will then use `lookBackPeriod - 1` returns in the construction of the realized measures. Default = FALSE.

Outputs (see 'Value' for a full description of each component):

- `spot`
- `RM`
- `lookBackPeriod`

This method returns the estimates of the spot volatility, a string containing the realized measure used, and the lookBackPeriod.

#### **(Non-overlapping) Pre-Averaged Realized Measures ("PARM")**

This estimator takes rolling historical window observations of intraday returns to estimate the spot volatility as in the option "RM" but adds return pre-averaging of the realized measures. For a description of return pre-averaging see the details on [spotDrift](#).

Parameters:

- RM String denoting which realized measure to use to estimate the local volatility. Possible values are: "rBPCov", "rMedRVar", "rMinRVar", "rCov", and "rRVar". Default = "rBPCov".
- lookBackPeriod positive integer denoting the amount of sub-sampled returns to use for the estimation of the local volatility. Default = 50.

Outputs (see 'Value' for a full description of each component):

- spot
- RM
- lookBackPeriod
- kn

#### **Value**

A spotVol object, which is a list containing one or more of the following outputs, depending on the method used:

- spot  
An xts or matrix object (depending on the input) containing spot volatility estimates  $\sigma_{t,i}$ , reported for each interval  $i$  between marketOpen and marketClose for every day  $t$  in data. The length of the intervals is specified by alignPeriod and alignBy. Methods that provide this output: All.
- daily  
An xts or numeric object (depending on the input) containing estimates of the daily volatility levels for each day  $t$  in data, if the used method decomposed spot volatility into a daily and an intraday component. Methods that provide this output: "detPer".
- periodic  
An xts or numeric object (depending on the input) containing estimates of the intraday periodicity factor for each day interval  $i$  between marketOpen and marketClose, if the spot volatility was decomposed into a daily and an intraday component. If the output is in xts format, this periodicity factor will be dated to the first day of the input data, but it is identical for each day in the sample. Methods that provide this output: "detPer".
- par  
A named list containing parameter estimates, for methods that estimate one or more parameters. Methods that provide this output: "stochper", "kernel".
- cp  
A vector containing the change points in the volatility, i.e. the observation indices after which the volatility level changed, according to the applied tests. The vector starts with a 0. Methods that provide this output: "piecewise".

- ugarchfit

A ugarchfit object, as used by the rugarch package, containing all output from fitting the GARCH model to the data. Methods that provide this output: "garch".

The spotVol function offers several methods to estimate spot volatility and its intraday seasonality, using high-frequency data. It returns an object of class spotVol, which can contain various outputs, depending on the method used. See 'Details' for a description of each method. In any case, the output will contain the spot volatility estimates.

The input can consist of price data or return data, either tick by tick or sampled at set intervals. The data will be converted to equispaced high-frequency returns  $r_{t,i}$  (read: the  $i$ -th return on day  $t$ ).

### Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

### References

Andersen, T. G. and Bollerslev, T. (1997). Intraday periodicity and volatility persistence in financial markets. *Journal of Empirical Finance*, 4, 115-158.

Beltratti, A. and Morana, C. (2001). Deterministic and stochastic methods for estimation of intraday seasonal components with high frequency data. *Economic Notes*, 30, 205-234.

Boudt K., Croux C., and Laurent S. (2011). Robust estimation of intraweek periodicity in volatility and jump detection. *Journal of Empirical Finance*, 18, 353-367.

Fried, R. (2012). On the online estimation of local constant volatilities. *Computational Statistics and Data Analysis*, 56, 3080-3090.

Kristensen, D. (2010). Nonparametric filtering of the realized spot volatility: A kernel-based approach. *Econometric Theory*, 26, 60-93.

Taylor, S. J. and Xu, X. (1997). The incremental volatility information in one million foreign exchange quotations. *Journal of Empirical Finance*, 4, 317-340.

### Examples

```
## Not run:
init <- list(sigma = 0.03, sigma_mu = 0.005, sigma_h = 0.007,
            sigma_k = 0.06, phi = 0.194, rho = 0.986, mu = c(1.87, -0.42),
            delta_c = c(0.25, -0.05, -0.2, 0.13, 0.02),
            delta_s = c(-1.2, 0.11, 0.26, -0.03, 0.08))

# Next method will take around 370 iterations
vol1 <- spotVol(sampleOneMinuteData[, list(DT, PRICE = MARKET)], method = "stochPer", init = init)
plot(vol1$spot[1:780])
legend("topright", c("stochPer"), col = c("black"), lty=1)
## End(Not run)

# Various kernel estimates
## Not run:
h1 <- bw.nrd0((1:nrow(sampleOneMinuteData[, list(DT, PRICE = MARKET)]))*60)
vol2 <- spotVol(sampleOneMinuteData[, list(DT, PRICE = MARKET)],
```

```

        method = "kernel", h = h1)
vol3 <- spotVol(sampleOneMinuteData[, list(DT, PRICE = MARKET)],
               method = "kernel", est = "quarticity")
vol4 <- spotVol(sampleOneMinuteData[, list(DT, PRICE = MARKET)],
               method = "kernel", est = "cv")
plot(cbind(vol2$spot, vol3$spot, vol4$spot))
xts::addLegend("topright", c("h = simple estimate", "h = quarticity corrected",
                             "h = crossvalidated"), col = 1:3, lty=1)

## End(Not run)

# Piecewise constant volatility
## Not run:
vol5 <- spotVol(sampleOneMinuteData[, list(DT, PRICE = MARKET)],
               method = "piecewise", m = 200, n = 100, online = FALSE)
plot(vol5)
## End(Not run)

# Compare regular GARCH(1,1) model to eGARCH, both with external regressors
## Not run:
vol6 <- spotVol(sampleOneMinuteData[, list(DT, PRICE = MARKET)], method = "garch", model = "sGARCH")
vol7 <- spotVol(sampleOneMinuteData[, list(DT, PRICE = MARKET)], method = "garch", model = "eGARCH")
plot(as.numeric(t(vol6$spot)), type = "l")
lines(as.numeric(t(vol7$spot)), col = "red")
legend("topleft", c("GARCH", "eGARCH"), col = c("black", "red"), lty = 1)

## End(Not run)

## Not run:
# Compare realized measure spot vol estimation to pre-averaged version
vol8 <- spotVol(sampleTDataEurope[, list(DT, PRICE)], method = "RM", marketOpen = "09:00:00",
               marketClose = "17:30:00", tz = "UTC", alignPeriod = 1, alignBy = "mins",
               lookBackPeriod = 10)
vol9 <- spotVol(sampleTDataEurope[, list(DT, PRICE)], method = "PARM", marketOpen = "09:00:00",
               marketClose = "17:30:00", tz = "UTC", lookBackPeriod = 10)
plot(zoo::na.locf(cbind(vol8$spot, vol9$spot)))

## End(Not run)

```

---

spreadPrices

---

*Convert to format for realized measures*


---

## Description

Convenience function to split data from one xts or data.table with at least "DT", "SYMBOL", and "PRICE" columns to a format that can be used in the functions for calculation of realized measures. This is the opposite of [gatherPrices](#).

## Usage

```
spreadPrices(data)
```

**Arguments**

`data` An `xts` or a `data.table` object with at least "DT", "SYMBOL", and "PRICE" columns. This data should already be cleaned.

**Value**

An `xts` or a `data.table` object with columns "DT" and a column named after each unique entrance in the "SYMBOL" column of the input. These columns contain the price of the associated symbol. We drop all other columns, e.g. SIZE.

**Author(s)**

Emil Sjoerup.

**See Also**

[gatherPrices](#)

**Examples**

```
## Not run:
library(data.table)
data1 <- copy(sampleTData)[, `:=`(PRICE = PRICE * runif(.N, min = 0.99, max = 1.01),
                               DT = DT + runif(.N, 0.01, 0.02))]
data2 <- copy(sampleTData)[, SYMBOL := 'XYZ']

dat <- rbind(data1, data2)
setkey(dat, "DT")
dat <- spreadPrices(dat)

rCov(dat, alignBy = 'minutes', alignPeriod = 5, makeReturns = TRUE, cor = TRUE)

## End(Not run)
```

---

SPYRM

*SPY realized measures*

---

**Description**

Realized measures for the SPY ETF calculated at 1 and 5 minute sampling.

**Usage**

```
SPYRM
```

**Format**

A `data.table` object

**Note**

The CLOSE column is NOT the official close price, but simply the last recorded price of the day. Thus, this may be slightly different from other sources.

---

summary.HARmodel	<i>Summary for HARmodel objects</i>
------------------	-------------------------------------

---

**Description**

Summary for HARmodel objects

**Usage**

```
## S3 method for class 'HARmodel'
summary(object, ...)
```

**Arguments**

object	An object of class HARmodel
...	pass lag to determine the maximum order of the Newey West estimator. Default is 22

**Value**

A modified summary.lm

---

tradesCleanup	<i>Cleans trade data</i>
---------------	--------------------------

---

**Description**

This is a wrapper function for cleaning the trade data of all stock data inside the folder dataSource. The result is saved in the folder dataDestination.

In case you supply the argument rawtData, the on-disk functionality is ignored. The function returns a vector indicating how many trades were removed at each cleaning step in this case. and the function returns an xts or data.table object.

The following cleaning functions are performed sequentially: [noZeroPrices](#), [autoSelectExchangeTrades](#) or [selectExchange](#), [tradesCondition](#), and [mergeTradesSameTimestamp](#).

Since the function [rmTradeOutliersUsingQuotes](#) also requires cleaned quote data as input, it is not incorporated here and there is a separate wrapper called [tradesCleanupUsingQuotes](#).



**Usage**

```
tradesCleanup(
  dataSource = NULL,
  dataDestination = NULL,
  exchanges = "auto",
  tDataRaw = NULL,
  report = TRUE,
  selection = "median",
  validConds = c("", "@", "E", "@E", "F", "FI", "@F", "@FI", "I", "@I"),
  marketOpen = "09:30:00",
  marketClose = "16:00:00",
  printExchange = TRUE,
  saveAsXTS = FALSE,
  tz = NULL
)
```

**Arguments**

dataSource	character indicating the folder in which the original data is stored.
dataDestination	character indicating the folder in which the cleaned data is stored.
exchanges	vector of stock exchange symbols for all data in dataSource, e.g. exchanges = c("T", "N") retrieves all stock market data from both NYSE and NASDAQ. The possible exchange symbols are: <ul style="list-style-type: none"> <li>• A: AMEX</li> <li>• N: NYSE</li> <li>• B: Boston</li> <li>• P: Arca</li> <li>• C: NSX</li> <li>• T/Q: NASDAQ</li> <li>• D: NASD ADF and TRF</li> <li>• X: Philadelphia</li> <li>• I: ISE</li> <li>• M: Chicago</li> <li>• W: CBOE</li> <li>• Z: BATS</li> </ul> <p>The default value is "auto" which automatically selects the exchange for the stocks and days independently using the <a href="#">autoSelectExchangeTrades</a></p>
tDataRaw	xts object containing raw trade data. This argument is NULL by default. Enabling it means the arguments from, to, dataSource and dataDestination will be ignored (only advisable for small chunks of data).
report	boolean and TRUE by default. In case it is true the function returns (also) a vector indicating how many trades remained after each cleaning step.
selection	argument to be passed on to the cleaning routine <a href="#">mergeTradesSameTimestamp</a> . The default is "median".

validConds	character vector containing valid sales conditions. Passed through to <code>tradesCondition</code> .
marketOpen	character in the format of "HH:MM:SS", specifying the opening time of the exchange(s).
marketClose	character in the format of "HH:MM:SS", specifying the closing time of the exchange(s).
printExchange	Argument passed to <code>autoSelectExchangeTrades</code> indicates whether the chosen exchange is printed on the console, default is TRUE. This is only used when exchanges is "auto"
saveAsXTS	indicates whether data should be saved in xts format instead of <code>data.table</code> when using on-disk functionality. FALSE by default.
tz	fallback time zone used in case we are unable to identify the timezone of the data, by default: <code>tz = NULL</code> . With the non-disk functionality, we attempt to extract the timezone from the DT column (or index) of the data, which may fail. In case of failure we use <code>tz</code> if specified, and if it is not specified, we use "UTC". In the on-disk functionality, if <code>tz</code> is not specified, the timezone used will be the system default.

## Details

Using the on-disk functionality with `.csv.zip` files from the WRDS database will write temporary files on your machine in order to unzip the files - we try to clean up after it, but cannot guarantee that there won't be files that slip through the crack if the permission settings on your machine does not match ours.

If the input `data.table` does not contain a DT column but it does contain DATE and TIME\_M columns, we create the DT column by REFERENCE, altering the `data.table` that may be in the user's environment.

## Value

For each day an `xts` or `data.table` object is saved into the folder of that date, containing the cleaned data. This procedure is performed for each stock in "ticker". The function returns a vector indicating how many trades remained after each cleaning step.

In case you supply the argument `rawtData`, the on-disk functionality is ignored and the function returns a list with the cleaned trades as `xts` object (see examples).

## Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup

## References

- Barndorff-Nielsen, O. E., Hansen, P. R., Lunde, A., and Shephard, N. (2009). Realized kernels in practice: Trades and quotes. *Econometrics Journal*, 12, C1-C32.
- Brownlees, C.T. and Gallo, G.M. (2006). Financial econometric analysis at ultra-high frequency: Data handling concerns. *Computational Statistics & Data Analysis*, 51, 2232-2245.

**Examples**

```
# Consider you have raw trade data for 1 stock for 2 days
head(sampleTDataRaw)
dim(sampleTDataRaw)
tDataAfterFirstCleaning <- tradesCleanup(tDataRaw = sampleTDataRaw,
                                         exchanges = list("N"))

tDataAfterFirstCleaning$report
dim(tDataAfterFirstCleaning$tData)
# In case you have more data it is advised to use the on-disk functionality
# via "dataSource" and "dataDestination" arguments
```

---

tradesCleanupUsingQuotes

*Perform a final cleaning procedure on trade data*

---

**Description**

Function performs cleaning procedure [rmTradeOutliersUsingQuotes](#) for the trades of all stocks data in "dataDestination". Note that preferably the input data for this function is trade and quote data cleaned by respectively e.g. [tradesCleanup](#) and [quotesCleanup](#).

**Usage**

```
tradesCleanupUsingQuotes(
  tradeDataSource = NULL,
  quoteDataSource = NULL,
  dataDestination = NULL,
  tData = NULL,
  qData = NULL,
  lagQuotes = 0,
  nSpreads = 1,
  BFM = FALSE,
  backwardsWindow = 3600,
  forwardsWindow = 0.5,
  plot = FALSE
)
```

**Arguments**

**tradeDataSource**  
character indicating the folder in which the original trade data is stored.

**quoteDataSource**  
character indicating the folder in which the original quote data is stored.

**dataDestination**  
character indicating the folder in which the cleaned data is stored, folder of **dataSource** by default.

tData	data.table or xts object containing trade data cleaned by <code>tradesCleanup</code> . This argument is NULL by default. Enabling it, means the arguments from, to, dataSource and dataDestination will be ignored (only advisable for small chunks of data).
qData	data.table or xts object containing cleaned quote data. This argument is NULL by default. Enabling it means the arguments from, to, dataSource, dataDestination will be ignored (only advisable for small chunks of data).
lagQuotes	numeric, number of seconds the quotes are registered faster than the trades (should be round and positive). Default is 0. For older datasets, i.e. before 2010, it may be a good idea to set this to, e.g., 2 (see, Vergote, 2005).
nSpreads	numeric of length 1 denotes how far above the offer and below bid we allow outliers to be. Trades are filtered out if they are MORE THAN nSpread * spread above (below) the offer (bid)
BFM	a logical determining whether to conduct "Backwards - Forwards matching" of trades and quotes. The algorithm tries to match trades that fall outside the bid - ask and first tries to match a small window forwards and if this fails, it tries to match backwards in a bigger window. The small window is a tolerance for inaccuracies in the timestamps of bids and asks. The backwards window allow for matching of late reported trades, i.e. block trades.
backwardsWindow	a numeric denoting the length of the backwards window used when BFM = TRUE. Default is 3600, corresponding to one hour.
forwardsWindow	a numeric denoting the length of the forwards window used when BFM = TRUE. Default is 0.5, corresponding to one half second.
plot	a logical denoting whether to visualize the forwards, backwards, and unmatched trades in a plot. Passed on to <code>rmTradeOutliersUsingQuotes</code>

### Details

In case you supply the arguments tData and qData, the on-disk functionality is ignored and the function returns cleaned trades as a data.table or xts object (see examples).

When using the on-disk functionality and tradeDataSource and quoteDataSource are the same, the quote files are all files in the folder that contains 'quote', and the rest are treated as containing trade data.

### Value

For each day an xts object is saved into the folder of that date, containing the cleaned data.

### Author(s)

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

### References

Barndorff-Nielsen, O. E., Hansen, P. R., Lunde, A., and Shephard, N. (2009). Realized kernels in practice: Trades and quotes. *Econometrics Journal*, 12, C1-C32.

Brownlees, C.T., and Gallo, G.M. (2006). Financial econometric analysis at ultra-high frequency: Data handling concerns. *Computational Statistics & Data Analysis*, 51, 2232-2245.

Christensen, K., Oomen, R. C. A., Podolskij, M. (2014): Fact or Friction: Jumps at ultra high frequency. *Journal of Financial Economics*, 144, 576-599

### Examples

```
# Consider you have raw trade data for 1 stock for 2 days
tDataAfterFirstCleaning <- tradesCleanup(tDataRow = sampleTDataRow,
                                         exchanges = "N", report = FALSE)
qData <- quotesCleanup(qDataRow = sampleQDataRow,
                      exchanges = "N", report = FALSE)
dim(tDataAfterFirstCleaning)
tDataAfterFinalCleaning <-
  tradesCleanupUsingQuotes(qData = qData[as.Date(DT) == "2018-01-02"],
                          tData = tDataAfterFirstCleaning[as.Date(DT) == "2018-01-02"])
dim(tDataAfterFinalCleaning)
# In case you have more data it is advised to use the on-disk functionality
# via the "tradeDataSource", "quoteDataSource", and "dataDestination" arguments
```

---

tradesCondition	<i>Delete entries with abnormal trades condition.</i>
-----------------	---

---

### Description

Delete entries with abnormal trades condition

### Usage

```
tradesCondition(
  tData,
  validConds = c("", "@", "E", "@E", "F", "FI", "@F", "@FI", "I", "@I")
)
```

### Arguments

tData	an xts or data.table object containing the time series data, with one column named "COND" indicating the Sale Condition.
validConds	a character vector containing valid sales conditions defaults to c(' ', '@', 'E', '@E', 'F', 'FI', '@F', '@FI', 'I', '@I'). See details.

### Details

To get more information on the sales conditions, see the NYSE documentation. Section about Daily TAQ Trades File. The current version (as of May 2020) can be found online at [NYSE's webpage](#)

### Value

xts or data.table object depending on input.

**Note**

Some CSV readers and the WRDS API parses empty strings as NAs. We transform NA values in COND to "".

**Author(s)**

Jonathan Cornelissen, Kris Boudt, Onno Kleen, and Emil Sjoerup.

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